

# GRNPar: Parallel Inference of Gene Regulatory Networks Using Boolean Network Models and Mutual Information

Anushka Gupta (ag4351), William Das (whd2108)

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## 1 Introduction

Gene regulatory networks (GRNs) are graph-like representations of genes prone to activating or inhibiting the expression of other genes in a localized network. Boolean networks are often used to model GRNs—these networks consist of a series of nodes with connections between genes represented as boolean functions. Each node is a boolean variable that encodes its state (0 or 1). Each node’s state is determined by a boolean expression that takes as input the states of a subset of other nodes in the network. Researchers have developed algorithms for inferring these boolean expressions to model gene regulation activity.

For our project, we implemented a parallelized algorithm for inferring gene regulatory networks from gene expression time-series data using the boolean network model. Specifically, we modified a state-of-the-art approach put forth by Barman & Kwon (2017), which used a mutual information based approach coupled with a ”swapping” subroutine to select dependent genes in the network and infer logical relations between input and output nodes.

In particular, we implemented and parallelized: (1) a mutual information approach for inferring dependencies in a boolean network, (2) boolean expressions mapping input nodes to output nodes, optimizing for a ”gene-wise dynamics consistency” criterion, and a (3) method for visualizing and graphing the inferred boolean network. We parallelized each step, and specifically optimized key operations in the computation of possible boolean expressions that satisfy the various gene expression interactions in the network, where we saw the most speed-up.

### 1.1 Boolean Networks

The boolean network model  $G(V, A)$  proposed by Barman & Kwon consists of nodes:  $V = \{v_1, \dots, v_n\}$  and a set of interactions, or directed edges between input and output nodes:  $A = \{(v_i, v_j) \mid v_i, v_j \in V\}$ , where  $v_j$  is a target node whose state depends on that of  $v_i$ .

We further extend this model to account for boolean logic between the inferred input nodes and output nodes.

## 2 GRNPar Algorithm

### 2.1 Overview

We infer gene regulatory networks from time-series data by:

1. First, finding the  $k$  input nodes with the highest mutual information in relation to every target node.
2. Second, finding an optimal boolean expression that takes the  $k$  inferred input nodes with the highest dynamics criterion with respect to the target node. We choose the expression among a combination of  $2^{k-1}$  possible boolean expressions.

We also plot the inferred network to visualize our results as a final feature.

To determine the  $k$  most "closely related" input nodes for each node in the network, we used a mutual inference feature selection (MIFS) method based on entropy values (2.2.1). The testing of boolean expressions consists of finding possible boolean expressions which can be evaluated using the top  $k$  input nodes mapping to each target node, and choosing the one with highest gene-wise dynamics consistency (2.2.2).

Let  $V = \{\mathbf{v}_0, \mathbf{v}_1, \dots, \mathbf{v}_n\}$  where each vector  $\mathbf{v}_i$  corresponds to a gene and  $\mathbf{v}_i(t)$  corresponds to its value, 0 or 1, at time  $t$ .

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**Algorithm 1** GRNPar algorithm

---

```
procedure GRNPAR( $V$ )  
  network  $\leftarrow$  generateNetwork( $k, V$ )  
  optimalExpressions  $\leftarrow$  getOptimalBoolExpressions(network,  $|\mathbf{v}_0|$ )  
  networkImage  $\leftarrow$  plotBoolNetwork(network)  
  return network, optimalExpressions, networkImage  
end procedure
```

---

$|\mathbf{v}_0|$  in *getOptimalBoolExpressions* corresponds to a target node—given the network and connections generated, we iterate through each node and test for boolean expressions of its top  $k$  input nodes.

Finally, we plot the network as a directed graph, and return the inferred network, optimal boolean expressions for each node, and the image.

## 2.2 Criteria

### 2.2.1 Mutual Information

The mutual information metric used in Algorithm 2  $I(X; Y)$  is based on the entropy of two variables. First, the entropy  $H(X)$  of a discrete random variable (gene)  $X$  is defined to measure the uncertainty of  $X$  over all time steps. A joint entropy  $H(X, Y)$  between  $X$  and  $Y$  measures the joint probability distribution between  $X$  and  $Y$ . The mutual information metric is then calculated based on these two entropy values.

$$\begin{aligned} H(X) &= - \sum_{x \in X} (p(x) \log p(x)) \\ H(X, Y) &= - \sum_{x \in X} \sum_{y \in Y} (p(x) \log p(x)) \\ I(X; Y) &= H(X) + H(Y) - H(X, Y) \end{aligned}$$

### 2.2.2 Gene-wise Dynamics Consistency

Given the length of the time-series  $T$ , and the observed and inferred boolean states of a node  $v$  and  $v'$  across a time-series, respectively, the **gene-wise dynamics consistency** is:

$$E(v, v') = \frac{\sum_{t=2}^T I(v(t) = v'(t))}{T - 1} \quad (1)$$

where  $I(v(t) = v'(t))$  here is equal to 1 if the condition  $v(t) = v'(t)$  is true, and 0 if false.  $v'(t)$  is obtained from a possible boolean expression that maps the inferred input nodes at time  $t$  with the target node at  $v'(t)$ .

In essence, this criterion exposes the proportion of nodes whose states are predicted correctly given a boolean expression that outputs  $v'(t)$  at every timestep in the series. We used this criterion to choose an optimal boolean expression that maps the states of inferred input nodes to a target node.

### 2.2.3 searchUpdateRule

The `searchUpdateRule` function in `src/BDDUtils.hs` we implemented is where we search for possible boolean expressions that can be evaluated using the top  $k$  input nodes for each target node.

The authors from the original study included a second subroutine that iteratively swaps the selected  $k$  nodes with unselected nodes to see if different input nodes could yield higher dynamics consistency metrics—in their algorithm, the resulting number of input nodes could be less than or equal to  $k$ —whereas our implementation, due to time constraints, does not implement this swapping routine and selects a fixed  $k$  input nodes for each target node.

The essence of their swapping routine was a "search\_update\_rule" that searched through

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**Algorithm 2** Generation of Boolean Network

---

```
procedure GENERATENETWORK( $k, V$ )  
  for each node  $v_i \in V$  do  
    connections  $\leftarrow \{\}$   
    create empty BoolNetwork boolNetwork  
    for each node  $w \in W (W = V \setminus v_i)$  do  
      mutualInfo  $\leftarrow I(v_i, w)$   
      if mutualInfo in highest  $k$  values then  
        connections  $+= w$   
      end if  
      boolNetwork  $+= newNodeState(v_i, connections)$   
    end for  
  end for  
  return boolNetwork  
end procedure
```

---

---

**Algorithm 3** Optimal Boolean Expression Inference

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```
procedure GETOPTIMALBOOLEXPRESSIONS( $boolNetwork, timeLength$ )  
  for each node  $v_i \in$  the nodes in boolNetwork do  
    regulatoryNodes  $\leftarrow boolNetwork(v_i)$   
    allValidExpressions  $\leftarrow createExpressions(regulatoryNodes)$   
    for each expression  $exp \in allValidExpressions$  do  
      find expression with highest geneWiseDynamicCosnsitency value and return  
    end for  
  end for  
end procedure
```

---

possible boolean expressions between the selected input nodes and updated the rule for each target node with the boolean expression that yielded the highest dynamics consistency. Our implementation of this lies in *getOptimalBoolExpressions* (Algorithm 3).

## 3 Haskell Implementation

### 3.1 Data Types

#### 3.1.1 NodeState

*NodeState* represents the states of each node across the time-series. It consists of a *String* attribute as the name of the node/gene, and an  $[Int]$  to represent the boolean states/expression of that particular node across the time-series from time  $1..T$ , where  $T$  is the length of the time-series.

#### 3.1.2 BoolEdge

*BoolEdge* consists of two *NodeState* attributes— $v_i$  and  $v_j$ , which represents a directed edge dependency in the network from node  $v_i$  to  $v_j$ .

#### 3.1.3 BoolNetwork

*BoolNetwork* represents a boolean network as a directed graph. It contains a an attribute of  $[NodeState]$  consisting of the different nodes and their states across the time series, and an attribute of  $[BoolEdge]$  to represented the directed edges.

#### 3.1.4 BDD

*BDD* is a recursive data type similar to a binary decision diagram. We created a variation to represent and evaluate boolean expressions. *BDD* consists of several different states:

- *Name String*: Represents the name of a particular boolean variable.
- *State Int*: Represents the state, 1 or 0, of a particular boolean variable.
- *AND BDD BDD*: Represents an AND logical operation between two *BDD* types.
- *OR BDD BDD*: Represents an OR logical operation between two *BDD* types.
- *XOR BDD BDD*: Represents an XOR logical operation between two *BDD* types.
- *NOT BDD*: Represents a NOT operation to be applied to a *BDD*.

The idea with *BDD* is to map out a boolean expression specifying variable names, and supply a  $[(String, Int)]$  which consists of Int boolean values for each variable name to a *BDD* data type that can evaluate the expression—*evaluateFunc* in **src/BDDUtils.hs** performs this task, like so:

```

-- Define a boolean expression with variable names x, y, a, z:
f = XOR (AND (Name "x") (OR (Name "y") (Name "a"))) (NOT (Name "z"))

-- Evaluate function by supplying values for each variable:
fromEnum $ evaluateFunc f [("x", 1), ("y", 0), ("a", 1), ("z", 1)]

```

This outputs 1 when evaluated. For simplicity, based on the original algorithm, we only look at a combination of conjunctive and disjunctive operations (AND/OR) evaluated using the top  $k$  input nodes, sorted in descending order based on each node's mutual information in relation to the target node.

## 3.2 Generating Random Time-Series Data

We generate random time series gene expression data in `src/generate_data.py`, which takes as input the number of nodes and timesteps—boolean states are randomly generated at each timestep.

# 4 Code Analysis

### 4.0.1 Mutual Information

First, we find the top  $k$  input nodes for each node in `genBoolEdgesSeq`, combining it into one list of `BoolEdge` and creating a `BoolNetwork` with the observed `nodeStates` and all of the generated `BoolEdge` connections (set of interactions).

```

genNetworkSeq :: [NodeState] -> Int -> BoolNetwork
genNetworkSeq nodeStates k = BoolNetwork nodeStates (combineEdgesSeq
  → nodeStates k)

combineEdgesSeq :: [NodeState] -> Int -> [BoolEdge]
combineEdgesSeq nodeStates k = concatMap (genBoolEdgesSeq nodeStates k)
  → nodeStates

genBoolEdgesSeq :: [NodeState] -> Int -> NodeState -> [BoolEdge]
genBoolEdgesSeq nodeStates k targetNode =
  let topKMutual = getMutualInfoSeq targetNode (filter (/= targetNode)
    → nodeStates) k
      in map (`BoolEdge` targetNode) topKMutual

```

### 4.0.2 Extracting Optimal Boolean Expressions

Next, we determine the optimal boolean expressions (`getOptimalBoolExpressions` - line 223 `BDDUtils.hs`) for each input node. Using the `boolNetwork` and top  $k$  connections generated for each node, we generate a set of  $2^{k-1}$  possible boolean expressions and use each expression to infer a time-series to compare with the observed expressions of each node and calculate the gene-wise dynamics consistency (`searchUpdateRule` - line 169 `BDDUtil.hs`).

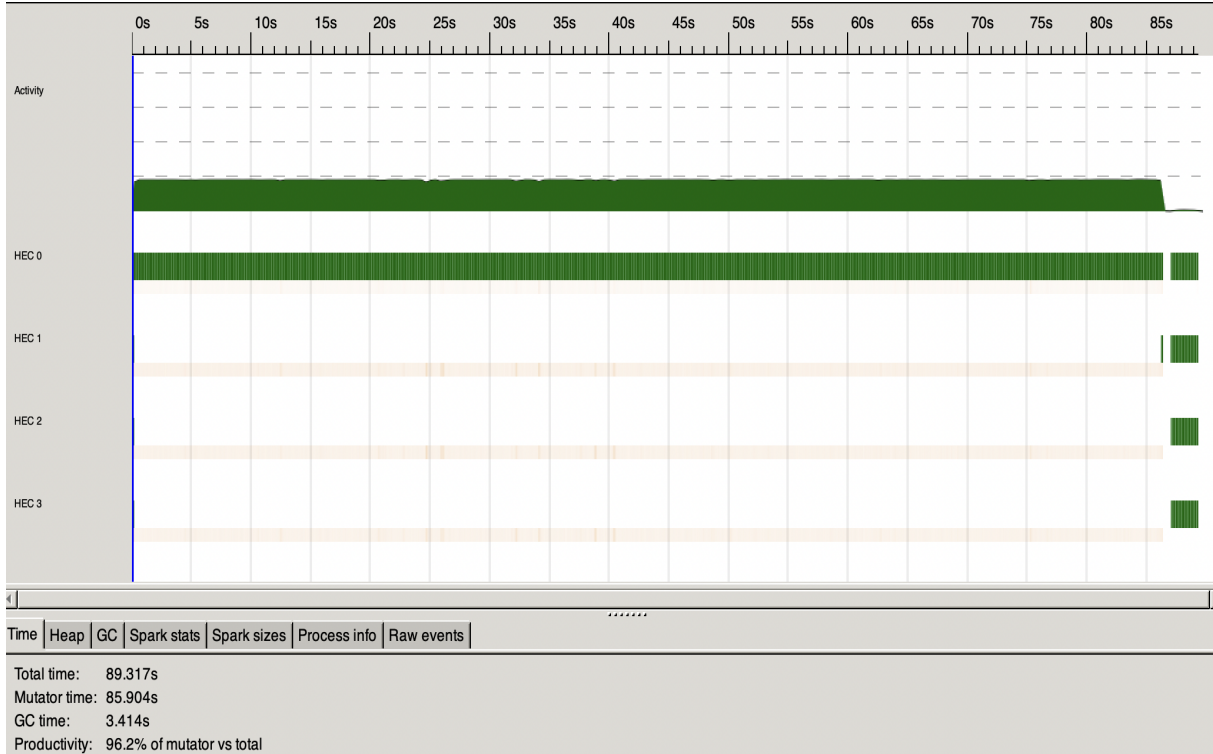


Figure 1: Sequential program for a randomized sample where 300 nodes are generated for 300 time steps and  $k=5$

For each boolean expression, we take the state of each target node from time 2 to time  $T$ , and infer its value at every timestep  $t$  by evaluating the expression using the states of the selected  $k$  input nodes at time  $t-1$ . Using the inferred time series expression for the target node, we compare it with observed time series expression for the target node, and calculate the dynamics consistency. We choose the boolean expression that maximizes the genewise dynamics consistency for each target node, and assign that expression to it.

Lastly, we plot the BoolNetwork using the Data.Graph.DGraph library and graphviz library.

```
plotBoolNetworkPng :: BoolNetwork -> FilePath -> Bool -> IO FilePath
plotBoolNetworkPng network fname labelEdges = plotDGPng networkDG fname
  ↪ labelEdges
  where
    networkDG = boolNetworkToDG network labelEdges
```

## 5 Parallel Solution

We used `genNetworkPar`, `getOptimalBoolExpressionsPar`, and `plotBoolNetworkPngPar` in `Main.hs` to run parallel strategies. We made `NFData` instances for `NodeState`, `BoolEdge`,

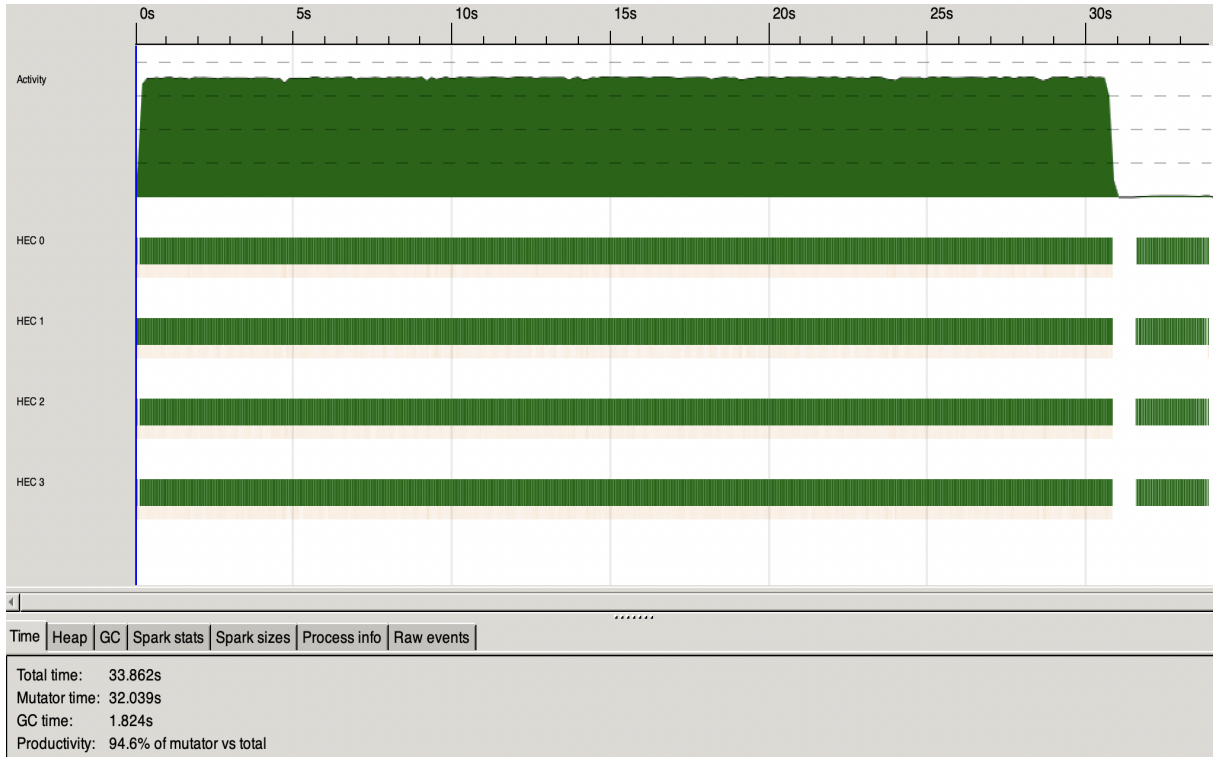


Figure 2: Parallel program for a randomized sample where 300 nodes are generated for 300 time steps and  $k=5$

and `BoolNetwork` to perform these computations.

There are three layers of parallelism applied to the implementation to improve the performance of the program. The first layer uses the `parMap deepSeq` functions from the package `Control.Parallel.Strategies`. The second and third layer use `parBuffer` and `parChunkList`, respectively.

We used `parMap rdeepseq` to parallelize map computations. We used `parMap` to combine the results of generating the top  $k$  connections into one list, shown in the new `combineEdgesPar` function in `GRPPar.hs`. Similarly, when parsing through all the possible nodes to determine the top  $k$  nodes based on mutual information, we applied `parMap rdeepseq` and ran the calculations in parallel.

```
allMutualInfo =
  map (\inp ->
    (inp, mutualInformation (timeStates inp) (timeStates targetNode)
      - sum (parMap rdeepseq (mutualInformation (timeStates inp) . timeStates)
        $ map fst regNodes))) inpNodes `using` parBuffer 3 rdeepseq
```

Here, we use `parBuffer` to iterate through the input nodes and calculate mutual information.



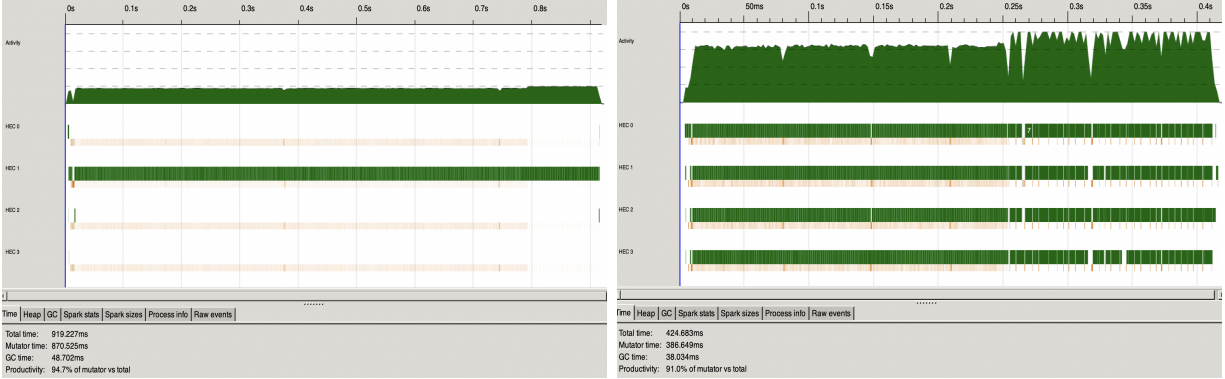


Figure 3: Sequential (left) and Parallel (right) program for GRNPar on Insilico E. coli Dataset using 4 cores.  $k = 8$ .

Figure 2 shows the eventlog when running parallel on a randomly generated time-series containing 300 nodes and 300 timesteps. The test was run on 4 cores with  $k = 5$ . The average runtime was 33.9 seconds.

## 6 Performance Analysis

### 6.1 Results

#### 6.1.1 Real-world Datasets

We tested GRNPar with three real gene expression datasets: an E. coli network with 10 genes and 20 timesteps, an Insilico E.coli network with 100 genes and 20 timesteps, and a fission yeast cell cycle network with 10 genes and 10 timesteps. We discretized the InSilico data using a rudimentary KMeans clustering algorithm, and the other datasets had been discretized to boolean states using KMeans clustering prior by Barman & Kwon.

We ran the Insilico E. coli dataset through GRNPar, only generating the network without computing expressions or outputting an image, both in parallel and sequentially—the results are shown in Figure 3. There was a 2.16x speedup in total time and 2.25x reduction in mutator time from the sequential to parallel run.

When running the Insilico data through GRNPar, there was an extra period for generating the image, in both the sequential and parallel versions of the algorithm. This is seen in the extra time taken to complete the algorithm in Figure 4. In both the sequential and parallel algorithms, it took 1.5 seconds extra to run as compared with the runs when the graph image was not generated.

The graph generated for the Insilico set is shown in figure 5. There is a tendency for the central nodes to be in the center of the graph, as they have more dependencies. Figure 6 shows the graphs generated by testing GRNPar on the other E. coli dataset and fission yeast cell cycle network—similar to the Insilico set, we observe 3.33x speedup between the

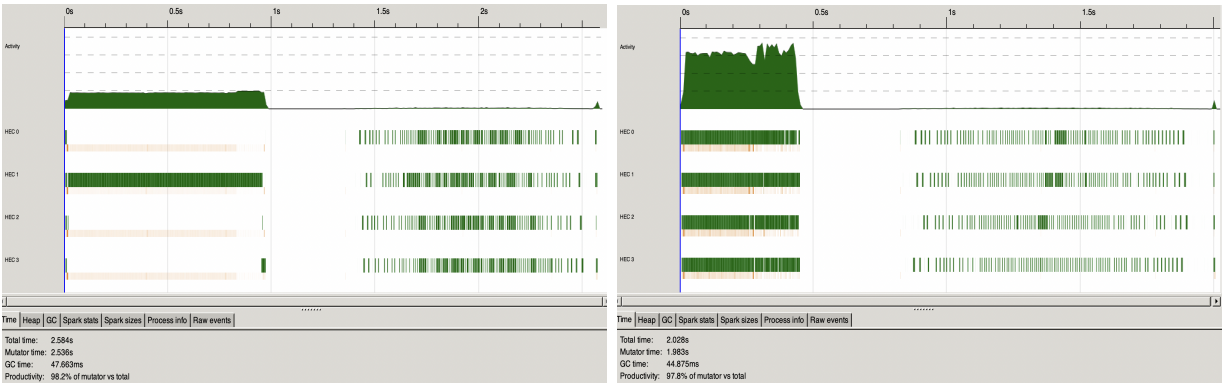


Figure 4: Generation of network + plotting image -i both the sequential (left) and parallel (right) implementation took 1.5 extra seconds, compared to figure 3

sequential and parallel usage of GRNPar.

### 6.1.2 Randomly Generated Data

We also analyzed how changing the number of nodes (genes), cores, and k-values affected performance of GRNPar on randomly generated time-series expression data. Figure 8 shows three tables worth of runtime data. In Table 1, as the number of nodes (genes) increases, the runtime for sequential GRNPar increases at a much larger rate than parallel GRNPar. However, when compared with the parallel runtime in Table 2 (Figure 8), the sequential runtime increases as the number of cores increases, since unnecessary garbage collection occurs during the sequential run as more cores are added on.

## 6.2 Running GRNPar

This program takes in five arguments:

```
1 stack exec GRNPar-exe <csvFilename> <k> <genExpressions> <genImage> <mode>
```

Specific implementation details can be found in the README. The output of the program is a .png file that has the boolean network mapped out in src/output\_files.

## 7 References

Barman S, Kwon YK (2017) A novel mutual information-based Boolean network inference method from time-series gene expression data. PLOS ONE 12(2): e0171097. <https://doi.org/10.1371/journal.pone.0171097>

Prill RJ, Marbach D, Saez-Rodriguez J, Sorger PK, Alexopoulos LG, Xue X, et al. Towards a Rigorous Assessment of Systems Biology Models: The DREAM3 Challenges. PLOS One.

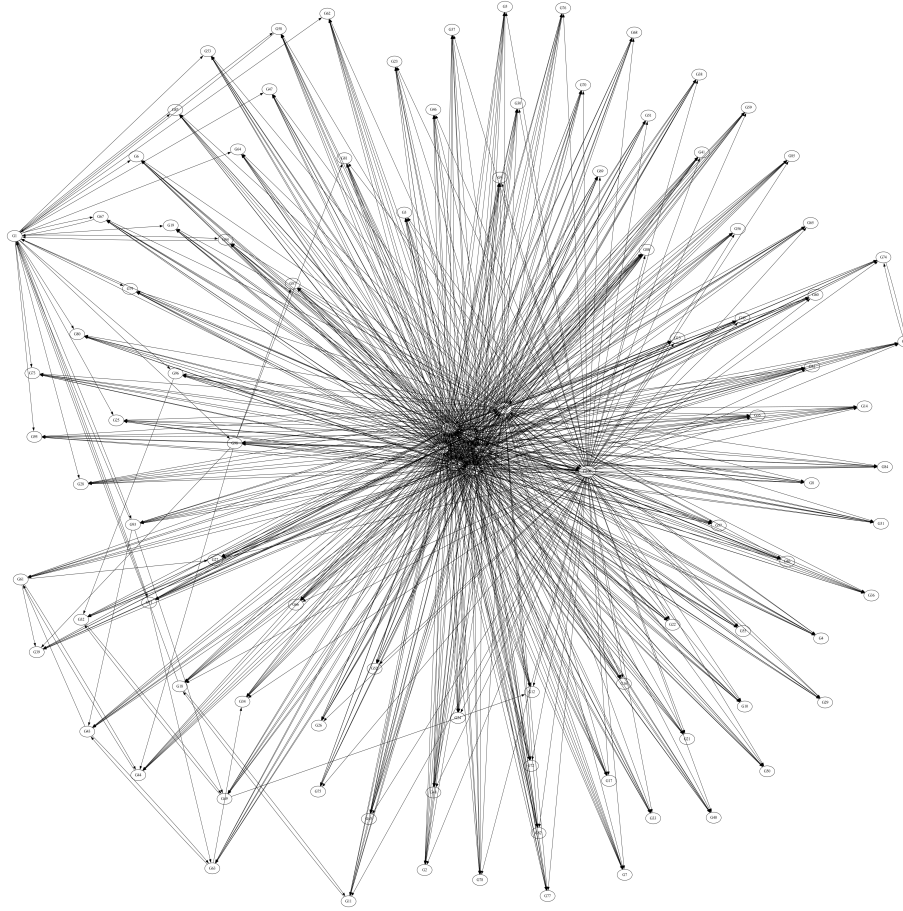


Figure 5: Boolean Network Inferred for InSilico Ecoli Protein Trajectories

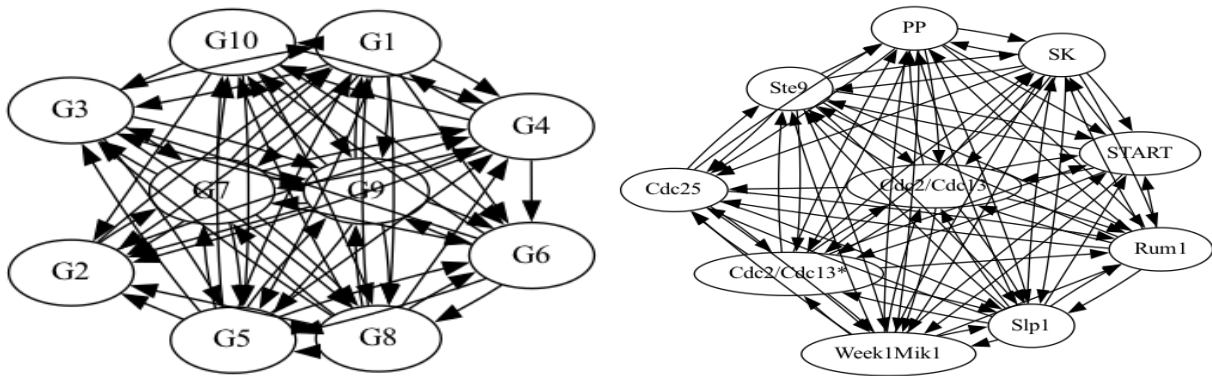


Figure 6: E. coli gene regulatory network(left) & a fission yeast cell cycle network (right)

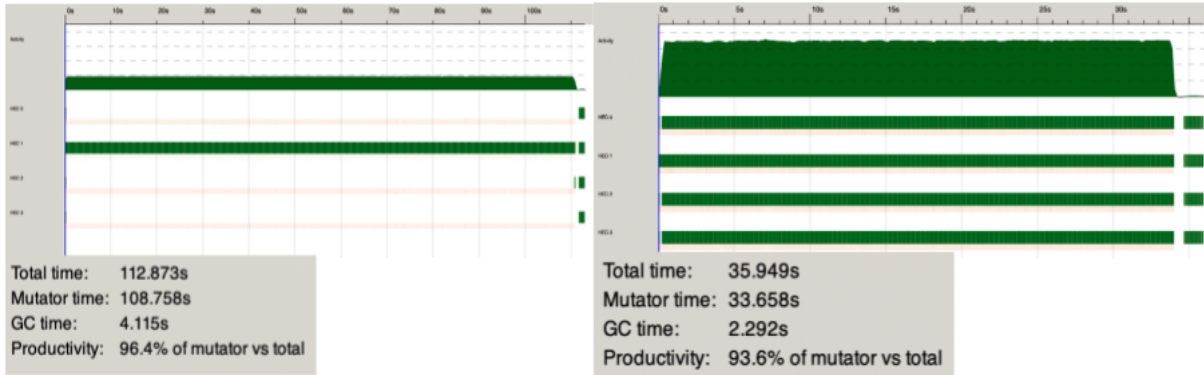


Figure 7: Randomly Generated Data: 500 Nodes over 300 time steps (4 cores) in a sequential and parallel method

Cores = 4, k = 3			Nodes = 300, k = 5			Nodes = 300, Cores = 4			
		runtime						runtime	
Nodes	par	seq	Cores	par	seq	k	par	seq	
100	1.732	4.779	4	12.714	40.147	3	12.493	41.234	
300	13.859	40.278	5	11.586	40.825	4	18.758	62.14	
500	36.603	111.648	6	9.948	42.407	5	27.429	87.863	
1000	137.177	482.837	7	9.096	44.005	6	39.134	122.933	
			8	9.095	44.932				

Figure 8: From left to right, Table 1, 2, 3. Table 1: Change in runtime for a parallel and sequential implementation as the number of nodes increases. Table 2: Change in runtime for a parallel and sequential implementation as the number of cores increases. Table 3: Change in runtime for a parallel and sequential implementation as the k value increases

## 8 Code Listing

### 8.1 app/Main.hs

```
1  {-
2  Main application program:
3  -}
4
5  module Main (main) where
6
7  import System.IO ()
8  import System.Environment (getArgs)
9  import Control.Monad
10
11 import GRNPar (genNetworkSeq, genNetworkPar)
12 import GraphUtils (plotBoolNetworkPng, plotBoolNetworkPngPar, NodeState(..))
13 import BDDUtils (getOptimalBoolExpressions, getOptimalBoolExpressionsPar)
14 import ProcessData (csvToNodeStates)
15
16 import Control.DeepSeq
17
18 {-
19 Main script:
20     1. Infer + generate boolean network from input file
21     2. Determine optimal boolean expression
22     3. Output network to png file
23
24 Usage: GRNPar-exe <csvFilename> <k> <outputFile> <genExpressions> <genImage>
25     ↪ <mode>
26 -}
27 main :: IO ()
28 main = do
29     args <- getArgs
30     case args of
31         [fname, k, genExpressions, genImage, mode] -> do
32             putStrLn fname
33             putStrLn "Parsing data..."
34             nodeStates@(x:_) <- csvToNodeStates fname 1
35
36             -- Generate network with dependencies
37             let k'          = read k :: Int
38                 timeLength = length $ timeStates x
39                 network    = if mode == "par"
40                             then force $ genNetworkPar nodeStates k'
41                             else force $ genNetworkSeq nodeStates k'
42             putStrLn "Generated network."
43
44         _ -> when (genExpressions == "1") $ do
```

```

44         -- Get optimal boolean expressions for each node
45         let optimalExpressions = if mode == "par"
46                                     then force $
↪   getOptimalBoolExpressionsPar network timeLength
47                                     else force $
↪   getOptimalBoolExpressions network timeLength
48         putStrLn "Optimal boolean expressions for each variable:"
49         mapM_ (\(n, b, c) -> putStrLn $ name n ++ " = " ++ show b ++
↪   ". Gene-wise consistency: " ++ show c) optimalExpressions
50         --print optimalExpressions
51
52         when (genImage == "1") $ do
53             -- Print image
54             let outputFile = "src/output_files/" ++ substring (length
↪   "src/data/") (length fname - 4) fname
55             print outputFile
56             imgFilePath <- if mode == "par"
57                                     then plotBoolNetworkPngPar network
↪   outputFile False
58                                     else plotBoolNetworkPng network outputFile
↪   False
59             putStrLn $ "Printed to " ++ imgFilePath ++ "."
60
61             putStrLn "Finished."
62             _ -> putStrLn "Usage: GRNPar-exe <csvFilename> <k> <outputFile>
↪   <genExpressions> <genImage> <mode>"
63
64 substring :: Int -> Int -> String -> String
65 substring x y s = take (y - x) (drop x s)

```

## 8.2 src/GRNPar.hs

```

1 {-# LANGUAGE ParallelListComp #-}
2
3 module GRNPar
4     ( genNetworkSeq
5     , genNetworkPar
6     ) where
7
8
9 import Control.Monad ()
10
11 import qualified Data.Map as Map
12 import Data.Ord (comparing)
13 import Data.List (maximumBy, sortBy)
14
15 import GraphUtils (NodeState(..), BoolEdge(..), BoolNetwork(..))

```

```

16
17 import Control.Parallel.Strategies (parMap, rdeepseq, parBuffer, using)
18 import Control.DeepSeq ()
19
20 {-
21 -- Testing with sample nodes:
22 x_1 :: NodeState
23 x_1 = NodeState "x_1" [1, 1, 0, 0, 0, 1, 0, 1]
24
25 x_2 :: NodeState
26 x_2 = NodeState "x_2" [1, 0, 1, 0, 1, 0, 1, 0]
27
28 x_3 :: NodeState
29 x_3 = NodeState "x_3" [1, 0, 1, 0, 1, 0, 1, 0]
30
31 x_4 :: NodeState
32 x_4 = NodeState "x_4" [1, 0, 0, 0, 1, 0, 1, 1]
33
34 x_5 :: NodeState
35 x_5 = NodeState "x_5" [1, 0, 1, 0, 0, 0, 0, 0]
36
37 x_6 :: NodeState
38 x_6 = NodeState "x_6" [1, 1, 0, 0, 1, 1, 1, 0]
39
40 sampleNodes :: [NodeState]
41 sampleNodes = [x_1,x_2,x_3,x_4,x_5,x_6]
42 -}
43
44 {-
45 Parallel pipeline for inferring boolean network given NodeState data.
46 -}
47 genNetworkPar :: [NodeState] -> Int -> BoolNetwork
48 genNetworkPar nodeStates k = BoolNetwork nodeStates (combineEdgesPar nodeStates
  ↪ k)
49
50 {-
51 Sequential pipeline for inferring boolean network given NodeState data.
52 -}
53 genNetworkSeq :: [NodeState] -> Int -> BoolNetwork
54 genNetworkSeq nodeStates k = BoolNetwork nodeStates (combineEdgesSeq nodeStates
  ↪ k)
55
56 {-
57 Combine all BoolEdge connections for each target node into one array.
58 -}
59 combineEdgesSeq :: [NodeState] -> Int -> [BoolEdge]
60 combineEdgesSeq nodeStates k = concatMap (genBoolEdgesSeq nodeStates k)
  ↪ nodeStates

```

```

61
62 {-
63 Generate BoolEdge connections in network given NodeState and a targetNode
64 -}
65 genBoolEdgesSeq :: [NodeState] -> Int -> NodeState -> [BoolEdge]
66 genBoolEdgesSeq nodeStates k targetNode =
67   let topKMutual = getMutualInfoSeq targetNode (filter (/= targetNode)
68     ↪ nodeStates) k
69   in map (`BoolEdge` targetNode) topKMutual
70
71 combineEdgesPar :: [NodeState] -> Int -> [BoolEdge]
72 combineEdgesPar nodeStates k = concat $ parMap rdeepseq (genBoolEdgesPar
73   ↪ nodeStates k) nodeStates
74
75 genBoolEdgesPar :: [NodeState] -> Int -> NodeState -> [BoolEdge]
76 genBoolEdgesPar nodeStates k targetNode = map (`BoolEdge` targetNode) topKMutual
77   where
78     topKMutual = getMutualInfoPar targetNode (filter (/= targetNode) nodeStates)
79     ↪ k
80
81 {-
82 Get top k input nodes with the highest mutual information relative to a target
83 ↪ node.
84
85 Return input nodes sorted descending based on mutual information with target
86 ↪ node.
87
88 * inputNodes should not contain targetNode when calling getMutualInfo
89 -}
90 getMutualInfoSeq :: NodeState -> [NodeState] -> Int -> [NodeState]
91 getMutualInfoSeq targetNode inputNodes k = map fst
92   $ sortBy (flip (comparing snd))
93   $ getMutualInfo' [maxMutualNodeInfo]
94   (filter (/= maxMutual) inputNodes) k
95
96 where
97   maxMutualNodeInfo@(maxMutual, _) = maximumBy (comparing snd)
98     $ map (\inp -> (inp, mutualInformation
99     ↪ (timeStates inp) (timeStates targetNode))) inputNodes
100   getMutualInfo' :: [(NodeState, Double)] -> [NodeState] -> Int -> [(NodeState,
101     ↪ Double)]
102   getMutualInfo' regNodes inpNodes k'
103     | length regNodes == k' = regNodes
104     | otherwise =
105       let newMaxInfo@(newMax, _) = maximumBy (comparing snd)
106         $ map (\inp -> (inp, mutualInformation
107         ↪ (timeStates inp) (timeStates targetNode)
108         ↪ - sum (map (mutualInformation
109         ↪ (timeStates inp) . timeStates) $ map fst regNodes))) inpNodes

```



```

100         newInpNodes          = filter (/= newMax) inpNodes
101         newRegNodes          = regNodes ++ [newMaxInfo]
102         in getMutualInfo' newRegNodes newInpNodes k'
103
104 getMutualInfoPar :: NodeState -> [NodeState] -> Int -> [NodeState]
105 getMutualInfoPar targetNode inputNodes k = map fst
106                                             $ sortBy (flip (comparing snd))
107                                             $ getMutualInfo' [maxMutualNodeInfo]
108                                             (filter (/= maxMutual) inputNodes) k
109     where
110         mutualInfo'                = map (\inp -> (inp, mutualInformation
111 ↪ (timeStates inp) (timeStates targetNode)))
112                                     inputNodes `using` parBuffer 3
113 ↪ rdeepseq
114     maxMutualNodeInfo@(maxMutual, _) = maximumBy (comparing snd) mutualInfo'
115     getMutualInfo' :: [(NodeState, Double)] -> [NodeState] -> Int -> [(NodeState,
116 ↪ Double)]
117     getMutualInfo' regNodes inpNodes k'
118     | length regNodes == k' = regNodes
119     | otherwise              =
120 ↪ let allMutualInfo          = map (\inp -> (inp, mutualInformation
121 ↪ (timeStates inp) (timeStates targetNode)
122 ↪ - sum (parMap rdeepseq
123 ↪ (mutualInformation (timeStates inp) . timeStates) $ map fst regNodes)))
124 ↪ inpNodes `using` parBuffer 3
125 ↪ rdeepseq
126     newMaxInfo@(newMax, _) = maximumBy (comparing snd) allMutualInfo
127     newInpNodes            = filter (/= newMax) inpNodes
128     newRegNodes            = regNodes ++ [newMaxInfo]
129     in getMutualInfo' newRegNodes newInpNodes k'
130
131 -- Compute the entropy of a list of numerical values
132 entropy :: (Ord a) => [a] -> Double
133 entropy xs = sum [ -p * logBase 2 p | p <- ps ]
134     where
135         counts = Map.fromListWith (+) [(x, 1 :: Int) | x <- xs]
136         values = Map.elems counts
137         total  = sum values
138         ps     = [fromIntegral v / fromIntegral total | v <- values]
139
140 -- Compute the mutual information of discrete variables x and y
141 mutualInformation :: (Ord a) => [a] -> [a] -> Double
142 mutualInformation xs ys = entropy xs + entropy ys - entropy (zip xs ys)

```

## 8.3 src/GraphUtils.hs

```
1 module GraphUtils
2   ( NodeState(..)
3   , BoolEdge(..)
4   , BoolNetwork(..)
5   , plotBoolNetworkPng
6   , plotBoolNetworkPngPar
7   , plotDGPng
8   ) where
9
10 import Data.GraphViz
11 import Data.GraphViz.Attributes.Complete
12 import Data.Hashable
13
14 import Control.Parallel.Strategies (parListChunk, rdeepseq, using)
15 import Control.DeepSeq (NFData(..))
16
17 import qualified Data.Text.Lazy    as TL
18 import qualified Data.Graph.DGraph as DG
19 import qualified Data.Graph.Types  as GT
20
21 {-
22  Data types representing boolean states of genes and boolean network consisting of
23  → NodeStates and directed edges.
24
25  - NodeState:
26    - name :: String -> name of gene
27    - timeStates :: [Int] -> expression of gene across time-series in order
28  -}
29 data NodeState = NodeState { name :: String
30                             , timeStates :: [Int] } deriving (Eq, Ord)
31
32 instance Show NodeState where
33   show (NodeState n _) = n
34
35 instance NFData NodeState where
36   rnf (NodeState n ts) = rnf n `seq` rnf ts
37
38 {-
39  - BoolEdge
40    - v_i :: NodeState -> source node
41    - v_j :: NodeState -> target node
42  -}
43 data BoolEdge = BoolEdge { v_i :: NodeState
44                           , v_j :: NodeState } deriving (Eq)
45
```

```

46 instance Show BoolEdge where
47     show (BoolEdge i j) = "(" ++ name i ++ " -> " ++ name j ++ ")"
48
49 instance NFData BoolEdge where
50     rnf (BoolEdge i j) = rnf i `seq` rnf j
51
52 {-
53 - BoolNetwork
54   - nodes :: [NodeState] -> all nodes/genes in network
55   - connections :: [BoolEdge] -> directed edges between genes
56 -}
57 data BoolNetwork = BoolNetwork { nodes :: [NodeState]
58                                 , connections :: [BoolEdge] } deriving (Eq, Show)
59 instance NFData BoolNetwork where
60     rnf (BoolNetwork n c) = rnf n `seq` rnf c
61
62 {-
63 Modified from graphite lib source code:
64 - Functions for plotting directed graph and BoolNetwork to png file
65 - graphviz needs to be installed on local machine to see output:
66   - brew install graphviz
67     OR
68   - sudo apt install graphviz
69
70 Example: Plot DGraph foundationUniverse to "foundation.png"
71
72 foundationUniverse :: DG.DGraph String Double
73 foundationUniverse = DG.fromArcsList
74   [ GT.Arc "Helicon" "Nishaya" 200.00
75     , GT.Arc "Helicon" "Wencory" 382.20
76     , GT.Arc "Nishaya" "Wencory" 820.32
77   ]
78
79 plotDGraphPng foundationUniverse "foundation"
80
81 -}
82 -- Plot a BoolNetwork to png file
83 boolNetworkToDG :: BoolNetwork -> Bool -> DG.DGraph String String
84 boolNetworkToDG network labelEdges = DG.fromArcsList
85     $ map (\(BoolEdge inp out) ->
86         GT.Arc (name inp) (name out) (if
87     ↪ labelEdges then "test" else ""))
88         (connections network)
89
90 -- Plot a BoolNetwork to png file
91 boolNetworkToDGPar :: BoolNetwork -> Bool -> DG.DGraph String String
92 boolNetworkToDGPar network labelEdges = DG.fromArcsList

```

```

92         (map (\(BoolEdge inp out) ->
93             GT.Arc (name inp) (name out) (if
94                 labelEdges then "test" else ""))
95                 (connections network)
96                 `using` parListChunk 50 rdeepseq)
97
98 -- Plot BoolNetwork to png file
99 plotBoolNetworkPng :: BoolNetwork -> FilePath -> Bool -> IO FilePath
100 plotBoolNetworkPng network fname labelEdges = plotDGPng networkDG fname
101     labelEdges
102     where
103         networkDG = boolNetworkToDG network labelEdges
104
105 plotBoolNetworkPngPar :: BoolNetwork -> FilePath -> Bool -> IO FilePath
106 plotBoolNetworkPngPar network fname labelEdges = plotDGPng networkDG fname
107     labelEdges
108     where
109         networkDG = boolNetworkToDGPar network labelEdges
110
111 -- | Plot a directed 'DGraph' to a PNG image file
112 plotDGPng :: (Hashable v, Ord v, PrintDot v, Show v, Show e)
113     => DG.DGraph v e
114     -> FilePath
115     -> Bool
116     -> IO FilePath
117 plotDGPng g fname labelEdges = addExtension (runGraphvizCommand Sfdp $
118     toDirectedDot labelEdges g) Png fname
119
120 labeledNodes :: (GT.Graph g, Show v) => g v e -> [(v, String)]
121 labeledNodes g = (\v -> (v, show v)) <$> GT.vertices g
122
123 labeledArcs :: (Hashable v, Eq v, Show e) => DG.DGraph v e -> [(v, v, String)]
124 labeledArcs g = (\(GT.Arc v1 v2 attr) -> (v1, v2, show attr)) <$> DG.arcs g
125
126 toDirectedDot :: (Hashable v, Ord v, Show v, Show e)
127     => Bool -- ^ Label edges
128     -> DG.DGraph v e
129     -> DotGraph v
130 toDirectedDot labelEdges g = graphElemsToDot params (labeledNodes g) (labeledArcs
131     g)
132     where params = sensibleDotParams True labelEdges
133
134 sensibleDotParams
135     :: Bool -- ^ Directed
136     -> Bool -- ^ Label edges
137     -> GraphvizParams t l String () l
138 sensibleDotParams directed edgeLabeled = nonClusteredParams

```

```

134     { isDirected = directed
135     , globalAttributes =
136         [ GraphAttrs [Overlap ScaleOverlaps]
137         , EdgeAttrs [FontColor (X11Color DarkGreen)]
138         ]
139     , fmtEdge = edgeFmt
140     }
141     where
142         edgeFmt (_, _, l) = if edgeLabeled
143             then [Label $ StrLabel $ TL.pack l]
144             else []

```

## 8.4 src/BDDUtils.hs

```

1  {-# LANGUAGE TupleSections #-}
2
3  module BDDUtils
4      ( BDD(..)
5      , evaluateFunc
6      , getOptimalBoolExpressions
7      , getOptimalBoolExpressionsPar
8      , getRegulatoryNodes
9      , searchUpdateRule
10     , getBDDFromFunc
11     ) where
12
13  import GraphUtils (NodeState(..), BoolEdge(..), BoolNetwork(..))
14
15  import Data.Ord (comparing)
16  import Data.List (maximumBy)
17
18  import qualified Data.Matrix as M
19  import qualified Data.Vector as Vec
20
21  import Control.Parallel.Strategies (parMap, rdeepseq, using, parListChunk,
22     ↪ parBuffer)
23
24  import Control.DeepSeq (NFData(..))
25
26  {-
27  Functions for evaluating and representing binary decision diagrams.
28  -}
29
30  {-
31  Binary decision diagram data type used for evaluating boolean expressions.
32  -}
33
34  Example:
35  - f = XOR (AND (Name "x") (OR (Name "y") (Name "a"))) (NOT (Name "z"))

```

```

33 - fromEnum $ evaluateFunc f [("x", 1), ("y", 0), ("a", 1), ("z", 1)]
34   - Output: 1
35 -}
36
37 -- Define binary decision diagram
38 data BDD = Name String -- name of node (gene name)
39         | State Int -- state of node (0 or 1)
40         | AND BDD BDD -- an AND node
41         | OR BDD BDD -- an OR node
42         | XOR BDD BDD -- an XOR node
43         | NOT BDD -- a NOT node
44         deriving (Eq)
45
46 instance Show BDD where
47   show (Name x) = x
48   show (State x) = show x
49   show (AND x y) = "(" ++ show x ++ " AND " ++ show y ++ ")"
50   show (OR x y) = "(" ++ show x ++ " OR " ++ show y ++ ")"
51   show (XOR x y) = "(" ++ show x ++ " XOR " ++ show y ++ ")"
52   show (NOT x) = "(NOT " ++ show x ++ ")"
53
54 instance NFData BDD where
55   rnf (Name x) = rnf x
56   rnf (State x) = rnf x
57   rnf (AND x y) = rnf x `seq` rnf y
58   rnf (OR x y) = rnf x `seq` rnf y
59   rnf (XOR x y) = rnf x `seq` rnf y
60   rnf (NOT x) = rnf x
61
62 {-
63 Evaluate a boolean expression given a BDD data type and a list of tuples
64   ↪ specifying values for each variable.
65
66 Params:
67 - BDD data type
68 - func: list of tuples [(varName, value)], where varName is a boolean variable
69   ↪ name in the BDD, and value is the value assigned to it
70
71 Example:
72 - f = XOR (AND (Name "x") (OR (Name "y") (Name "a"))) (NOT (Name "z"))
73 - fromEnum $ evaluateFunc f [("x", 1), ("y", 0), ("a", 1), ("z", 1)]
74   - Output: 1
75 -}
76 -- evaluate a BDD for a given assignment of the variables
77 evaluateFunc :: BDD -> [(String, Int)] -> Bool
78 evaluateFunc (Name x) func = case lookup x func of

```

```

78             Just a -> a == 1
79             Nothing -> error "Variable not in assignment"
80 evaluateFunc (AND x y) func = evaluateFunc x func && evaluateFunc y func
81 evaluateFunc (OR x y) func = evaluateFunc x func || evaluateFunc y func
82 evaluateFunc (XOR x y) func
83   | andTrue = False
84   | otherwise = evaluateFunc (OR x y) func
85 where
86   andTrue = evaluateFunc x func && evaluateFunc y func
87 evaluateFunc (NOT b) func = not (evaluateFunc b func)
88 evaluateFunc (State x) _
89   | x == 1 = True
90   | otherwise = False
91
92
93 {-
94 Get gene wise dynamics consistency metric given a predicted time series and the
95 ↪ actual time series.
96
97 Params:
98 - predictedStates :: [Int]
99 - actualStates :: [Int]
100 -}
101 geneWiseDynamicsConsistency :: [Int] -> [Int] -> Double
102 geneWiseDynamicsConsistency predictedStates actualStates = sumPredictions /
103 ↪ fromIntegral timeLength
104 where
105   sumPredictions = sum $ zipWith (\x y -> if x == y then 1 :: Double else 0 ::
106 ↪ Double) predictedStates actualStates
107   timeLength = length predictedStates
108
109 {-
110 Get all combinations of conjunctive and disjunctive boolean expressions.
111
112 Params:
113 - n :: Int -> number of operators to evaluate
114
115 Returns:
116 - [[Int]] -> list of Int lists, where each list corresponds to a sequence of
117 ↪ AND/OR operations.
118
119 Each list, e.g. [1, 0, 1], signifies a sequence of AND/OR operators, where 1 =
120 ↪ AND and 0 = OR
121
122 Example: given a list of truth values, such as [1, 0, 0, 1], and a boolean
123 ↪ expression combination represented as [1, 0, 1]:

```

```

119     - Using the BDD data type, we would evaluate this as: ((1 AND 0) OR 0) AND 1
120 -}
121 getConjDisjCombos :: Int -> [[Int]]
122 getConjDisjCombos 1 = [[0], [1]]
123 getConjDisjCombos n = [[mod x 2^i | i <- [0..n-1]] | x <- [0..(2^n)-1]]
124
125
126 {-
127 Construct a BDD given boolean variable names and a combination of
  ↪ conjunctive/disjunctive operations.
128
129 Params:
130 - (x:xs) :: [String] -> boolean variable names
131 - ops :: [Int] -> conjunctive/disjunctive combinations as one element outputted
  ↪ by getConjDisjCombos
132
133 Returns: BDD
134
135 The number of variables should always be 1 more than the number of operations.
136
137 Example:
138 - getBDDFromFunc ["v1", "v2", "v3"] [1, 0] returns a BDD of: ((v1 AND v2) OR v3)
139 - bdd = getBDDFromFunc ["v1", "v2", "v3"] [1, 0]
140 - fromEnum $ evaluateFunc bdd [("v1", 1), ("v2", 0), ("v3", 1)]
141   - Output: 1
142 -}
143 getBDDFromFunc :: [String] -> [Int] -> BDD
144 getBDDFromFunc [] _ = error "Invalid input."
145 getBDDFromFunc [_] _ = error "Invalid input."
146 getBDDFromFunc (x:xs) ops = foldl (\acc (y, ys) -> if ys == 1 then AND acc (Name
  ↪ y) else OR acc (Name y)) (Name x) tailZipped
147   where
148     tailZipped = zip xs ops
149
150 {-
151 Get regulatory genes of node given target node and boolean network.
152
153 Params:
154 - targetNode: target gene
155 - network    : BoolNetwork
156 -}
157 getRegulatoryNodes :: NodeState -> BoolNetwork -> [NodeState]
158 getRegulatoryNodes targetNode network = map v_i $ filter (\(BoolEdge _ out) ->
  ↪ out == targetNode) $ connections network
159
160
161 {-

```



```

162 Compute genewise dynamics consistency metric for possible boolean expressions in
    ↪ input nodes sorted by mutual information.
163
164 Params:
165 - inpNodes :: [NodeState] -> top k input nodes with highest mutual information
    ↪ with respect to targetNode
166 - targetNode :: NodeState
167 - timeLength :: Int -> length of time series
168 -}
169 searchUpdateRule :: [NodeState] -> NodeState -> Int -> [(Double, BDD)]
170 searchUpdateRule inpNodes targetNode timeLength =
171     case allTargetStates of
172     []           -> error "Invalid target states."
173     [_]         -> error "Invalid target states."
174     (_:targetStates) -> map (\(p, r) -> (geneWiseDynamicsConsistency p
    ↪ targetStates, r)) predStates
175     where
176     -- Get target states of target node
177     allTargetStates = timeStates targetNode
178
179     inpNodeNames = map name inpNodes
180     inpMatrix     = M.fromLists $ map (\xs -> map (name xs,) (timeStates xs))
    ↪ inpNodes
181
182     -- Get boolean expression combos
183     ruleCombos    = map (getBDDFromFunc inpNodeNames) $ getConjDisjCombos (length
    ↪ inpNodes - 1)
184
185     -- Predict states using boolean expression
186     predStates    = map (\ruleBDD ->
187     ↪ let p = map (fromEnum . \t -> evaluateFunc ruleBDD
    ↪ (filter (\(nn, _) -> nn `elem` inpNodeNames)
188     ↪ $ Vec.toList (M.getCol t
    ↪ inpMatrix)))
189     ↪ [1..(timeLength - 1)]
190     ↪ in (p, ruleBDD))
191     ↪ ruleCombos
192
193 searchUpdateRulePar :: [NodeState] -> NodeState -> Int -> [(Double, BDD)]
194 searchUpdateRulePar inpNodes targetNode timeLength =
195     case allTargetStates of
196     []           -> error "Invalid target states."
197     [_]         -> error "Invalid target states."
198     (_:targetStates) -> map (\(p, r) -> (geneWiseDynamicsConsistency p
    ↪ targetStates, r)) predStates
199     where
200     -- Get target states of target node

```

```

201     allTargetStates = timeStates targetNode
202
203     inpNodeNames     = map name inpNodes
204     inpMatrix        = M.fromLists $ map (\xs -> map (name xs,) (timeStates xs)
↳ `using` parBuffer 50 rdeepseq) inpNodes
205
206     -- Get boolean expression combos
207     ruleCombos       = map (getBDDFromFunc inpNodeNames) (getConjDisjCombos
↳ (length inpNodes)) `using` parBuffer 100 rdeepseq
208
209     -- Predict states using boolean expression
210     predStates       = parMap rdeepseq (\ruleBDD ->
211                               let p = map (fromEnum . \t -> evaluateFunc ruleBDD
↳ (filter (\(nn, _) -> nn `elem` inpNodeNames)
212                               $ Vec.toList (M.getCol t inpMatrix)))
213                               [1..(timeLength - 1)]
214                               `using` parBuffer 50 rdeepseq
215                               in (p, ruleBDD))
216                               ruleCombos
217
218     {-
219     Get optimal boolean expressions for each node in network that optimizes genewise
↳ dynamics consistency.
220     -}
221     getOptimalBoolExpressions :: BoolNetwork -> Int -> [(NodeState, BDD, Double)]
222     getOptimalBoolExpressions inferredNetwork timeLength = map (\targetNode ->
223                               let inpNodes
↳ = getRegulatoryNodes targetNode inferredNetwork
224                               -- Get
↳ consistency metrics for each boolean expression
225
↳ consistencyMetrics          = searchUpdateRule inpNodes targetNode
↳ timeLength
226                               -- Get boolean
↳ expression with max consistency metric
227                               (maxConsistency,
↳ optimalBDD) = maximumBy (comparing fst) consistencyMetrics
228                               in (targetNode,
↳ optimalBDD, maxConsistency))
229                               $ nodes inferredNetwork
230
231     getOptimalBoolExpressionsPar :: BoolNetwork -> Int -> [(NodeState, BDD, Double)]
232     getOptimalBoolExpressionsPar inferredNetwork k = map (\targetNode ->
233                               let inpNodes
↳ = getRegulatoryNodes targetNode inferredNetwork
234                               consistencyMetrics
↳ = searchUpdateRulePar inpNodes targetNode k

```

```

235                                     (maxConsistency,
↳ optimalBDD) = maximumBy (comparing fst) consistencyMetrics
236                                     in (targetNode,
↳ optimalBDD, maxConsistency))
237                                     (nodes inferredNetwork)
238                                     `using` parListChunk 50 rdeepseq

```

## 8.5 src/ProcessData.hs

```

1  module ProcessData
2    ( csvToNodeStates
3    ) where
4
5  import qualified Data.ByteString.Char8 as C
6
7  import GraphUtils (NodeState(..))
8  import qualified Data.Matrix as M
9  import qualified Data.Vector as Vec
10
11
12  -- Get CSV Data
13  -- Return (header, values as multi-D list)
14  getCSVData :: String -> IO ([String], [[Int]])
15  getCSVData fname = do
16      inp <- C.readFile fname
17      let inpLines = C.lines inp
18          case inpLines of
19              []          -> error "Invalid csv file."
20              [_]         -> error "Invalid csv file."
21              (header:csvLines) -> do
22                  let headerFormatted = map C.unpack (C.split ',' header)
23                      csvLinesFormatted = map (map (\l2 -> read (C.unpack l2) :: Int)) .
↳ C.split ',' csvLines
24                      return (headerFormatted, csvLinesFormatted)
25
26  {-
27  Params:
28      - x: csvData returned by getCSVData
29      - axis: 0 = row, 1 = column
30  -}
31  parseCSVData :: IO ([String], [[Int]]) -> Int -> IO [NodeState]
32  parseCSVData x axis = do
33      csvData <- x
34      let (header, csvList) = csvData
35          csvMatrix         = M.fromLists csvList
36          nodeStates        = foldl (\acc (i, hName) -> acc ++ [NodeState hName]
↳ (Vec.toList $

```

```

37                                     if axis == 0
38                                         then M.getRow i
39                                     else M.getCol i
↪ csvMatrix
39                                     else M.getCol i
↪ csvMatrix
40                                     )))
41                                     []
42                                     $ filter (\(_, n) -> n /= "time") (zip [0..]
↪ header)
43
44     return nodeStates
45
46 {-
47 Params:
48     - fname: csv filename
49     - axis: 0 = row, 1 = column
50
51 Example:
52 t <- csvToNodeStates ".././test2.csv" 1
53 -}
54 csvToNodeStates :: String -> Int -> IO [NodeState]
55 csvToNodeStates fname = parseCSVData (getCSVData fname)

```

## 8.6 src/generate\_data.py

```

1 # Generate large test samples
2 """
3 Main script for generating random large datasets of input/output gene expression
↪ samples
4 """
5
6 import random
7 import pandas as pd
8 import numpy as np
9 import argparse
10
11 def generate_io_pairs(num_nodes, time):
12     nodes = ["v" + str(i) for i in range(1, num_nodes + 1)] + ["v" + str(i) + ""
↪ for i in range(1, num_nodes + 1)]
13     state_series = []
14
15     inp_seen = []
16     out_seen = []
17
18     for t in range(1, time + 1):
19         rand_states_inp = [random.randint(0, 1) for _ in range(num_nodes)]
20         rand_states_out = [random.randint(0, 1) for _ in range(num_nodes)]

```

```

21
22     inp_done = False
23     out_done = False
24
25     while not (inp_done and out_done):
26         if rand_states_inp not in inp_seen:
27             inp_seen.append(rand_states_inp)
28             inp_done = True
29         else:
30             rand_states_inp = [random.randint(0, 1) for _ in
31                               ↪ range(num_nodes)]
32
33         if rand_states_out not in out_seen:
34             out_seen.append(rand_states_out)
35             out_done = True
36         else:
37             rand_states_out = [random.randint(0, 1) for _ in
38                               ↪ range(num_nodes)]
39
40     state_series.append(rand_states_inp + rand_states_out)
41
42     state_series_df = pd.DataFrame(state_series, columns = nodes)
43     return state_series_df
44
45 def generate_data_time_series(num_nodes, time):
46     nodes = ["v" + str(i) for i in range(1, num_nodes + 1)]
47     state_series = []
48     states_seen = []
49     for t in range(1, time + 1):
50         rand_states = [random.randint(0, 1) for _ in range(len(nodes))]
51         while True:
52             if rand_states not in states_seen:
53                 states_seen.append(rand_states)
54                 break
55             else:
56                 rand_states = [random.randint(0, 1) for _ in range(len(nodes))]
57
58         state_series.append([t] + rand_states)
59
60     state_series_df = pd.DataFrame(state_series, columns = ["time"] + nodes)
61     return state_series_df
62
63 def output_data_to_file(state_series_df, fname):
64     state_series_df.to_csv(fname, index=False)
65     print("Printed data to {}".format(fname))

```

```

66 def parse_args():
67     parser = argparse.ArgumentParser()
68
69     parser.add_argument("--numNodes", type=int, help="Number of nodes")
70     parser.add_argument("--time", type=int, help="Length of time-series")
71     parser.add_argument("--outputFile", help="Output file")
72
73     args = parser.parse_args()
74
75     return args
76
77 # Example: python generate_data.py --numNodes 100 --time 300 --outputFile
78 ↪ "test.csv"
79 if __name__ == "__main__":
80     args = parse_args()
81     data = generate_data_time_series(args.numNodes, args.time)
82     print(data)
83     output_data_to_file(data, args.outputFile)

```