

CS 4995 – Fall 2022

Logic and Computability

Lectures: Wednesday 4:10-6:30, 331 URIS

Instructor: Toniann Pitassi, toni@cs.columbia.edu

TA: Yasaman Mahdaviyeh

Office hours: Tuesday 2:45-3:45 (Yasaman), Monday 5-6 (Toni)

Web Page: <http://www.cs.columbia.edu/toni/Courses/Logic2022/4995.html>

Course Notes: PDF files for course notes, lecture notes and other handouts will be available on the course webpage.

Office Hours: Monday office hours via zoom (see Courseworks for link). Please email ahead of time if you plan to attend office hours (on either day).

Topics:

Propositional logic: syntax and semantics, Resolution and Propositional Sequent Calculus soundness and completeness. First order logic: syntax and semantics, First Order Sequent Calculus soundness and completeness. Godel's Incompleteness theorems. Computability: Recursive and recursively enumerable functions, Church's thesis, unsolvable problems

Marking Scheme:

2 assignments (each worth 20% of final grade)

First Term test (20% of final grade)

Second Term Test (20% of final grade)

Class participation (10% of final grade)

Due Dates:

First Test (In Class): Wednesday Oct 19, 4:10-6:30pm

Second Test (In Class): Wednesday, Dec 7, 4:10-6:30pm

Assignment 1 due date: Tuesday Oct 11 11:59pm

Assignment 2 due date: Tuesday Nov 29 11:59pm

The work you submit must be your own. You may discuss problems with each other; however, you should prepare written solutions alone.

Optional Supplementary References:

S Buss: Chapter I: An introduction to proof theory, in **Handbook of Proof Theory**, S Buss Ed., Elsevier, 1998, pp1-78. (grad)

J Bell and M Machover: **A Course in Mathematical Logic**. North-Holland, 1977. (grad)

H.B. Enderton, **A Mathematical Introduction to Logic** (undergrad)

G Boolos and R.C. Jeffrey, **Computability and Logic** (undergrad)

E. Mendelson, **Introduction to Mathematical Logic**, 3rd edition (undergrad/ grad)

J.N. Crossley and others, **What is Mathematical Logic?** (informal, readable)

A.J.Kfoury, R.Moll, and M. Arbib, **A Programming Approach to Computability** (undergrad)

M.Davis, R. Sigal, and E. Weyuker, **Computability, Complexity, and Languages: Fundamentals of Theoretical Computer Science** (undergrad/grad)