Recurrent Neural Networks (RNNs) CSC413H1S 2021 Tutorial 7

Slides by: Ian Shi

Many domains feature sequences of data with temporal dependencies:

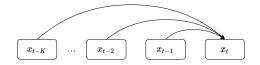
- Natural Language Processing (NLP)
- Time series forecasting (Healthcare, Finance, etc.)

Common tasks:

- Predict the next value in a sequence
- Convert data sequence to equivalent sequence in another space (translation)
- Classify the entire sequence into specific class.

How do we model data which contains time dependency?

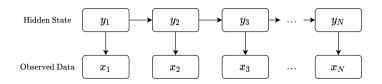
Autoregressive methods: Predict next data observation as a linear equation of previously observed data points.



• Ex:
$$x_t = w_1 * x_{t-1} + w_2 * x_{t-2} + \dots + w_K * x_{t-K}$$

• Representational ability is limited. Only looks K steps back in time!

Hidden Markov Models (CSC412)



Use a hidden state to represent higher level information about sequence:

• Ex: If we're modelling a sequence of temperature measurements, attempt to encode information about season into hidden state.

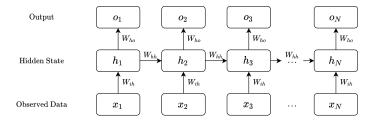
Limitations

- Updates between hidden states generally have to be linear
- Makes Markov assumptions (no long term dependencies possible)

Recurrent Neural Networks (RNNs) offer several advantages:

- Non-linear hidden state updates allows high representational power.
- Can represent long term dependencies in hidden state (theoretically).
- Shared weights, can be used on sequences of arbitrary length.

Recurrent Neural Networks



$$\mathbf{h}_{t} = W_{ih} \mathbf{x}_{t} + W_{hh} \mathbf{h}_{t-1} + b_{ih} + b_{hh}$$
(1)

$$\mathbf{a}_{t} = \tanh(\mathbf{h}_{t})$$
(2)

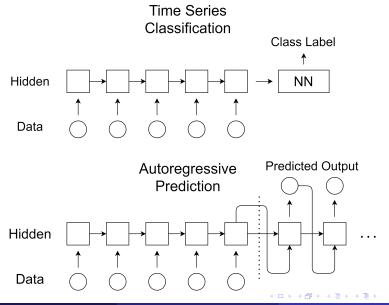
$$\mathbf{o}_{t} = \operatorname{softmax}(W_{ho} \mathbf{a}_{t} + b_{ho})$$
(3)

Weight matrices are shared, meaning sequence can be arbitrary length.

æ

< □ > < □ > < □ > < □ > < □ > < □ >

Applications of RNN



э

Switching to code notebook.

-∢ ∃ ▶

When your data is an actual time series (ex. stock prices, not English sentences), including time as an input feature can be extremely helpful.

- Useful when time series are irregularly sampled.
- Also allows interpolation between observed sequences.

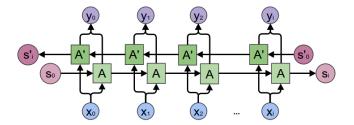
Generally, handle by including the time delta between observations.

• Instead of x_i , feed augmented input $\{x_i, t_i - t_{i-1}\}$ to RNN.

Also see: GRU-D (Che et al. 2018), a sophisticated method to handle irregularly and sparsely observed time series.

RNN Modifications: Bidirectional RNNs

Bidirectional RNNs (Schuster and Paliwal 1997)



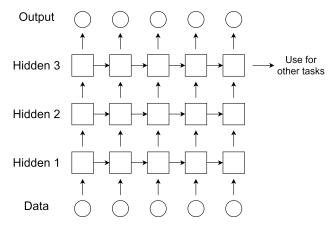
Source: http://colah.github.io/posts/2015-09-NN-Types-FP/

Runs two separate RNN in opposite directions, and concatenate output.

- Access to the future values can improve RNN representations.
- Example: The _____ is a flightless bird that lives in Antarctica.

RNN Modifications: Stacked RNNs

Stacked RNNs



문 🛌 🖻

PyTorch Implementation

CLASS torch.nn.RNN(*args, **kwargs)

Applies a multi-layer Elman RNN with tanh or ReLU non-linearity to an input sequence.

For each element in the input sequence, each layer computes the following function:

$$h_t = \tanh(W_{ih}x_t + b_{ih} + W_{hh}h_{(t-1)} + b_{hh})$$

where h_t is the hidden state at time t, x_t is the input at time t, and $h_{(t-1)}$ is the hidden state of the previous layer at time t-1 or the initial hidden state at time o. If nonlinearity is 'relu', then ReLU is used instead of $\tanh a$.

Parameters

- input_size The number of expected features in the input x
- hidden_size The number of features in the hidden state h
- num_layers Number of recurrent layers. E.g., setting num_layers=2 would mean stacking two RNNs together to form a stacked RNN, with the second RNN taking in outputs of the first RNN and computing the final results. Default: 1
- · nonlinearity The non-linearity to use. Can be either 'tanh' or 'relu'. Default: 'tanh'
- bias If False, then the layer does not use bias weights b_ih and b_hh. Default: True
- batch_first If True, then the input and output tensors are provided as (batch, seq, feature). Default:
 False
- dropout If non-zero, introduces a Dropout layer on the outputs of each RNN layer except the last layer, with dropout probability equal to dropout. Default: 0
- bidirectional If True, becomes a bidirectional RNN. Default: False

12 / 27

[SOURCE

< ロト < 同ト < ヨト < ヨト

Questions?

Slides by: Ian Shi

3

イロト イヨト イヨト イヨト

Prediction tasks in time series often requires long term information from observations ago.

Example: "The flamingo is a pink bird which lives in warmer regions of the world, and they like to speak in run-on sentences for the sake of this example. Surprisingly, _____ are not naturally pink, but rather appear pink because they are always embarrassed."

Task: Fill in the blank. The RNN needs to store information about the subject for an arbitrarily long length. Experiments show RNNs have a hard time remembering.

イロト イヨト イヨト -

Consider: Deepest feed forward models contain up to \sim 150 layers, but the type of sequential data used in RNNs can easily exceed this in length. What happens to the gradient?

Some intuition:

- Backprop is chain rule, i.e., recursive multiplication of many VJPs.
- The derivative of the Tanh / Sigmoid activation is always less than 1.
- Multiplying gradient with enough activation Jacobians will cause the gradient will go to 0.
- Gradients can explode with ReLU activations (since its unbounded).

Hacky fixes: Gradient clipping to prevent explosion.

Long Short-Term Memory (LSTM) units introduce long term cell state, allowing gradients to flow without being forced to change.

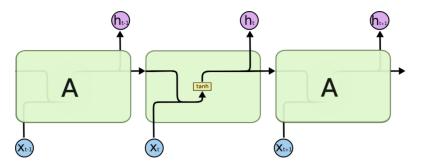
• Well, that description was unclear. Lets break it down!

The following figures are directly taken from Chris Olah's blog: https://colah.github.io/posts/2015-08-Understanding-LSTMs/

- Avoiding citing each image to save space, but I claim no credit!
- Side note: his blog contains many top tier tutorials, and is worth checking out.



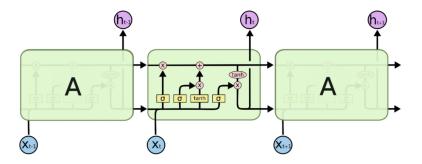
RNN Diagram



æ



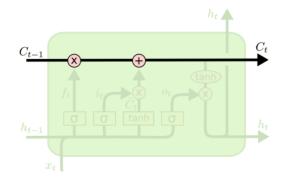
LSTM Diagram



3

イロト イヨト イヨト イヨト

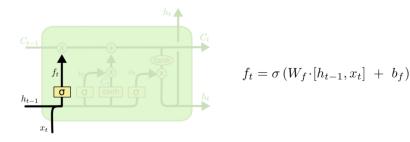
Personally, I think of cell state as long-term memory. Protected by gates (next slides) from unwanted gradient updates.



- (日)

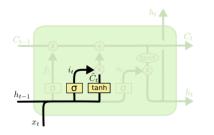
LSTMs

Forget Gate: Deletes information from cell state.



- Takes linear combination of x_t and $h_{t=1}$.
- Sigmoid activation squashes to range 0 (forget) to 1 (remember).
- Output multiplied element-wise with cell state to forget certain pieces of long term information (e.g., if the subject switches).

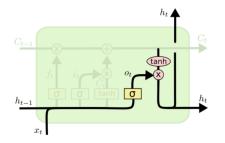
Input Gate: Adds information to cell state.



$$\begin{split} i_t &= \sigma \left(W_i \!\cdot\! [h_{t-1}, x_t] \;+\; b_i \right) \\ \tilde{C}_t &= \tanh(W_C \!\cdot\! [h_{t-1}, x_t] \;+\; b_C) \end{split}$$

- First function determines which cell dimensions to update.
- Second function determines what values to update cell state with.
- Output of input gate is added to cell state.

Output Gate: Decides what information to output from cell state.



$$o_t = \sigma \left(W_o \left[h_{t-1}, x_t \right] + b_o \right)$$
$$h_t = o_t * \tanh \left(C_t \right)$$

• Afterwards, hidden and cell states passed to next cell.

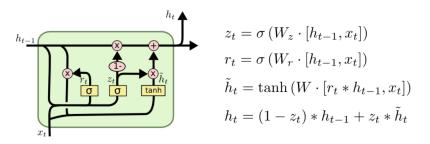
Switching to Notebook

2

イロト イヨト イヨト イヨト

LSTMs are pretty complex, and require many weights.

Gated Recurrent Units (GRUs) (Cho et al. 2014) simplify LSTMs, and should perform roughly as well.



Merge cell and hidden states, but keep the concept of gating updates to hidden state.

- 4 間 ト - 4 三 ト - 4 三 ト

Conclusions

So do LSTMs actually solve the vanishing gradient problem? Kinda!

- Many deployed real-world applications. Powered Google Translate for many years.
- Long term dependencies still challenging in reality.

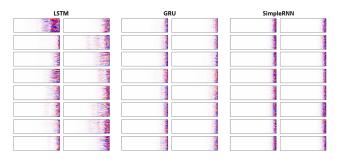


Figure: Heatmap of gradient flow mapped out by depth. Source: https://github.com/OverLordGoldDragon/see-rnn Having to somehow pass long term information through hidden states may be a fundamentally flawed paradigm.

• Example: When we read, we don't actually look at the whole sentence, only keywords.

Next time on CSC413: Attention & Transformers – teaching our models to focus on the important parts.





Zhengping Che et al. "Recurrent neural networks for multivariate time series with missing values". In: *Scientific reports* 8.1 (2018), pp. 1–12.

Kyunghyun Cho et al. "Learning phrase representations using RNN encoder-decoder for statistical machine translation". In: *arXiv preprint arXiv:1406.1078* (2014).

Mike Schuster and Kuldip K Paliwal. "Bidirectional recurrent neural networks". In: *IEEE transactions on Signal Processing* 45.11 (1997), pp. 2673–2681.