

Syntax and Parsing

COMS W4115

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Fall 2006

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Lexical Analysis (Scanning)

Lexical Analysis (Scanning)

Translates a stream of characters to a stream of tokens

$f \circ o \sqcup = \sqcup a + \sqcup \text{bar}(2, \sqcup q);$

ID	EQUALS	ID	PLUS	ID	Lparen	NUM
COMMA	ID	Lparen	SEMI			

Token	Lexemes	Pattern
EQUALS	=	an equals sign
PLUS	+	a plus sign
ID	a foo bar	letter followed by letters or digits
NUM	0 42	one or more digits

Lexical Analysis

Describing Tokens

Goal: simplify the job of the parser.

Scanners are usually much faster than parsers.

Discard as many irrelevant details as possible (e.g., whitespace, comments).

Parser does not care that the identifier is “supercaffragisticexpialidocious.”

Parser rules are only concerned with tokens.

Alphabet: A finite set of symbols

Examples: { 0, 1 }, { A, B, C, …, Z }, ASCII, Unicode

String: A finite sequence of symbols from an alphabet

Examples: ϵ (the empty string), Stephen, $\alpha\beta\gamma$

Language: A set of strings over an alphabet

Examples: \emptyset (the empty language), { 1, 11, 111, 1111 }, all English words, strings that start with a letter followed by any sequence of letters and digits

Operations on Languages

Let $L = \{ \epsilon, \text{wo} \}$, $M = \{ \text{man}, \text{men} \}$

Concatenation: Strings from one followed by the other

$L.M = \{ \text{man, men, woman, women} \}$

Union: All strings from each language

$L \cup M = \{ \epsilon, \text{wo, man, men} \}$

Kleene Closure: Zero or more concatenations

$M^* = \{ \epsilon, M, MM, MMM, \dots \} = \{ \epsilon, \text{man, men, manman, manmen, menmen, manmanman, manmanmen, manmenmen, \dots} \}$

Kleene Closure

Regular Expression Examples

RE	Language
$a b$	$\{a, b\}$
$(a b)(a b)$	$\{aa, ab, ba, bb\}$
a^*	$\{\epsilon, a, aa, aaa, aaaa, \dots\}$
$(a b)^*$	$\{\epsilon, a, b, aa, ab, ba, bb, aaa, aab, aba, abb, \dots\}$
$a a^*$	$\{a, b, ab, aab, acab, acaaab, \dots\}$
$(r)^*$	$\{tu : t \in L(r), u \in L(s)\}$
$(r)^*$	$\{r\}^* \text{ denotes } \{tu : t \in L(r), u \in L(s)\}$
$(r)^*$	$\{r\}^* \text{ denotes } \bigcup_{i=0}^{\infty} L^i \text{ (} L^0 = \{\epsilon\} \text{ and } L^i = LL^{i-1}\text{)}$



The asterisk operator (*) is called the Kleene Closure operator after the inventor of regular expressions, Stephen Cole Kleene, who pronounced his last name “CLAY-nee.” His son Ken writes “As far as I am aware this pronunciation is incorrect in all known languages. I believe that this novel pronunciation was invented by my father.”

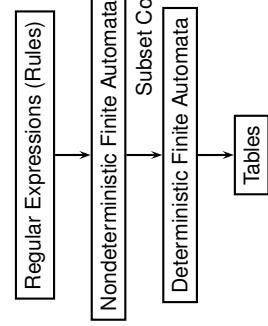
Specifying Tokens with REs

Typical choice: $\Sigma = \text{ASCII characters, i.e., } \{\text{f}, \text{,}, \text{!}, \text{,}, \text{#}, \text{,}, \text{0}, \text{,}, \text{1}, \text{,}, \text{,}, \text{9}, \text{,}, \text{A}, \text{,}, \text{,}, \text{Z}, \text{,}, \text{,}, \text{~}\}$

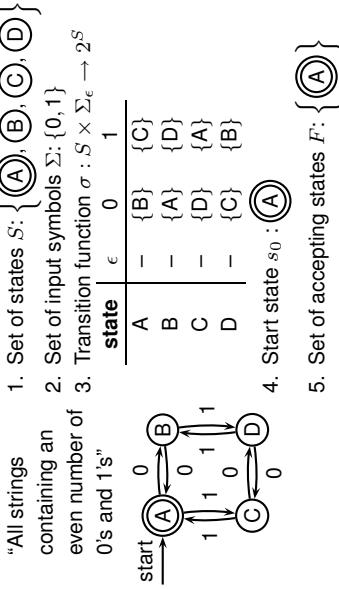
letters: $A|B|\dots|Z|a|\dots|z$

digits: $0|1|\dots|9$

identifier: letter (letter | digit)^{*}



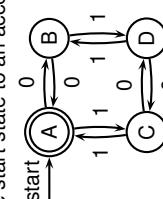
Implementing Scanners Automatically



Nondeterministic Finite Automata

The Language induced by an NFA

An NFA accepts an input string x iff there is a path from the start state to an accepting state that "spells out" x .

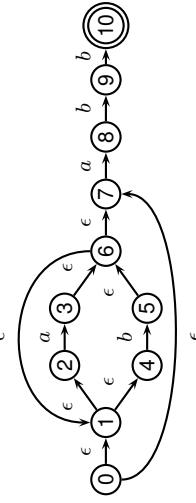


Show that the string "010010" is accepted.



Translating REs into NFAs

Example: translate $(a|b)^*abb$ into an NFA



Show that the string "aabbb" is accepted.
 $\text{0} \xrightarrow{\epsilon} \text{1} \xrightarrow{\epsilon} \text{2} \xrightarrow{a} \text{3} \xrightarrow{\epsilon} \text{4} \xrightarrow{a} \text{5} \xrightarrow{\epsilon} \text{6} \xrightarrow{\epsilon} \text{7} \xrightarrow{a} \text{8} \xrightarrow{b} \text{9} \xrightarrow{b} \text{10}$

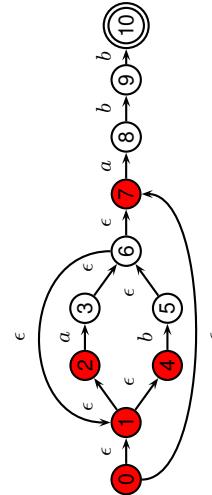
Simulating NFAs

Problem: you must follow the "right" arcs to show that a string is accepted. How do you know which arc is right? Solution: follow them all and sort it out later.

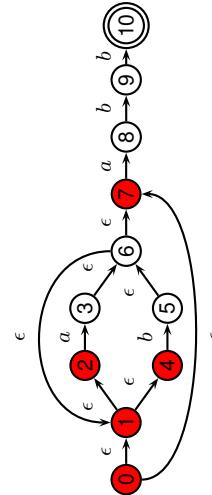
"Two-stack" NFA simulation algorithm:

- Initial states: the ϵ -closure of the start state
- For each character c ,
 - New states: follow all transitions labeled c
 - Form the ϵ -closure of the current states
- Accept if any final state is accepting

Simulating an NFA: ·aabb, Start



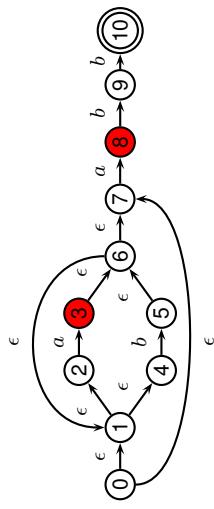
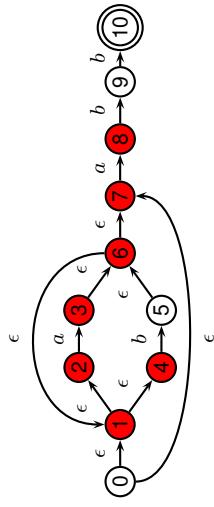
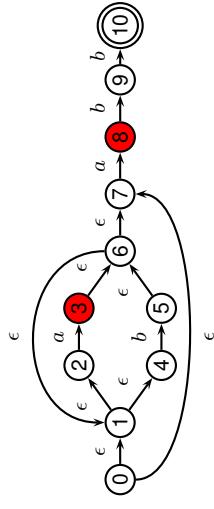
Simulating an NFA: ·aabb, ε-closure



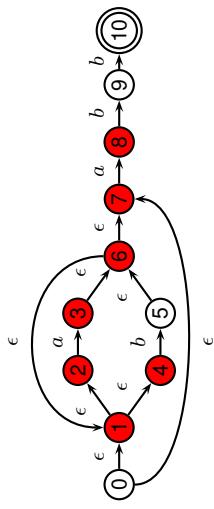
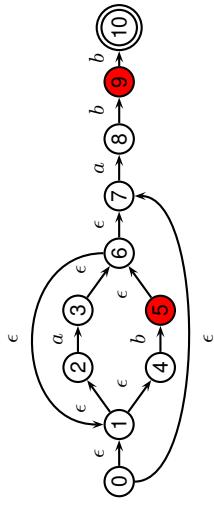
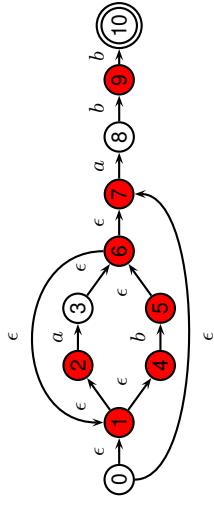
Simulating an NFA: $aabb$

Simulating an NFA: $aabb$, ϵ -closure

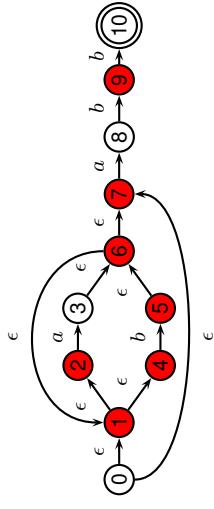
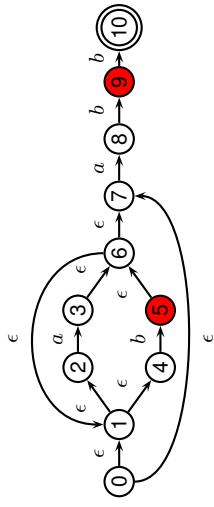
Simulating an NFA: $aa \cdot abb$



Simulating an NFA: $aa \cdot bb$, ϵ -closure



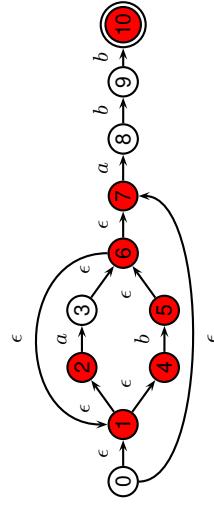
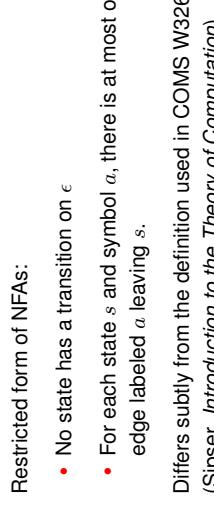
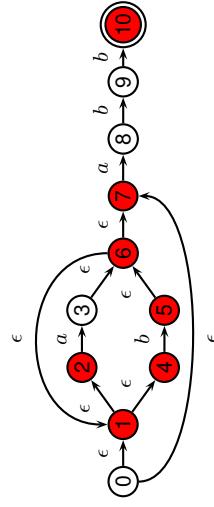
Simulating an NFA: $aab \cdot b$



Simulating an NFA: $aab \cdot b$, ϵ -closure

Simulating an NFA: $aabb$.

Simulating an NFA: $aabb$, Done



Restricted form of NFAs:

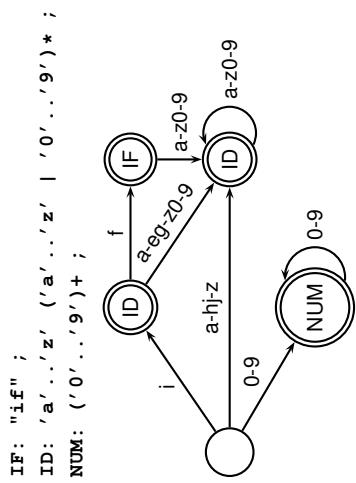
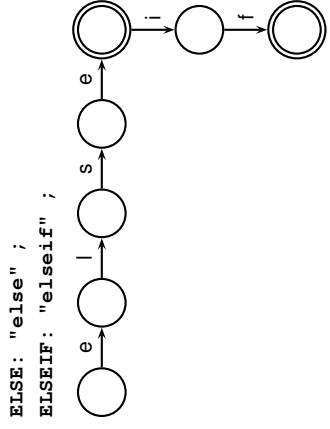
- No state has a transition on ϵ
- For each state s and symbol a , there is at most one edge labeled a leaving s .

Differs subtly from the definition used in COMS W3261 (Sipser, *Introduction to the Theory of Computation*)
Very easy to check acceptance: simulate by maintaining current state. Accept if you end up on an accepting state. Reject if you end on a non-accepting state or if there is no transition from the current state for the next symbol.

Deterministic Finite Automata

Deterministic Finite Automata

Deterministic Finite Automata



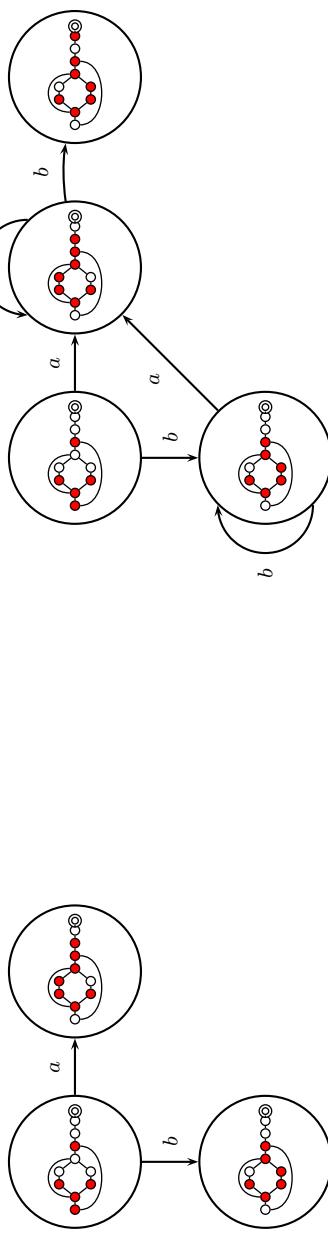
Building a DFA from an NFA

Subset construction algorithm
Simulate the NFA for all possible inputs and track the states that appear.
Each unique state during simulation becomes a state in the DFA.

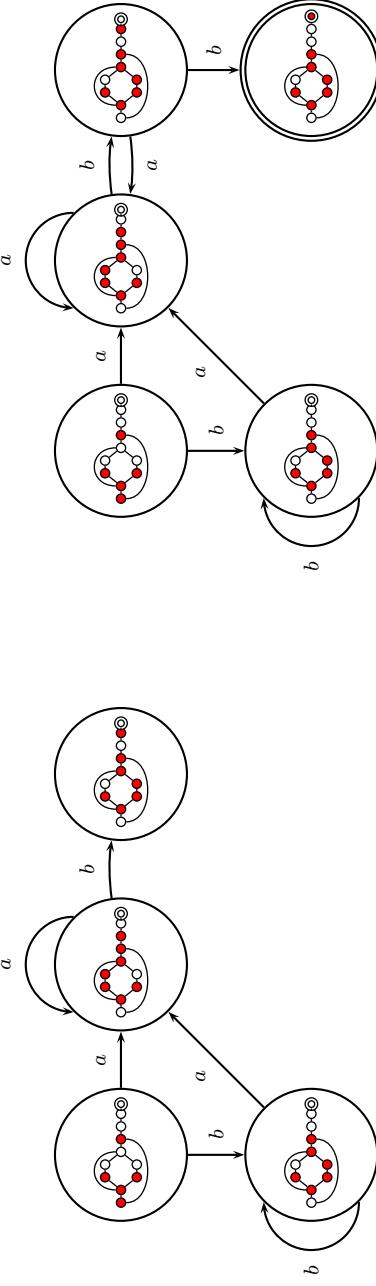
Deterministic Finite Automata

Subset construction algorithm
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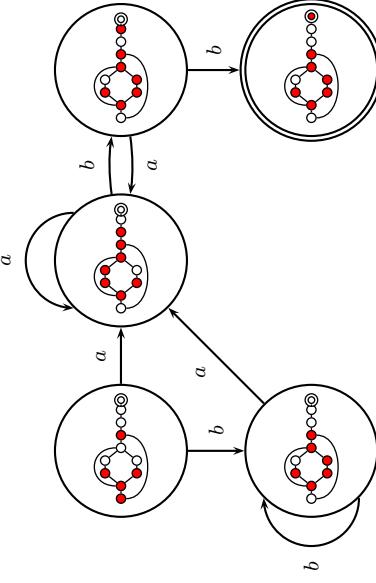
Subset construction for $(a|b)^*abb$ (1)



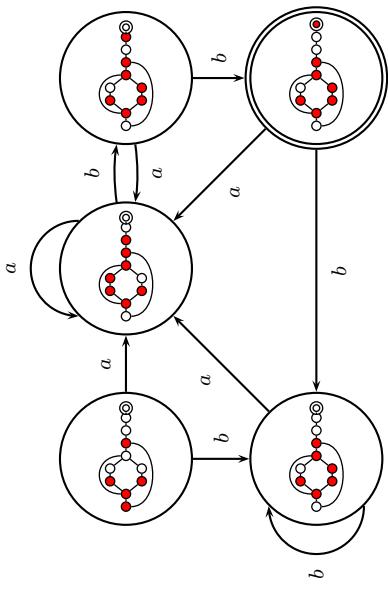
Subset construction for $(a|b)^*abb$ (2)



Subset construction for $(a|b)^*abb$ (3)



Subset construction for $(a|b)^*abb$ (4)



Subset Construction

An DFA can be exponentially larger than the corresponding NFA.
 n states versus 2^n
Tools often try to strike a balance between the two representations.
ANTLR uses a different technique.

The ANTLR Compiler Generator

Language and compiler for writing compilers
Running ANTLR on an ANTLR file produces Java source files that can be compiled and run.
ANTLR can generate
• Scanners (lexical analyzers)
• Parsers
• Tree walkers

An ANTLR File for a Simple Scanner

ANTLR Specifications for Scanners

```
class CalcLexer extends Lexer;
{
    LPAREN : '(' ; // Rules for punctuation
    RPAREN : ')' ;
    STAR : '*' ;
    PLUS : '+' ;
    SEMI : ';' ;
    IF : "if" ;
    PROTECTED : "protected" ; // Can only be used as a sub-rule
    DIGIT : '0'... '9' ; // Any character between 0 and 9
    INT : (DIGIT)+ ; // One or more digits
    WS : (' ' | '\t' | '\n' | '\r') // Whitespace
        { setType(Token.SKIP); } // Action: ignore
}
```

Rules are names starting with a capital letter.

A character in single quotes matches that character.

LPAREN : '(' ;

A string in double quotes matches the string

IF : "if" ;

A vertical bar indicates a choice:

OP : '+' | '-' | '*' | '/' ;

WS : (' ' | '\t' | '\n' | '\r') // Whitespace

{ setType(Token.SKIP); } // Action: ignore

Question mark makes a clause optional.

```
PERSON : ("wo")? 'm' ('a'|'e') 'n' ;
(Matches man, men, woman, and women.)
```

Double dots indicate a range of characters:

```
DIGIT : '0'...'9' ;
Asterisk and plus match "zero or more," "one or more."
ID : LETTER (LETTER | DIGIT)* ;
NUMBER : (DIGIT)+ ;
```

Asterisk and plus match "zero or more," "one or more."

Free-Format Languages

Typical style arising from scanner/parser division

Program text is a series of tokens possibly separated by whitespace and comments, which are both ignored.

- keywords (if while)
- punctuation (, (+)
- identifiers (foo bar)
- numbers (10 -3.14159e+32)
- strings ("A String")

Free-Format Languages

Java C C++ Algol Pascal

Some deviate a little (e.g., C and C++ have a separate preprocessor)

But not all languages are free-format.



When column 6 is not a space, line is considered part of the previous.

Fixed-length line works well with a one-line buffer.

Makes sense on punch cards.

FORTRAN 77

FORTRAN 77 is not free-format: 72-character lines:

```
100 IF(IN.EQ.'Y'.OR.IN.EQ.'y'.OR.
      $ IN.EQ.'T'.OR.IN.EQ.'t') THEN
      1 ... 5   6   7 ... 72
      Statement label Continuation Normal
```

Syntax and Language Design

Does syntax matter? Yes and no

More important is a language's *semantics*—its meaning.

The syntax is aesthetic, but can be a religious issue.

But aesthetics matter to people, and can be critical.

Verbosity does matter: smaller is usually better.

Too small can be a problem: API is a compact, cryptic language with its own character set ()!

E→A TEST B;L

L→0 .5

This is succinct, but can be error-prone.

How do you wrap a conditional around instructions?

Python

The Python scripting language groups with indentation

```
i = 0
while i < 10:
    i = i + 1
    print i # Prints 1, 2, ..., 10
print i # Just prints 10
This is succinct, but can be error-prone.
```

How do you wrap a conditional around instructions?

Some syntax is error-prone. Classic FORTRAN example:

```
DO 5 I = 1,25 ! Loop header (for i = 1 to 25)
DO 5 I = 1,25 ! Assignment to variable DO5I
```

Trying too hard to reuse existing syntax in C++:

```
vector< vector<int> > foo; // Syntax error
vector<vector<int>> foo; // Syntax error
C distinguishes > and >> as different operators.
```

Parsing

Grammars

Objective: build an abstract syntax tree (AST) for the token sequence from the scanner.

Parsing

$$2 * 3 + 4 \Rightarrow \begin{array}{c} + \\ / \quad \backslash \\ 2 \quad 3 \end{array}$$

Goal: discard irrelevant information to make it easier for the next stage.

Parentheses and most other forms of punctuation removed.

Most programming languages described using a *context-free grammar*.

Compared to regular languages, context-free languages add one important thing: recursion.

Recursion allows you to count, e.g., to match pairs of nested parentheses.

Which languages do humans speak? I'd say it's regular: I do not not not not not not not not understand this sentence.

Languages

Regular languages (t is a terminal):

$$A \rightarrow t_1 \dots t_n B$$

$$A \rightarrow t_1 \dots t_n$$

Context-free languages (P is terminal or a variable):

$$A \rightarrow P_1 \dots P_n$$

Context-sensitive languages:

$$\alpha_1 A \alpha_2 \rightarrow \alpha_1 B \alpha_2$$

" $B \rightarrow A$ only in the 'context' of $\alpha_1 \dots \alpha_2$ "

Issues

Ambiguous grammars

Precedence of operators

Left- versus right-recursive

Top-down vs. bottom-up parsers

Parse Tree vs. Abstract Syntax Tree

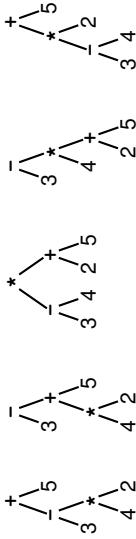
Ambiguous Grammars

A grammar can easily be ambiguous. Consider parsing

$$3 - 4 * 2 + 5$$

with the grammar

$$e \rightarrow e + e \mid e * e \mid e / e \mid N$$



Operator Precedence and Associativity

Defines how "sticky" an operator is.

$$1 * 2 + 3 * 4$$

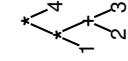
* at higher precedence than +:

$$(1 * 2) + (3 * 4)$$

+ at higher precedence than *:

$$1 * (2 + 3) * 4$$

$((1 - 2) - 3) \cdot 4$
left associative



Operator Precedence

Whether to evaluate left-to-right or right-to-left
Most operators are left-associative

$$1 - 2 - 3 - 4$$

$1 / (2 \cdot 3) \cdot 4$
right associative

Associativity

Fixing Ambiguous Grammars

Assigning Precedence Levels

Original ANTLR grammar specification

```
expr : expr '+' expr
      | expr '-' expr
      | expr '*' expr
      | expr '/' expr
      | NUMBER

atom : NUMBER ;
```

Ambiguous: no precedence or associativity.

Still ambiguous: associativity not defined

Parsing Context-Free Grammars

Assigning Associativity

Make one side or the other the next level of precedence

```
expr : expr '+' term
      | expr '-' term
      | term ;

term : term '*' atom
      | term '/' atom
      | atom ;
```

atom : NUMBER ;

Parsing LL(k) Grammars

LL: Left-to-right, Left-most derivation
k: number of tokens to look ahead

Parsed by top-down, predictive, recursive parsers
Basic idea: look at the next token to predict which production to use

ANTLR builds recursive LL(k) parsers
Almost a direct translation from the grammar.

Parsing LL(1) Grammars

Implementing a Top-Down Parser

```
stmt : 'if' expr 'then' expr
      | 'while' expr 'do' expr
      | expr ':' expr ;
expr : NUMBER | '(' expr ')' ;
stmt() {
    switch (next-token) {
        case IF:
            match(IF); expr(); match(THEN); expr();
            break;
        case WHILE:
            match(WHILE); expr(); match(DO); expr();
            break;
        case NUMBER or LPAREN:
            expr(); match(COLEQ); expr();
    }
}
```

Writing LL(k) Grammars

Cannot have left-recursion

```
expr : expr '+' term | term ;
becomes
AST expr() {
    switch (next-token) {
        case NUMBER : expr(); /* Infinite Recursion */
        break;
```

Cannot have common prefixes

```
expr : ID '(' expr ')'
      | ID '=' expr ;
becomes
expr() {
    switch (next-token) {
        case ID:
            match(ID); match(LPAR); expr(); match(RPAR); break;
        case ID:
            match(ID); match(EQUALS); expr();
            break;
```

Eliminating Common Prefixes

Consolidate common prefixes:

```
expr : expr '+' term
      | expr '-' term
      | term ;
becomes
expr {
    switch (next-token) {
        case '+':
            expr ('+' term | '-' term )
        break;
```

Eliminating Left Recursion

Using ANTLR's EBNF

Understand the recursion and add tail rules

```
expr : expr ('+' term | '-' term )
      | term ;
becomes
expr : term exprt ;
exprt : '+' term exprt
      | '-' term exprt
      | /* nothing */ ;
;
```

ANTLR makes this easier since it supports * and -:

```
expr : expr '+' term
      | expr '-' term
      | term ;
becomes
expr : term ( '+' term | '-' term ) * ;
```

Who owns the else?

```
if (a) if (b) c() ; else d() ;
      or
      if
      / \
      a   if
           / \
           b   c()
           |
           d()
```

Grammars are usually ambiguous; manuals give disambiguating rules such as C's:

As usual the "else" is resolved by connecting an else with the last encountered elseifless if.

The Dangling Else Problem

The Dangling Else Problem

The Dangling Else Problem

Understand the recursion and add tail rules

```
stmt : "if" expr "then" stmt iftail
      | other-statements ;
iftail
: "else" stmt
| /* nothing */ ;
;
```

The Dangling Else Problem

The Dangling Else Problem

ANTLR can resolve this problem by making certain rules "greedy." If a conditional is marked as greedy, it will take that option even if the "nothing" option would also match:

```
stmt
: "if" expr "then" stmt
  ( options {greedy = true; }
  : "else" stmt
  )?
  | other-statements
;
```

Problem comes when matching "iftail".

Normally, an empty choice is taken if the next token is in the "follow set" of the rule. But since "else" can follow an iftail, the decision is ambiguous.

Statement separators/terminators

C uses ; as a statement terminator.

```
if (a>b) printf("a less");
else {
  printf("b"); printf(" less");
}
```

Pascal uses ; as a statement separator.

```
if a < b then writeln('a less')
else begin
  write('a'); writeln(' less')
end
```

Pascal later made a final ; optional.

Some languages resolve this problem by insisting on nesting everything.

E.g., Algol 68:

```
if a < b then a else b fi;
"fi" is "if" spelled backwards. The language also uses do-od and case-easac.
```

Rightmost Derivation

```
1: e->t + e
2: e->t
3: t->id * t
4: t->id
```

A rightmost derivation for id * id + id:

Basic idea of bottom-up parsing:
construct this rightmost derivation
backward.

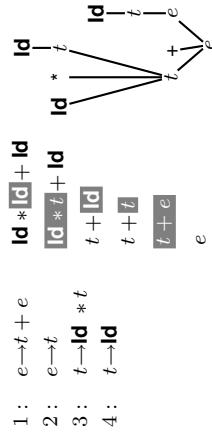
```
[e]
t + e
t + t
t + id
id * id + id
```

Bottom-up Parsing

Handles

Shift-reduce Parsing

LR Parsing



Each highlighted section is a **handle**.

Taken in order, the handles build the tree from the leaves to the root.

Scan input left-to-right, looking for handles.
An oracle tells what to do

	action	stack	input	action	stack	input	action	stack	input	action	stack
1 :	$e \rightarrow t + e$	$\text{id} * \text{id} + \text{id}$	id								
2 :	$e \rightarrow t$	$\text{id} * \text{id} + \text{id}$	id	$\text{id} * \text{id}$	id	t	shift	$\text{id} * \text{id} + \text{id}$	id	shift, goto 1	
3 :	$t \rightarrow \text{id} * t$	$\text{id} * \text{id} + \text{id}$	id	$\text{id} * \text{id}$	id	id	shift	$\text{id} * \text{id}$	id	shift	
4 :	$t \rightarrow \text{id}$	$\text{id} * \text{id}$	$t + \text{id}$	id	id	$\text{id} * \text{id}$	reduce (4)	$\text{id} + \text{id}$	id	reduce (3)	

1. Look at state on top of stack
2. and the next input token
3. to find the next action
4. In this case, shift the token onto the stack and go to state 1.

LR Parsing

Constructing the SLR Parse Table

	action	stack	input	action	stack	input	action	stack	input	action	stack
1 :	$e \rightarrow t + e$	$\text{id} * \text{id} + \text{id}$	id	shift	$\text{id} * \text{id} + \text{id}$	id	shift	$\text{id} * \text{id} + \text{id}$	id	shift, goto 1	
2 :	$e \rightarrow t$	$\text{id} * \text{id} + \text{id}$	id	$\text{id} * \text{id}$	id	t	shift	$\text{id} * \text{id}$	id	shift	
3 :	$t \rightarrow \text{id} * t$	$\text{id} * \text{id}$	id	$\text{id} * \text{id}$	id	id	reduce (2)	$\text{id} + \text{id}$	id	reduce (1)	
4 :	$t \rightarrow \text{id}$	id	$t + \text{id}$	id	id	id	reduce (4)	$\text{id} + \text{id}$	id	reduce (3)	

1. Look at state on top of stack
2. and the next input token
3. to find the next action
4. In this case, shift the token onto the stack and go to state 1.

Constructing the SLR Parsing Table

The Punchline

This is a tricky, but mechanical procedure. The parser generators YACC, Bison, Cup, and others (but not ANTLR) use a modified version of this technique to generate fast bottom-up parsers.

You need to understand it to comprehend error messages:
Shift/reduce conflicts are caused by a state like

$t \rightarrow \text{id} \cdot \ast$,
 $t \rightarrow \text{id} \cdot t$,
 $t \rightarrow \text{id} \cdot \text{id}$,
 $e \rightarrow t + e$

Reduce/reduce conflicts are caused by a state like

$t \rightarrow \text{id} \cdot \ast$,
 $t \rightarrow \text{id} \cdot t$,
 $t \rightarrow \text{id} \cdot \text{id}$,
 $e \rightarrow t + e$

