# **Differential Privacy**









# Data—The New Oil or the New Plutonium?

- Data can be very useful, both to its collectors and to others
  - Marketing
  - "Suggestion" algorithms
  - Researchers
  - Public issues, e.g., election districts, federal aid, etc.
- Data can be very dangerous if compromised
  - Intentional, controlled release
  - Hackers
  - Legal process





## **Protecting Released Data: First Attempts**

- Remove PII
- No problem, right?





# **Early Privacy Techniques**

### • *k*-Anonymity

Statistical queries only









- others
- Similar to what HIPAA requires
- Often unclear how much privacy is guaranteed

### Ensure that any record in a dataset cannot be distinguished from at least k-1





# HIPAA Privacy Safe Harbor

- Delete a list of 18 specific identifiers
  - Name, address, SSN, birth date (but not age unless over 90), etc.
- Delete other items known to be identifying
- Can include important demographic information such as gender and race
- Note: HIPAA applies to health care providers, health care plans, and "business associates"—but not to Google, Microsoft, etc.
- Note well: this is **very** oversimplified

Aggregate by state or by the first three digits of zip code if that's more than 20,000 people







## **Statistical Queries**

- Don't release the dataset; allow only specific queries
- to achieve good privacy

But — if powerful-enough queries are allowed, it is mathematically impossible





### Raw Data

### (Note: Randomly generated)

Last Name	First Name	Phone	Zip Code	Random ID	Gender	Birthdate	Salary	Race	Medical
Bryan	Frank	805-269-4479	60629	6973721572	М	Jun 12, 1958	\$52,400	Black	Heart
Dery	Douglas	708-781-4211	79936	3389209159	М	Apr 28, 1985	\$118,300	White	
Dube	Bessie	859-817-1388	90011	7574713594	F	May 20, 1938	\$91,000	White	Heart
Haines	Fernando	414-614-0455	11385	2741335550	М	Apr 13, 1977	\$115,600	-	Cancer
Jones	Naomi	816-202-7762	90650	3717441036	F	Sep 2, 1960	\$136,800	White	Cancer
Neary	Hai	706-415-9488	77494	1561829881	NB	Apr 29, 1983	\$141,300	White	
Razo	Jesabel	507-454-2166	91331	9037803106	F	Feb 18, 1951	\$113,800	Hispanic	
Romano	Carlos	480-391-4486	90201	5132078469	М	Jun 22, 1988	\$102,200	Hispanic	
Worley	Elizabeth	617-298-9122	11226	3819315445	F	May 27, 1952	\$100,000	White	
Martinez	Mary	775-551-5327	10467	6730204579	F	Jun 13, 1978	\$82,200	Hispanic	HIV





## Sanitized Data

Zip Code	Random ID	Gender	Birthdate	Salary	Race	Medical
60629	6973721572	М	Jun 12, 1958	\$52,400	Black	Heart
79936	3389209159	М	Apr 28, 1985	\$118,300	White	
90011	7574713594	F	May 20, 1938	\$91,000	White	Heart
11385	2741335550	М	Apr 13, 1977	\$115,600	-	Cancer
90650	3717441036	F	Sep 2, 1960	\$136,800	White	Cancer
77494	1561829881	NB	Apr 29, 1983	\$141,300	White	
91331	9037803106	F	Feb 18, 1951	\$113,800	Hispanic	
90201	5132078469	М	Jun 22, 1988	\$102,200	Hispanic	
11226	3819315445	F	May 27, 1952	\$100,000	White	
10467	6730204579	F	Jun 13, 1978	\$82,200	Hispanic	HIV





# Is This Data Sufficiently Protected?

- Medical information is quite sensitive
  - (N.Y. PBH §2782: No person who obtains confidential HIV related
  - And there's HIPAA
- Can the individuals be identified without the redacted PII?
- Sometimes, yes...

information in the course of providing any health or social service or pursuant to a release of confidential HIV related information may disclose or be compelled to disclose such information, except to the following...)





## Reidentification

- gender, and zip code
  - These fields are not considered PII!
  - age people
  - (Another study put the number at 63% but that's still a lot)
- Now factor in race and likely income bracket

### Latanya Sweeney: 87% of Americans are uniquely identified by birthdate,

Many of the remainder were in places like college towns, with many similar-





## **Reidentification Works**

- Sweeney located the health records of the governor of Massachusetts
- The NY Times identified some individuals in anonymized AOL query data
- Narayanan and Shmatikov identified individuals in a released Netflix dataset







# **Several Strategies for Reidentification**

- Outside data
  - Narayanan and Shmatikov use IMDb ratings
- Uniqueness of birthdate/gender/zipcode
- Uniqueness of query strings

Now what?





# **Differential Privacy**

- privacy
- But—there is a tradeoff with accuracy
- The parameter  $\varepsilon$  specifies the tradeoff
- algorithms)

### Differential privacy provides a mathematical guarantee of a certain amount of

And: differential privacy is a property, not an algorithm (but there are such





# **Defining Differential Privacy**

- Assume that there are two datasets,  $D_1$  and  $D_2$ , differing in at most one element
- Assume a "randomized function"  $\mathcal{K}$  and a set  $S \subseteq Range(\mathcal{K})$
- Then  $\mathcal{K}$  is " $\epsilon$ -differentially private" if



### $\Pr[\mathcal{K}(D_1) \in S] \leq e^{\varepsilon} \cdot \Pr[\mathcal{K}(D_2) \in S]$





# Huh?

### $\Pr[\mathcal{K}(D_1) \in S] \leq e^{\varepsilon} \cdot \Pr[\mathcal{K}(D_2) \in S]$

- $D_1$  and  $D_2$  are, for example, sets of medical history data
- i.e., the possible outcomes
- S is a set of particular outcomes, e.g., cancer
- $\Pr[\mathcal{K}(D_i) \in S]$  is the probability of predicting some medical outcome, e.g., cancer
- e is the base of the natural logarithms, 2.71828...
- outcome from a small change in the dataset is bounded by a factor of  $e^{\varepsilon}$

•  $\mathcal{K}$  is a function that predicts medical outcomes. The "range" of  $\mathcal{K}$  is the set of possible values,

 $\Pr[\mathcal{K}(D_1) \in S] \le e^{\varepsilon} \cdot \Pr[\mathcal{K}(D_2) \in S]$  shows that the change in the probability of predicting an





## **Intuitive Translation**

their data is included in the dataset.

the more privacy you obtain, but the less accurate your results will be

results

- The privacy risk to an individual should not change significantly whether or not
- The privacy parameter  $\varepsilon$  should be a small, positive number the smaller it is,
- The smaller  $\varepsilon$  is, the larger your dataset must be to produce useful statistical





# How Do We Achieve Differential Privacy?

- General technique: add "noise"
- That is: generate a random value from a (carefully chosen) distribution parameterized by  $\varepsilon$
- Add this value to numeric fields in the dataset
- Note well: if you want privacy for c individuals, the effective privacy bound is

- In other words, you get good privacy protection for up to  $c \approx 1/\varepsilon$  individuals, and very little for  $c \approx 10/\varepsilon$  individuals
- $C \cdot \mathcal{E}$





# Why is Differential Privacy Good?

- It's a precise mathematical definition
- It gives an exact guarantee of privacy
- It's mathematically tractable, so we can prove theorems about privacy





# **Real-World Challenges**

- Generating differentially private datasets can be expensive
  - (In our census experiments, we needed a fair number of AWS cores for several days, and we were only doing a few counties)
- Differential privacy doesn't work well for "high-dimensionality" datasets ones with many columns
  - Some things, e.g., text, are hard to fit into the DP model
- There are real-world constraints on some values—you can't have a non-integral number of family members; children can't be older than their (biological) parents, etc.
- Is the accuracy good enough? Recall that lower values of  $\varepsilon$  imply more privacy but less accuracy.







# Who Uses Differential Privacy?

- Apple, to protect collected user data
- Google
- Microsoft, for telemetry in Windows
- Facebook
- Wikimedia
- The Census Bureau, for the 2020 census
- (Not used for HIPAA—legal liability issue...)







## The Census Bureau

- By law, individuals' data must be kept confidential
- Department of Commerce or bureau or agency thereof... may... make any under this title can be identified"
- to attack
- But census data *must* be accurate (enough)
- given up on using differential privacy for it

• 13 U.S.C. §9(a)(2): "Neither the Secretary, nor any other officer or employee of the publication whereby the data furnished by any particular establishment or individual

• Researchers there found that their older privacy mechanism, swapping, was subject

The American Community Survey is high-dimensional—and the Census Bureau has





# Daily Bird



Solitary sandpiper, Central Park, September 20, 2023



