LANGUAGE FOR LINEAR ALGEBRA

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# Contents

1 Introduction .......................... 2
  1.1 Background .............................. 2
  1.2 Features ................................. 2
  1.3 Related Work ............................. 3

2 Tutorial ................................ 3
  2.1 Compile the program ...................... 3
  2.2 Write the program ........................ 4
    2.2.1 Date types ............................ 4
    2.2.2 Control flows ......................... 4
    2.2.3 Define functions ...................... 5
    2.2.4 Built-in functions .................... 5
    2.2.5 Combine together ..................... 5

3 Language Reference Manual .............. 7
  3.1 Introduction ............................ 7
  3.2 Lexical conventions ...................... 7
    3.2.1 Identifiers ........................... 7
    3.2.2 Keywords .............................. 7
    3.2.3 Constants ............................. 8
    3.2.4 Comments .............................. 8
    3.2.5 Data Type ............................. 8
  3.3 Operators ............................... 11
    3.3.1 Unary operators ....................... 11
    3.3.2 Logical operators ..................... 12
    3.3.3 Assignment operator: = ............... 12
    3.3.4 Arithmetic operators .................. 12
    3.3.5 Comparison operators ................. 14
    3.3.6 Linear algebra domain operators ....... 15
    3.3.7 Precedence and Associativity .......... 16
  3.4 Syntax .................................. 16
    3.4.1 Program structure ..................... 16
4 Project Plan
4.1 Specification Process ........................................ 25
4.2 Development Process ........................................ 26
4.3 Testing Process ............................................... 26
4.4 Team Responsibilities ...................................... 26
4.5 Project Timeline ............................................. 26
4.6 Project Log .................................................. 27
4.7 Development Environment ................................. 27
4.8 Programming Guide ........................................ 28

5 Architectural Design ........................................... 28
5.1 Compiler Architecture ...................................... 28
  5.1.1 Scanner (Guitang, Chenzhe, Liang) .................. 29
  5.1.2 Parser (Zhiyuan, Guitang) ............................ 29
  5.1.3 Type Checker (Zhiyuan, Chenzhe) ................. 29
  5.1.4 Code Generator (Zhiyuan, Guitang, Liang) ...... 29
5.2 Python Library ............................................ 29
  5.2.1 Basic Classes (Chenzhe, Guitang) .................. 29
  5.2.2 Builtin Functions (ChenZhe, Guitang) .......... 29

6 Test Plan ..................................................... 30
6.1 Source to Target .......................................... 30
6.2 Test Suites ............................................... 33
  6.2.1 Testing Cases ........................................ 34
  6.2.2 Automation Testing .................................. 34
  6.2.3 Test Roles ........................................... 34

7 Lessons Learned ............................................... 34
7.1 Chenzhe Qian .............................................. 34
7.2 Guitian Lan ............................................... 35
7.3 Jin Liang .................................................. 35
7.4 Zhiyuan Guo .............................................. 35
1 Introduction

The Language for Linear Algebra (LFLA) is a multi-paradigm and domain-specific programming language. It is focused on linear algebra programming and mainly designed for educational purpose. This language will help linear algebra learner to have a clear understanding of linear algebra concepts and terminologies, and use the language for computation. The input language of LFLA syntactically resembles the Matlab programming language. The output of the translator is Python code with a built-in library, compiles to an executable python script. LFLA inherits the benefits of functional programming language and powered by object-like primitive types (see Features). LFLA makes linear algebra calculation easy to code, read and understand. Besides, LFLA’s syntax resembles common imperative languages so that makes programmers be comfortable to build complex programs.

1.1 Background

Linear algebra programming, though can be done by many existed languages such Matlab, R, Maple and etc, is still confusing on the concept-level. For example, none of the modern suitable languages clearly separates the concept of vector and matrix. Learners, even experienced programmers, may consider a matrix consists of vector(s). Such misunderstanding may not affect too much on industrial-orientated environment but will significantly mislead students to catch its essence.

We believe that computer science should play a crucial role in math education especially helping students to learn tough subjects like linear algebra. A good linear algebra programming language should not only do computing, but also help the students comprehend the fundamentals and the beauty of the linear algebra. Given this situation, we would like to create a domain language to help students and teachers in learning and teaching linear algebra. The Language for Linear Algebra(LFLA) is mainly designed for educational purpose.

1.2 Features

LFLA introduces several primitive types direct corresponding to the concepts in linear algebra. Except as the matrix, it has vector, vector space, affine spaces and inner product space as primitive types. Besides the basic matrix calculation, LFLA emphasizes the relation between vector space, vectors and matrix (considered as a
map). LFLA also incorporates the formal math notations into its language syntax to be consistent with math language.

1.3 Related Work

As mentioned in above, many modern programming languages support linear algebra programming. Matlab is known for its easiness to represent matrix and python is good for logical design and function building. LFLA mixes the syntax of Matlab and Python and is uniquely designed on the concepts of linear algebra. The built-in library that performs complicated calculations is implemented in Python.

2 Tutorial

2.1 Compile the program

Our compiler is named LFLA, which stands for language for linear algebra. So for the program file name, it should have postfix .la, as a indication of LFLA language. Here is a sample program.

```plaintext
# filename: sample.la
function main()
{
    print(1);
}
```

In sample.la, we only have one main function, which is the execution start of the program. In main function, it calls a built-in function print.

To compile sample.la file, specify the input file and output file to the compiler:

```
> ./LFLA sample.la -o sample
```

If you don’t specify output file name, compiler will generate an a.out file:

```
> ./LFLA sample.la
```

Then execute the output file and get the results:

```
> ./sample
1
```
2.2 Write the program

2.2.1 Date types

LFLA has 6 primitive data types, which are:

\[\text{var vector matrix vecspace inspace affspace}\]

It also supports the array data structures for each type. For array declaration, it should specify the length of array explicitly.

```c
# types.la
function main()
{
    var a = 1;
    vector b = [1,2,3];
    vector c[2] = {{1,0}, [0,1]};
    matrix d = [1,2;3,4];
    vecspace e = L([1,2], [4,5]);
    inspace f = inspace({[1,0],[0,1]}, c);
    affspace g = affspace(b,d);
    print(a);
    print(b);
    print(c);
    print(d);
}
```

Compile the program and execute:

```
> ./LFLA types.la
> ./a.out
1
[1 2 3]
[array([1, 2]), array([3, 4])]
[[1 2]
[3 4]]
```

2.2.2 Control flows

LFLA supports 3 common control flows, which are if, while and for. The syntax for each one is as follows:
# if statements
if expression { }

# while statements
while expression { }

# for loop
var a;
for a = n1:n2 { }

## 2.2.3 Define functions
To define a function in LFLA, it should start with a reserved word function, then follows the name of function. And every program should have a main function, which is the execute start of the program.

```lfla
# function .la
function foo ( var a) {
    print(a);
}

function main () {
    foo(10);
}
```

Compile and execute:

```
> ./ LFLA function .la
> ./a. out
10
```

## 2.2.4 Built-in functions
To help programmer better use this language, LFLA provide several built-in functions. Here is a list of built-in functions:

```
ceil floor sqrt dim size basis rank trace eigenValue
```

## 2.2.5 Combine together
Combine all these together, we can acheive some wonderful work using LFLA. Here is a sample code checking the linear independence of an array of vectors.
# sample1.la

function linearIndep(vector[] vectors, var n) {
    if n==1 { return 1; }
    if n > dim(vectors[0])
    { return 0; }

    vecspace vs;
    var i;
    for i = 0:n
    {
        if vectors[i]@vs
            {return 0;}
        vs = vs + L(vectors[i]);
    }

    return 1;
}

function main()
{
    vector v = [1,2,3];
    vector u = [2,22,3];
    vector w = v + u;
    vector x[2] = { v, u};
    vector y[3] = {v, u, w};

    print(linearIndep(x, 2));

    print(linearIndep(y, 3));
}

Compile and execute:

> ./LFLA sample1.la
> ./a.out

8
3 Language Reference Manual

3.1 Introduction

This manual describes LFLA, a imperative programming language. LFLA is designed to simulate the theory. Features defining the language include various primitive types and operations corresponding to important concepts and theory of linear algebra. This manual describes in detail the lexical conventions, types, operations, built-in functions, and grammar of the LFLA language.

3.2 Lexical conventions

3.2.1 Identifiers

An identifier in LFLA represents a name for functions or variables. The identifier starts with a letter, and is optionally followed by letters, digits or underscores. An identifier name is thus defined by the following regular expression:

\[ ['a' - 'z' 'A' -'Z' ] ['a' - 'z' 'A' - 'Z' '0' - '9' '_']^* \]

3.2.2 Keywords

LFLA has a set of reserved keywords that can not be used as identifiers.

3.2.2.1 Types

Each primitive type, var, vector, vecspace, inspace, affspace and matrix, has a name that the program uses for declarations:

\texttt{var vector vecspace inspace affspace matrix}

3.2.2.2 Function

The keyword for declaration of function:

\texttt{function}

3.2.2.3 Entry point of the program

The keyword for indication of entry function:

\texttt{main}
3.2.2.4 Control flow
The following keywords are used for control flow:
if else for while break continue return

3.2.2.5 Built-in functions
The following keywords are reserved for built in functions:
print dim basis sqrt ceil floor size rank trace eigenValue solve image L

3.2.3 Constants
LFLA supports integer, double as well as vector, matrix constants.

3.2.3.1 Integer
In LFLA an integer is a signed 31-bit integer without decimal point or exponent.
It is given by the following regular expression:
[+ - ]\[ '0' - '9 ' \]+

3.2.3.2 Double
In LFLA a double is a 64-bit floating point number. More precisely it has an integral part, a fraction part and an exponent part. The integral part can begin with an optional '+', then follows by digits. And if it is not zero, the first digit should not be '0'. The fraction part is just a decimal followed by a finite sequence of digits. The exponent part begins with 'e' or 'E', then followed by an optional '+' or '-', then sequence of digits which has non-'0' first digit. Having the fraction part, the integral part and exponent part can be missing. If both the fraction part and exponent part are missing, then an extra decimal point should be added in the end of the integral part.

3.2.4 Comments
Line Comments: #
Block Comments: ### ... ###

3.2.5 Data Type
In LFLA, there are four primitive data types: var, vector, matrix, vecspace, inspace and affspace.

3.2.5.1 Var
The primitive type var is a hybrid of integer and float point number.
3.2.5.2 Vector
The type vector directly corresponds to the concept of vector in linear algebra. Formally it is a finite sequence of var separated by commas and included by brackets .The length is its dimension.

```
vector a = [1,2,3];
```

3.2.5.3 Matrix
The type matrix directly corresponds to the concept of matrix in linear algebra. It is given by several rows of var which are separated by semicolons and have the same length. Each row is consisted of a finite sequence of var separated by commas:

```
vector a = [1,2,3;4,5,6;7,8,9;];
```

3.2.5.4 Vector space
The type vecspace directly corresponds to the concept of vector space in linear algebra. Down to earth, it can be represented by a basis which is a maximal set of linear independent vectors in the vector space. In other word, it is linear spanned by a basis. Its dimension equals to the number of vectors in a basis. The built-in L function is used as the constructor :

```
vector a = [1,2,3];
vector b = [2,0,0];
vecspace vs = L(a,b);
```

3.2.5.5 Inner product space
The type inspace directly corresponds to the concept of inner product space in linear algebra. It is a pair (v, <, >), where v is vector space , and <, > is an inner product. An inner product is a map $V \times V \to \mathbb{R}$ satisfy the following properties:

\[
< x, y > = < y, x > \\
< x, x > \geq 0, \text{ it is iff } x = 0 \\
< ax_1 + by_1, cx_2 + dy_2 > = ac < x_1, x_2 > + ad < x_1, y_2 > + bc < y_1, x_2 > + bd < y_1, y_2 >
\]

for $a, b, c, d \in \mathbb{R}$ and $x_1, x_2, y_1, y_2 \in V$. 

11
But down to earth, it is given a by the Gram matrix with respect to some basis. So in LFLA, an `inspace` object is defined by an array of vectors which serves as a basis and a positive definite matrix which serves as Gram matrix. The `inspace` function is used as the constructor:

```plaintext
vector v1 = [1,0,0];
vector v2 = [0,1,0];
vector v3 = [0,0,1];

matrix mat = [1,0,0;0,1,0;0,0,1;];
vector vecs[3] = {v1, v2, v3};
inspace ins = inspace(vecs, mat);
```

### 3.2.5.6 Affine space

The type `affspace` directly corresponds to the concept of affine space in linear algebra. It is a pair `(w, V)`, where `w` is a vector, and `V` is a vector space. The dimension of `w` should equal to the dimension of any vector in `V`. The `affspace` function is used as the constructor:

```plaintext
vector v1 = [1,1,1];
vector v2 = [1,2,3];
vector v3 = [2,3,4];
vecspace vs = L(v2);
affspace aff = affspace(v1,vs);
```

### 3.2.5.7 Array

For any above type, there is a form in which contains multiple instances of the same type, known as array. By an array of type `X`, we means a sequence of object of type `X`. Array is length fixed which means that once it is initialized, its length is immutable. In LFLA array is given by comma separated object sequence in braces.

```plaintext
vector v1 = [1,0,0];
vector v2 = [0,1,0];
vector v3 = [0,0,1];
vector vecs[3] = {v1, v2, v3};
```
To access elements of an array, we use the identifier follows by a bracket included index, for example:

```plaintext
vecs[3]
```

The index of array starts with 0 instead of 1, so the index should be less than the length of the array.

### 3.3 Operators

LFLA contains all operators in common languages like Java and C++, except for bit manipulation operators. However, there are subtle differences between scalar-scalar, scalar-object and object-object operations and object-object operations. We will introduce these operators one by one. And in the last part of this section, we will conclude the precedence and associativity of these operators.

#### 3.3.1 Unary operators

**3.3.1.1 Negative operator ‘-’**

```plaintext
var a = 1;
var b = -a;
```

Return the negative of the expression and have the same type. The type of the expression must be `var`, `vector`, `matrix`.

**3.3.1.2 Increment operator ‘++’ and decrement operator ‘--’**

The value of the expression is incremented by 1 or decremented by 1, and return the new value. Here the type of expression could only be `var` type.

```plaintext
var a = 1;
a++;
a--;
```

**3.3.1.3 Matrix transpose operator ‘’**

This is the transpose operator. Return the transpose of a matrix denoted by the expression, which could only be `matrix` type.

```plaintext
matrix a = [1,2,3; 3,4,5];
matrix b = a';
```
3.3.2 Logical operators

3.3.2.1 AND operator : &&
This is the logical operator AND. It is a binary operator. The result has value 1 if and only if both expr1 and expr2 are non zero. Otherwise the result has value 0; It is used in the following form:

\[ \text{expr1} \&\& \text{expr2} \]

In this structure, expr1 will be executed first. Only if expr1 has nonzero value, expr2 will be executed.

3.3.2.2 OR operator : ||
The is the logical operator OR. It is a binary operator. The result has value 1 if and only if either expr1 or expr2 is non zero. Otherwise the result has value 0; It is used in the following form:

\[ \text{expr1} || \text{expr2} \]

In this structure, expr1 will be executed first. Only if expr1 has zero value, expr2 will be executed.

3.3.3 Assignment operator: =
It is a binary operator. It is used in the following form :

\[ \text{id} = \text{expr} \]

In this structure, 'id' should be an identifier for a variable, and 'expr' should be an expression of exactly the same type as the variable. The 'expr' will be executed first, then its value will be stored into the variable represented by the 'id'. LFLA does not support implicit type cast.

3.3.4 Arithmetic operators

3.3.4.1 Addition: +
It is an binary operator applied to expression of type var , vector, matrix and vecspace. It is used in the following form:

\[ \text{expr1} + \text{expr2} \]

For var type expression, it adds values of two expressions and return the new value. For vector type, both operands should have the same dimension. It will
add the elements in correspond position from two operand, and return a vector of
the same dimension. For matrix type, both operands should have the same sizes.
It will add the elements in correspond position from two operand, and return a
vector of the same size. For vecspace type, both space should be subspaces of
some $\mathbb{R}^n$, i.e. their vectors should have the same dimension. It will return the
vecspace corresponding to the sum of the two vector space in linear algebra.

3.3.4.2 Dot addition: +.
It is an binary operator applied to expression of type var with vector or matrix.
It adds a var value to every elements in vector or matrix. And return the new
vector or matrix. It is used in the following form:

\[
\text{expr1} +. \text{expr2}
\]

'expr1' should be an expression of type var while 'expr2' should be an expresssion
of type vector or matrix.

3.3.4.3 Substraction: -
It is an binary operator applied to expression of type var, vector and matrix.
Return the difference of values of two expression. It works analogously to the '+'
operator. It is used in the following form:

\[
\text{expr1} - \text{expr2}
\]

For vector type or matrix type, both operands should have the same dimension
or size.

3.3.4.4 Dot substraction: -.
It is an binary operator applied to expression of type var with vector or matrix.
It works analogously to the '+.' operator. It is used in the following form:

\[
\text{expr1} -. \text{expr2}
\]

'expr1' should be an expression of type var while 'expr2' should be an expresssion
of type vector or matrix.

3.3.4.5 multiplication: *
It is an binary operator applied to expression of type var and matrix. It is used
in the following form:

\[
\text{expr1} * \text{expr2}
\]
For \texttt{var} type expression, it is just the ordinary multiplication. For \texttt{matrix} type, it is the matrix multiplication. So it requires that the column number of \texttt{expr1} should be coincide with the row number of \texttt{expr2}.

3.3.4.6 Dot multiplication: \texttt{*}. 
It is an binary operator applied to expression of type \texttt{var} with \texttt{vector} or \texttt{matrix} or type \texttt{matrix} with \texttt{matrix}. If the left operand is a \texttt{var}, then it will multiply a \texttt{var} value to every elements in \texttt{vector} or \texttt{matrix}. If both the operands are \texttt{matrix}, then it requires that the two operands should have the same size. It will return a new matrix by multiplying the corresponding elements of the two matrices. It is used in the following form:

\texttt{expr1 \,*\, expr2}

If \texttt{expr1} is an expression of type \texttt{var}, then \texttt{expr2} could be an expression of type \texttt{vector} or \texttt{matrix}. If \texttt{expr1} is of type \texttt{matrix}, then \texttt{expr2} should be of type \texttt{matrix}.

3.3.4.7 Division: \texttt{/} 
It is an binary operator only applied to expression of type \texttt{var}. If the two operands are integers, it will perform integer division and return an integer value \texttt{var}. If any operand is double numbers, it will perform float point division and return a double value \texttt{var}. It is used in the following form:

\texttt{expr1 \,/, \, expr2}

In any case \texttt{expr2} should not be zero.

3.3.4.8 Dot division: \texttt{/}. 
It is an binary operator applied to expression of type \texttt{var} with \texttt{vector} or \texttt{matrix}. It works analogously to the \texttt{*}. operator. It is used in the following form:

\texttt{expr1 \,/, \, expr2}

3.3.5 Comparation operators 
There are six types of comparation operators: \texttt{<}, \texttt{>}, \texttt{<=}, \texttt{>=}, \texttt{!} = and \texttt{==}. All these comparison operators are only applied to expression of type \texttt{var}. It returns 0 if it is not true and otherwise 1. They are used in the following form:
3.3.6 Linear algebra domain operators

3.3.6.1 Belongs: @
It is an binary operator applied to expression of type vector with vecspace or affspace. It is used in the following form:

```plaintext
expr1 @ expr2
```

'expr1' should be vector type expression while 'expr2' a vecspace or affspace type expression. It return 1 if the vector (left operand) belongs to the vector space or affine space (right operand). Otherwise return 0.

3.3.6.2 LieBracket: [[·, ·]]
It is an binary operator applied to expression of type matrix. It is used in the following form:

```plaintext
[[ expr1 , expr2 ]]
```

Both operands should be square matrices and have the same size. It returns the value: expr1 *expr2 - expr2*expr1.

3.3.6.3 Inner product: <<·, ·>>
It is used in the following form:

```plaintext
id <<expr1 , expr2 >>
```

'id' should be an identifier for an inspace type variable while 'expr1' and 'expr2' are expression of vector type. The dimension of the two textbfvector should be the same as the dimension of the inspace. It returns a var type value: the inner product of the two vectors, where the inner product is defined by the inspace object.
3.3.6.4 Matrix action: &
It is an binary operator applied to expression of type matrix with vector. It is used in the following form:

\[ \text{expr1} \& \ \text{expr2} \]

'expr1' is matrix type while 'expr2' vector type. It corresponds to the concept of matrix action on vector in linear algebra. The column number of the matrix should be the same as the dimension of the vector. It will return vector type.

3.3.7 Precedence and Associativity

<table>
<thead>
<tr>
<th>Operators</th>
<th>Associativity</th>
<th>Precedence</th>
</tr>
</thead>
<tbody>
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<td>non associativity</td>
<td>Highest 7</td>
</tr>
<tr>
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<td>non associativity</td>
<td>6</td>
</tr>
<tr>
<td>′, @</td>
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</tr>
<tr>
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<td></td>
<td></td>
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<tr>
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<td>left to right</td>
<td>2</td>
</tr>
<tr>
<td>&lt;, &gt;, &lt;=, &gt;=, !=, ==</td>
<td>left to right</td>
<td>1</td>
</tr>
<tr>
<td>=</td>
<td>right to left</td>
<td>Lowest 0</td>
</tr>
</tbody>
</table>

3.4 Syntax

3.4.1 Program structure

3.4.2 Declarations

3.4.2.1 Variable Declarations
All variables must be declared with its data type before used. The initial value is optional. If there is one, it must be an expression resulting in the same type with variable. The grammar for primary type variable declarator is following:

`primary_date_type identifier`

Data type can be any primary type: var, vector, vecspace, matrix, inspace, affspace. To declare a variable, the data type cannot be missed, and it must follows by a valid identifier. If declaring a variable with initial value, the type of value must matches the type of variable that assigned to.
Variable of **array** type have a special syntax. The grammar for array type variable declarator is following:

```
primary_date_type identifier [ expr ]
```

'expr' should be an nonnegative value integral **var**. It is used to designate the length of the array.

The following are some examples of variable declaration and initialization.

```
var v;
var v1 = 5;  # Integer value
var v2 = 5.1; # double number value

vector vec;
vector vec1 = [1, 2, 4.2, 5, 1.0];
vector vec2 = [v, v1, v2];

matrix mat;
matrix mat1 = [1, 2.0; 3, 4];
matrix mat2 = [v1, v2; v, v1, v2; v, v1, v2];
### Following is NOT allowed,
   because matrix cannot interchange with vector
matrix mat3 = [vec1; vec1];
###

vecspace vecsp;
vecspace vecsp0 = L()  # an zero vector space
vecspace vecsp1 = L(vec1, vec2);
vector vectors[2] = {vec1, vec2};
vecspace vecsp2 = L(vectors);

var vars1[5];
var n = 3;
var vars2[n];
vars = {1.0, 2, 3.4};
var vars3[n] = {1.0, 2, 3.4};
```
var vars4[n] = {v1, 0.2, 1, v2};

vector vecs[2] = {[1,2], [1,1]};
matrix mat = [1,2;2,8];
inspace insp;
inspace insp1 = inspace(vecs, mat);

affspace afsp;
vecspace vecsp3 = L(vec1, vec1, vec1);
affspace afsp1 = affspace(vec1, vecsp3);

vector vecs1[n];
matrix mats[n];
inspace insps[n];
affspace afsps[n];

3.4.2.2 Function Declarations
A function has header and body. The function header contains function name, parameter list if any and NO need for return type. However, to declare a function it must start from keyword function. The name of function and names of parameters must be valid identifiers. The function body is enclosed in braces and must follow rules of statements.

The grammar for function declarator is following:

function identifier (optional parameter-list)
{ function body}

The optional parameter-list can be empty or the following form:

Date_type id, Date_type id,..., Data_type id

A simple example of a complete function definition is

function plus(var v1, var v2)
{
    v2 = v1 + v2;
    return v2;
}
3.4.3 Statements

Statements are executed in sequence.

3.4.3.1 Expression statement

The form of expression:

```plaintext
expression;
```

Most statements are expression statements. Usually expression statements are
assignments, operator with expressions and function calls.

3.4.3.2 Assignment statements

An assignment statement takes the following form:

```plaintext
id = expression;
```

The `id` should be an identifier for a variable which had been declared before.
The expression should have the same type as the variable. This statement first
evaluate the `expression` then store it to the `id` variable.

3.4.3.3 Block statements

The form of block:

```plaintext
{statements}
```

A block encloses a series of statements by braces.

3.4.3.4 Conditional statement

Three forms of the conditional statement:

```plaintext
if expression1 { statements1 }
```

```plaintext
if expression1 { statements1 }
else { statements2 }
```

```plaintext
if expression1 { statements1 }
else if expression2 { statements2 }
else { statements3 }
```

In all cases the `expression1` is evaluated. If it is non-zero, the `substatements1` is
executed. In the second case, the `statements2` is executed only if the `expression1`
is 0. In the third case, the 'statements2' is executed only if the 'expression1' is 0 and
the 'expression2' is non-zero. In the third case, the 'statements3' is executed only if both the 'expression1' and 'expression2' are 0. As usual the 'else' ambiguity is resolved by connecting an else with the last encountered elseless if. Sample code:

```javascript
var v1 = 5;
var v2 = 6;
if v1 < v2
{
    return v1;
}
else if v1 == v2
{
    return v1+v2;
}
else
{
    return v2;
}
```

### 3.4.3.5 While statement

The form of while statement:

```javascript
while expression { statements }
```

The 'statements' is executed repeatedly as long as the value of the 'expression' remains non-zero. The test takes place before each execution of the 'statement'. Sample code:

```javascript
while 1
{
    print "hello world";
}
```

### 3.4.3.6 For statement

The form of for statement:

```javascript
for specialexpression { statements }
```
The special expression specifies the condition of the loop including initialization, test, and iteration step. It has two form:

```
var id = constant1 : constant2
```

'id' is an identifier while 'constant1' and 'constant2' are var type constant. It means the var variable 'id' starts with 'constant1' and increase value 1 for each iteration of the for loop untill larger than 'constant2'. or

```
var id = constant1 : constant2 : constant3
```

'id' is an identifier while 'constant1', 'constant2' and 'constant3' are var type constant. It means the var variable 'id' starts with 'constant1' and increase value 'constant2' for each iteration of the for loop untill larger than 'constant3'.

Sample code:

```java
for var i = 1:5
{
    print(i);
}
```

### 3.4.3.7 Break statement

The form of break statement:

```
break;
```

This statement causes termination of the enclosing while and for statement. It controls to pass the statement following the terminated statement. Sample code:

```java
for var i = 1:5
{
    if i == 2
    {
        break;
    }
}
```

### 3.4.3.8 Continue statement

The form of continue statement:
continue;

This statement causes control to pass to the loop-continuation portion of the enclosing while and for statement. In other words, this leads to the end of the loop. Sample code:

```plaintext
for var i = 1:5
{
  if i == 2
  {
    continue;
  }
}
```

### 3.4.3.9 Return statement

The form of return statement:

```plaintext
return expression;
```

The value of the expression is returned to the caller of the function.

```plaintext
function foo()
{
  return 0;
}
```

### 3.4.3.10 Empty statement

The form of empty statement:

```plaintext
;
```

### 3.4.3.11 Built-in Functions

In LFLA language, several built-in functions are provided.

- `sqrt(var x)` : Returns the positive square root of a var value. Sample code:

```plaintext
var x = 9;
var result = sqrt(x);
# result = 3.0
```
• `ceil(var x)` : Returns the smallest integer value that is greater than or equal to the argument. Sample code:

```
var x = 8.8
var result = ceil(x);
# result = 9
```

• `floor(var x)` : Returns the largest integer value that is less than or equal to the argument. Sample code:

```
var x = 8.8;
var result = floor(x);
# result = 8
```

• `dim(vector v)` : Returns the dimension of a vector. Sample code:

```
vector v = [1, 2, 3];
var result = dim(v);
# result = 3
```

• `dim(vecspace vs)` : Returns the dimension of a vector space. Sample code:

```
vector w = [2,1,1];
vector u = [1,0,0];
vecspace vs = L(w,u);
var result = dim(vs);
# result = 2
```

• `dim(affspace affs)` : Returns the dimension of an affine vector space. Sample code:

```
vector w = [2,1,1];
vector u = [1,0,0];
vector t = [0,0,1];
vecspace vs = L(w,u);
affspace affs = affspace(t,vs);
var result = dim(affs);
# result = 2
```
• **dim(inspace ins)**: Returns the dimension of an inner product space. Sample code:

```plaintext
vector v1 = [1,0,0];
vector v2 = [0,1,0];
vector v3 = [0,0,1];
matrix mat = [1,0,0;0,1,0;0,0,1];
vector vecs[3] = {v1, v2, v3};
inspace ins = inspace(vecs, mat);
var result = dim(ins);
# result = 3
```

• **size(matrix m)**: Returns the size of a matrix. Return type is an array of type var of length two. Sample code:

```plaintext
matrix m = [1, 2; 3, 4];
result = size(m);
# result = [2, 2]
```

• **basis(vecspace vs)**: Return one basis of a vector space. Return type is an array of vector. Sample code:

```plaintext
vector v1 = [1, 0];
vector v2 = [0, 1];
vecspace vs = L(v1, v2);
var[] result = basis(vs);
# result = {[1, 0], [0, 1]}
```

• **rank(matrix m)**: Returns the rank of a matrix. Sample code:

```plaintext
matrix m = [1, 2, 3; 2, 4, 6];
var result = rank(m);
# result = 1
```

• **trace(matrix m)**: Returns the trace of a square matrix. Sample code:

```plaintext
matrix m = [1, 2, 3; 4, 5, 6; 7, 8, 9];
var result = trace(m);
# result = 15
```
• eigenValue(matrix m) : Returns the eigenvalues of a matrix. Return type is an array of var value. Sample code:

```java
matrix m = [3, 2, 4; 2, 0, 2; 4, 2, 3;];
var result[3] = eigenValue(m);
# result = [8, -1];
```

• image(matrix m) : Returns the image of a matrix. Return type is vecspace. Sample code:

```java
matrix m = [1, 2; 3, 4;];
vecspace result = image(m);
# result = L([1,3],[2,4])
```

• solve(matrix m, vector b) : Solve the linear equation given by the coefficient matrix m and target vector b, i.e. given $m \cdot x = b$, solve x. Its return type is affspace. Sample code:

```java
matrix m = [1,2;3,6;];
vector b = [3,9;]
affspace result = solveEquation(m,b);
# result = affspace([1,1] L([-2,1]));
```

4 Project Plan

Throughout the project we used incremental strategy coupled with iterative planning process. We split the whole project into four major components: scanner, parser, type checker and code generator. For each component, we performed iterative tactic to hit the goal. We assigned roles for each team member and hold weekly meeting. The target goals and actual achievements are outlined in the following sections. Thanks to Prof. Edwards for helping us set milestones.

4.1 Specification Process

In the very beginning, we discussed what domain our language should target to. We were conscientious of selecting the domain and prepared the proposal. Once the domain was set, we decided the lexical and syntax specifications, which we implemented in the lexer and parser and wrote the language reference manual.
We assigned tasks to team members based on the reference manual and our interests. However, as the language was developing, we changed specifications as the situation called for.

4.2 Development Process

Development is pretty straightforward as the compiler pipeline / architecture discussed in the lecture. We started from the lexer to the parser, then the semantics checker, and the code generator at last. As mentioned above, we used incremental strategy before the 'Hello World' milestone was archived. Then we added automation tests. Since then, we switched strategy to iterative process.

4.3 Testing Process

We had a few unit tests and integration test before the 'Hello word' milestone. After that, we worked on test-driven process. Each new test case would be tested right-away. If not pass, we work to fix the problem. Importantly, each test case was carefully created to test the basic of the language and the core functions of the language. Overall, the test cases include positive tests, negative tests, unit tests, integration tests and system tests.

4.4 Team Responsibilities

The team responsibilities were assigned to four members as described in the table below. However, there was no strict division of responsibilities as multiple members contributed to multiple parts, depending on the stage of the project.

<table>
<thead>
<tr>
<th>Member</th>
<th>Responsibility</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zhiyuan Guo</td>
<td>Compiler, Code generation, Semantics</td>
</tr>
<tr>
<td>Chenzhe Qian</td>
<td>Python libraries, Code generation, Documentation</td>
</tr>
<tr>
<td>Guitang Lan</td>
<td>Test case creation, Compiler, Semantic validation</td>
</tr>
<tr>
<td>Jin Liang</td>
<td>Test case creation, Testing automation, Documentation</td>
</tr>
</tbody>
</table>

4.5 Project Timeline

The target project timeline as shown in the below.
<table>
<thead>
<tr>
<th>Date</th>
<th>Milestone</th>
</tr>
</thead>
<tbody>
<tr>
<td>September 30</td>
<td>Language proposal</td>
</tr>
<tr>
<td>October 26</td>
<td>Language Reference Manual</td>
</tr>
<tr>
<td>November 6</td>
<td>Basic Scanner, Parser and AST complete</td>
</tr>
<tr>
<td>November 13</td>
<td>Code generation complete</td>
</tr>
<tr>
<td>November 16</td>
<td>&quot;Hello World&quot; complete and passed</td>
</tr>
<tr>
<td>November 27</td>
<td>Complete Python AST</td>
</tr>
<tr>
<td>December 18</td>
<td>Comprehensive functionality complete</td>
</tr>
<tr>
<td>December 21</td>
<td>Presentation and Demo</td>
</tr>
<tr>
<td>December 22</td>
<td>Final Report</td>
</tr>
</tbody>
</table>

4.6 Project Log

The actual achievement log as shown in the below

<table>
<thead>
<tr>
<th>Date</th>
<th>Milestone</th>
</tr>
</thead>
<tbody>
<tr>
<td>September 23</td>
<td>Draft proposal</td>
</tr>
<tr>
<td>September 30</td>
<td>Language proposal</td>
</tr>
<tr>
<td>October 20</td>
<td>Draft Language Reference Manual</td>
</tr>
<tr>
<td>October 26</td>
<td>Language Reference Manual</td>
</tr>
<tr>
<td>November 30</td>
<td>Basic Scanner and Parser complete</td>
</tr>
<tr>
<td>November 6</td>
<td>Basic AST Complete</td>
</tr>
<tr>
<td>November 13</td>
<td>Code generation complete</td>
</tr>
<tr>
<td>November 16</td>
<td>&quot;Hello World&quot; complete and passed</td>
</tr>
<tr>
<td>November 20</td>
<td>Automated test-case complete</td>
</tr>
<tr>
<td>December 4</td>
<td>Complete Python AST</td>
</tr>
<tr>
<td>December 11</td>
<td>Core functionality complete</td>
</tr>
<tr>
<td>December 18</td>
<td>Comprehensive functionality complete</td>
</tr>
<tr>
<td>December 20</td>
<td>Testing and debugging</td>
</tr>
<tr>
<td>December 21</td>
<td>Presentation and Demo</td>
</tr>
<tr>
<td>December 22</td>
<td>Final Report</td>
</tr>
</tbody>
</table>

4.7 Development Environment

Compiler language: Ocaml version 4.02.3
Compiling helping tool: Ocamlyacc, Ocamllex
Target environment: Python
4.8 Programming Guide

We generally followed the guidelines of Macro C that is provided by Prof. Edwards.

5 Architectural Design

5.1 Compiler Architecture

The architecture of LFLA compiler consists of four major parts: Scanner, Parser, Type Checker and Code Generator. And there are two main data structures AST(Abstract Syntax Tree) and Python AST. These parts are implemented in different ocaml code files. Scanner.mll is the scanner implemented using Ocamllex, where we provided basic identifiers regular expression. So after passing source file to scanner, we get tokens of the original program. Then Parser.mly implement the parser using Ocamlyacc by providing grammar rules. Then we get our ast. rranslate.ml and Translate_env.ml help translating the AST to Python AST. During the translation, Check.ml provide interfaces to do type checking. Finally Compile.ml translate the Python AST to python code to get final executable file.

Figure 1: Pipeline
5.1.1 Scanner (Guitang, Chenzhe, Liang)
Because LFLA doesn’t support string and char types. So Scanner.mll only needs to accept identifiers, literals, operators, reserved words, etc. Scanner.mll also throw exception when meeting syntax error and give out which line of code goes wrong.

5.1.2 Parser (Zhiyuan, Guitang)
Parser.mll takes in the tokens generated by Scanner and generate AST based on the grammar rules provided.

5.1.3 Type Checker (Zhiyuan, Chenzhe)
During translating AST to Python AST, program informations are all stored in translation environment, a data structure containing several symbol tables. When doing type checking, it first looks for type information of a expression from symbol tables, and do pattern matching based on our type restrictions.

5.1.4 Code Generator (Zhiyuan, Guitang, Liang)
Taking in python AST, compile.ml translate it into python code. One thing need to pay attention is the indentation in the python code.

5.2 Python Library
Python library is an important part for LFLA. It implements some basic mathematical classes and functionalities. It uses python numpy package as a main tool.

5.2.1 Basic Classes (Chenzhe, Guitang)
VecSpace.py, InSpace.py and AffSpace.py implements three major data types vector space, inner product space and affine space and their related functions. For VecSpace.py, it stores a list vectors internally as a basis in vector space. For InSpace, it owns a list of vectors and a matrix internally. For AffSpace, it has a vector and a vector space internally. They all provide simple interfaces that can be easily used when we generate python code.

5.2.2 Builtin Functions (ChenZhe, Guitang)
Core.py implements main builtin functions such as rank, trace, ceil, floor, etc, which are provided in LFLA.
6 Test Plan

6.1 Source to Target

Two representative source language programs are shown here, along with the corresponding target program for each.

Source Program 1:

```plaintext
function main()
{
    vector v1 = [1,2,3];
    vector v2 = [2,3,4];
    vector v3 = [3,5,7];
    vecspace vs1 = L(v1, v2);
    vecspace vs2 = L(v1, v2, v3);
    vecspace vs3 = L();
    vector vecs[3] = {v1,v2,v3};
    vecspace vs4 = L(vecs);
    print(basis(vs1));
    print(basis(vs2));
    print(basis(vs3));
    print(basis(vs4));
}
```

Target Program 1:

```python
#!/usr/bin/python
import sys
sys.path.append('./lib')
from InSpace import *
from AffSpace import *
from Core import *

def main():
```

32
v1=np.array([1,2,3])
v2=np.array([2,3,4])
v3=np.array([3,5,7])
vs1=VecSpace([v1,v2])
vs2=VecSpace([v1,v2,v3])
vs3=VecSpace([])
vecs=[v1,v2,v3]
vs4=VecSpace(vecs)
print(vs1.basis())
print(vs2.basis())
print(vs3.basis())
print(vs4.basis())
main()

Source Program 2:

function main()
{
    matrix a = [ 1,2;3,4;];
    matrix b = [1,1,1;1,1,1;];
    matrix c = a *b;
    print(c);
}

Target Program 2:

#!/usr/bin/python
import sys
sys.path.append('./lib')
from InSpace import *
from AffSpace import *
from Core import *
def main() :
    a=np.matrix(((1,2),(3,4)))
    b=np.matrix(((1,1,1),(1,1,1)))
    c=a * b
    print(c)

main()

Source Program 3:

function main()
{
    vector v1 = [1,0,0];
    vector v2 = [0,1,0];
    vector v3 = [0,0,1];

    matrix mat = [1,0,0;0,1,0;0,0,1;];
    vector vecs[3] = {v1, v2, v3};
    inspace ins = inspace(vecs, mat);
    print(dim(ins));
}

Target Program 3:

#!/usr/bin/python
import sys
sys.path.append('./lib')
from InSpace import *
from AffSpace import *
from Core import *

def main() :
    v1=np.array([1,0,0])
    v2=np.array([0,1,0])

    v3=np.array([0,0,1])

6.2 Test Suites

Several testing strategies and techniques are implemented to achieve the validness and robustness of the LFLA language. Test suites includes positive and negative testing, unit testing and integration testing, white-box and black-box testing, regression testing, and automation testing.

Our tests can be divided into two categories - positive tests and negative ones. Positive tests are designed for valid assertions of statements, which should compile and run successfully, while negative tests aim to detect invalid code, and are expected to fail. Furthermore, both white-box and black-box testing are applied to test the LFLA language. We found that the white-box testing is efficient in finding errors and problems. In the meantime, the black-box testing is good complementary to the white-box testing, and we are able to focus on the functionality of the LFLA language. White-box testing do control flow testing, branch testing, data flow testing, and so forth.

Our testing suites are also conducted in varied levels. We do unit testing on smaller testable units of the LFLA language. Unit testing can catch the bugs early on before any integration, and integration testing is carried out to examine the integrity of the whole system.

Regression testing is the most beneficial testing technique in the whole project. Along with the ongoing changes in the compiler, we recycled our previously established completed tests to check whether the fixed faults have re-emerged. We tried to keep up with the good coding practice. Since it is inefficient to run regression testing manually, we introduce automation testing into our testing suits.
With the help of automated testing, we are able to run the code against the tests regularly. We also intuitively use unit testing on the small testable part of the program, which greatly simply the later-on integration testing. Integration testing are constructed to examine whether the components of the compiler.

6.2.1 Testing Cases
Testing cases are written to test the syntax, semantics, and functionality of the LFLA language. Testing cases can start from the very small pieces to the more complete ones. Testing cases aim to test the LFLA language according to the specifications and the Language Reference Manual. Testing cases cover the identifiers, keywords, statements and blocks, control flows, data types, arrays, built-in functions, comments, operators, variable, as well as function declarations and definitions.

6.2.2 Automation Testing
We have about sixty testing cases. Automation becomes necessary as the project is moving forward. At the beginning, we found the automation testing will streamline our workflow of testing. With the test-driven process in mind, we follows the sequences in its life cycle. We create new tests for new or modified features of our language. Then we run all the tests to check if they are working. Next, if the tests fail, we focus on fix the code to pass the tests, and if the tests pass, we repeat the process from the start. We rely heavily on regression testing, and automated testing enable to automate the repeated tasks on previously completed tests.

6.2.3 Test Roles
Jin Liang designed test cases, and reported bugs to the member responsible for the code (Zhiyuan Guo or ChenZhe Qian), who would in turn find and solve the reported error. Guitang Lan created the testing infrastructure.

7 Lessons Learned
7.1 Chenzhe Qian
I learned several things from this project. First, to have a holistic view of the whole project is the key. Such view can offer a great and efficient management to complete the project. Though no one can know everything before head, it is good to approximate the difficulty of each components. Second, knowing the capability
of each team member is significant. As a team, we need to assign various tasks to
different team members. If we can make good use of everyone, it affects a lot.
Last, we need act as a team. Even in a small team of size four, team work is way
more powerful than individual work if we can act like a whole.

7.2 Guitian Lan
First, about team management: for a small team, hierachical structure is a better
choice for team management. Democracy will only make the project never end.
Also, communication and compromise are key to efficient team; Second, about
meeting: it is better to make a detail plan before weekly meeting, otherwise it is
easy to become a chit chat. Finally, about coding: it is difficult to code the same
file with others. Coding is a very private thing. It is better to divide the program
into several modules, so that each member works on one module by their own.
Advice: Start the project at the first day of class. It is never too earlier to stat
the project.

7.3 Jin Liang
Starting early is the key. Ocaml is hard to get started. Compiler is cool. LFLA
Team is A-Team.

7.4 Zhiyuan Guo
This course is one that theory and practical are tightly combined. Only read the
text book will make everything too abstract to understand. So getting hand dirty
and code our own compiler is a perfect way to learn this course. It will help you
understand the theory more deeply. For the project management, it is difficult to
get a clear path at the beginning of the project. So it will make it a little difficult
to allocate tasks to each one clearly. It delay the project process at some level.
Team work is important in future, I learned a lot about it from this project.

8 Appendix

Listing 1: scanner.mly

```
{ open Lexing
open Parser
(*
+ update line number in the context
```
let next_line lexbuf =
let pos = lexbuf.lex_curr_p in
lexbuf.lex_curr_p <-
  ( pos with pos_idx = lexbuf.lex_curr_pos ;
pos_num = pos.pos_num+1)
)

let Exp = 'e'('+'| '-')?[ '0'−'9']+

rule token = parse

  [' ' '] { token lexbuf }
  [TLR ' ' 'n'']| \r\n { next_line lexbuf ; token lexbuf }
  '###' { comment lexbuf }
  '|' { line_comment lexbuf }
  |'L' { VSCONST }
  |'dim' { DIM }
  |'size' { SIZE }
  |'basis' { BASIS }
  |'print' { PRINT }
  |'rank' { RANK }
  |'trace' { TRACK }
  |'image' { IMAGE }
  |'eigenValue' { EVALUE }
  |'cei l' { CEIL }
  |'floor' { FLOOR }
  |'sqrt' { SQRT }
  |'solve' { SOLVE }

(* several kinds of delimiters *)
'id' { LBRACE }
|'}' { RBRACE }
|'(' { LPAREN }
|')' { RPAREN }
|'.' { SEMI }
|',' { COMMA }
|':' { COLON }
|'= ' { ASSIGN }
|'[[' { LLBRACK }
|'] ]' { RRBRACK }
|'<<' { LIN }
|'@' { ACTION }

(* logical operators *)
|'&&' { AND }
|'||' { OR }

(* additive operators *)
|'+.' { PLUS }
|'-.' { MINUS }
|'+.' { PLUSDOT }
|'-.' { MINUSDOT }

(* multiplicative operators *)
|'*' { TIMES }
|'/.' { DIVIDE }
|'*.' { TIMEDOT }
|'/.' { DIVIDEDOT }

(* unary operator *)
|'\' \' { TRAPOSE }
|'\' \' { BELONGS }
|'&' { ACTION }

(* comparison operators *)
|'<' { LT }
|'=' { LEQ }
|'>' { GT }
|'>=' { GEQ }
|'=' { EQ }


Listing 2: parser.mly
% left LT LEQ GT GEQ EQ NEQ
% left PLUS MINUS PLUS DOT MINUS DOT
% left TIMES DIVIDE TIMES DOT DIVIDE DOT
% left AND OR
% left TRANSPOSE BELONGS ACTION

%start program
%type <ast.program> program
%
%
program:
    programs EOF ( List . rev $1 )
programs :
    /\ nothing */
    { [] }
    | programs function declaration ( Function($2)::$1 )
    | programs global normal declaration { Variable($2)::$1 }
    | error ( raise ( ParseErr ( error "syntax error" ( Parsing . symbol . start . pos ( ) ) ) ) )
function declaration:
    FUNCTION ID LPAREN parameter_list_opt RPAREN LBRACE statement_list RBRACE { $fname=$2; param=$4; body=List . rev $7; ret_type = Unit }
parameter_list_opt:
    /\ nothing */
    { [] }
    | parameter_list ( List . rev $1 )
parameter_list:
    primitive_type ID
    [ ] Lvardecl([vname = $2; value = Notknown; data_type = $1; pos = let pos . start = Parsing . symbol . start . pos ( )])
    | primitive_type LBRACK RBRACK ID
    [ ] Larraydecl([aname = $4; elements = []; data_type = array_type $1; length = max_int; pos = let pos . start = Parsing . symbol . start . pos ( )])
    | parameter_list ID & shape primitive_type ID LBRACK RBRACK
    [ ] Larraydecl([aname = $4; elements = []; data_type = array_type $3; length = max_int; pos = let pos . start = Parsing . symbol . start . pos ( )])
    | error ( raise ( ParseErr ( error "syntax error" ( Parsing . symbol . start . pos ( ) ) ) ) )
local normal declaration:
    local normal declaration expression SEMI { $1 }%
local normal declaration expression:
    variable declaration expression ( Lvardecl($1) )
    | array declaration expression ( Larraydecl($1) )
    | primitive_type ID /
    | global normal declaration expression SEMI { $1 }%
global normal declaration expression:
    variable declaration expression ( Gvardecl($1) )
    | array declaration expression ( Garraydecl($1) )
    | primitive_type ID /
variable declaration expression:
    var declaration expression ( $1 )
    | vector declaration expression ( $1 )
    | matrix declaration expression ( $1 )
    | vecspace declaration expression ( $1 )
    | impspace declaration expression ( $1 )
    | affspace declaration expression ( $1 )
var declaration expression:
    VAR ID
    { vname = $2; value = Notknown; data_type = Var; }
VAR ID ASSIGN LITERAL { Vardec({vname = $2; value = VValue($4); data_type = Var }) } 

expression contains LITERAL */ 

VAR ID ASSIGN expression 

{ vname = $2; value = Expression(Var,$4); data_type = Var; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

vector_declaration_expression : 

VECTOR ID 

{ vname = $2; value = Notknown; data_type = Vector; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

*/ | VECTOR ID ASSIGN LBRACK vector_elements_list_opt RBRACK 

{ vname = $2; value = VecValue($5); data_type = Vector; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

*/ | VECTOR ID ASSIGN expression 

{ vname = $2; value = Expression(Vector,$4); data_type = Vector; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

| nothing */ 

vector_elements_list_opt : 

{ [] } 

| vector_elements_list { List.rev $1 } 

vector_elements_list : 

LITERAL { [$1] } 

| MINUS LITERAL { [String.concat "" ["-";$2]] } 

| vector_elements_list COMMA LITERAL { [$1];$1 } 

| vector_elements_list COMMA MINUS LITERAL { (String.concat "" ["-";$4])::$1 } 

| error 

raise { ParseErr (error "syntax error" (Parsing.symbol_start_pos () (Parsing.symbol_end_pos ()))) } 

matrix_declaration_expression : 

MATRIX ID 

{ vname = $2; value = Notknown; data_type = Matrix; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

*/ | MATRIX ID ASSIGN LBRACK matrix_elements_list opt RBRACK 

{ vname = $2; value = MatValue($5); data_type = Matrix; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

*/ | MATRIX ID ASSIGN expression 

{ vname = $2; value = Expression(Matrix,$4); data_type = Matrix; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

| nothing 

matrix_elements_list : 

vector_elements_list SEMI { [List.rev $1] } 

| vector_elements_list SEMI matrix_elements_list { (List.rev $1)::$3 } 

vecspace_declaration_expression : 

VECSPACE ID 

{ vname = $2; value = Notknown; data_type = VecSpace; 
pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_num } 

| VECSPACE ID ASSIGN expression
```java
{
    vname = $2; value = Expression(VecSpace, $4); data_type = VecSpace;
    pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
}

inspace_declaration_expression :

INSPACE ID
{
    vname = $2; value = Notknown; data_type = InSpace;
    pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
}
| INSPACE ID ASSIGN INSPACE LPAREN expression COMMA expression RPAREN
{
    vname = $2; value = InSpValue($6, $8); data_type = InSpace;
    pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
}

affspace_declaration_expression :

AFFSPACE ID
{
    vname = $2; value = Notknown; data_type = AffSpace;
    pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
}
| AFFSPACE ID ASSIGN AFFSPACE LPAREN expression COMMA expression RPAREN
{
    vname = $2; value = AffSpValue($6, $8); data_type = AffSpace;
    pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
}

array_declaration_expression :

VAR ID LBRACK LITERAL RBRACK
{
    try { aname = $2; elements = []; data_type = VarArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| VAR ID LBRACK LITERAL RBRACK ASSIGN LBRACK array_elements_list RBRACE
{
    try { aname = $2; elements = (List.rev $8); data_type = VarArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| VECTOR ID LBRACK LITERAL RBRACK
{
    try { aname = $2; elements = []; data_type = VectorArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| VECTOR ID LBRACK LITERAL RBRACK ASSIGN LBRACK array_elements_list RBRACE
{
    try { aname = $2; elements = (List.rev $8); data_type = VectorArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| MATRIX ID LBRACK LITERAL RBRACK
{
    try { aname = $2; elements = []; data_type = MatrixArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| MATRIX ID LBRACK LITERAL RBRACK ASSIGN LBRACK array_elements_list RBRACE
{
    try { aname = $2; elements = (List.rev $8); data_type = MatrixArr; length = int_of_string $4;
            pos = let pos_start = Parsing.symbol_start_pos() in pos_start_pos
        } with Failure "int_of_string" -> raise(Failure "not valid array length");
}
| INSPACE ID LBRACK LITERAL RBRACK
{
```
try { name = $2; elements = []; data_type = InSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| INSPACE ID LBRACK LITERAL RBRACK ASSIGN LITERAL array_elements_list RBRACK
| try { name = $2; elements = (List.rev $8); data_type = InSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| AFFSPACE ID LBRACK LITERAL RBRACK
| try { name = $2; elements = []; data_type = AffSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| AFFSPACE ID LBRACK LITERAL RBRACK ASSIGN LITERAL array_elements_list RBRACK
| try { name = $2; elements = (List.rev $8); data_type = AffSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| VECSPACE ID LBRACK LITERAL RBRACK
| try { name = $2; elements = []; data_type = VecSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| VECSPACE ID LBRACK LITERAL RBRACK ASSIGN LITERAL array_elements_list RBRACK
| try { name = $2; elements = (List.rev $8); data_type = VecSpaceArr; length = int_of_string $4; pos = let pos_start = Parsing.symbol_start_pos () in pos_start.pos_inum
 avec Failure "int_of_string" -> raise(Failure "not valid array length");)

| local_declarations
| array_elements_list :
| | expression
| | { [$1] }
| | array_elements_list COMMA expression { $3::$1 }
| |
| statement :
| | expression SEMI
| | { Expr($1) }
| | RETURN expression SEMI { Return($2) }
| | BREAK SEMI { Break }
| | CONTINUE SEMI { Continue }
| | LBRACE statement_list RBRACE { Block(List.rev $2) }
| | IF expression LBRACE statement_list RBRACE ELSE LBRACE statement_list RBRACE
| | IF expression LBRACE statement_list RBRACE
| | IF $2, List.rev $4, $[]
| | FOR ID ASSIGN expression COLON expression LBRACE statement_list RBRACE
| | WHILE expression LBRACE statement_list RBRACE { While($2, List.rev $4) }
| | local_normal_declaration { Decl($1) }
| |
| statement_list :
| | /\ nothing */ { [] }
| | statement_list statement { $2::$1 }
| |
| expression :
| | LITERAL
| | { Literal($1) }
| | element
| | { Id($1) }
| | MINUS LITERAL
| | { Literal(String.concat "" "" '-' $2) }
| | expression TRANSPOSE
| | { Callbuiltin(Transpose, [$1]) }
| | expression PLUS expression
| | { Binop($1, Add, $3) }
| | expression MINUS expression
| | { Binop($1, Sub, $3) }
| | expression TIMES expression
| | { Binop($1, Mult, $3) }
| | expression DIVIDE expression
| | { Binop($1, Div, $3) }
| | expression EQ
| | { Binop($1, Equal, $3) }
| |
Listing 3: ast.ml
type op = Add | Sub | Mult | Div | Add Dot | Sub Dot | Mult Dot
| Div Dot | Equal | Neq | Less | Leq | Greater | Geq
| And | Or
(*
* element, normal id or
* array id with index
*)
type elem =
| Nid of string (* normal identifier *)
| Arrayid of string (* array identifier *)
(* builtin functions *)
type builtin_func =
| Sqrt
| Ceil
| Floor
| Dim
| Size
| Basis
| Image
| Trace
| Eval
| Solve
| Belongs
| LieBracket
| Inpro
| Transpose
| Print
| Action
(* primitive types, separate
* normal types and array types
*)
type prim_type =
| Var
| Vector
| Matrix
| VecSpace
| InSpace
| AffSpace
| VarArr
| VectorArr
| MatrixArr
| VecSpaceArr
| InSpaceArr
| AffSpaceArr
| Unit
(* expressions
* *)
type expr =
| Literal of string
| Id of elem
| Binop of expr * op * expr
| Assign of elem * expr
| AssignArr of elem * expr list
| Call of string * expr list
| Callbuiltin of builtin_func * expr list
| ExprValue of prim_value
| Noexpr
(* value of primitive types *)
and prim_value =
| VValue of string
| VecValue of string list
| MatValue of string list list
| VecSpValue of expr list
| InSpValue of expr * expr
```
(* variable declaration
  * vname : name of variable
  * value : value of variable
  * data_type : type of variable
  * pos : position in original code (not used)
  *
  type var_decl = {
    vname : string;
    value : prim_value;
    data_type : prim_type;
    pos : int;
  }
)

(* array declaration
  * aname : name of array identifier
  * elements : expression list represents the elements of array
  * length : length of the array
  * data_type : type of variable
  * pos : position in original code (not used)
  *
  type array_decl = {
    aname : string;
    elements : expr list;
    data_type : prim_type;
    mutable length : int;
    pos : int;
  }
)

(* combine variable declarations and array declarations
  * only represent global declaration
  *
  type gNormal_decl =
    Gvardecl of var_decl
    | Garraydecl of array_decl
)

(* combine variable declarations and array declarations
  * only represent local declaration
  *
  type lNormal_decl =
    Lvardecl of var_decl
    | Larraydecl of array_decl
)

(* statements *)

type stmt =
  Block of stmt list
  | Expr of expr
  | Return of expr
  | If of expr * stmt list * stmt list
  | For of string * expr * expr * stmt list
  | While of expr * stmt list
  | Continue
  | Break
  | Decl of lNormal_decl

(* function declaration
  * fname : name of function
  * params : list of local normal declarations
  * body : main part of function, a list of statements
  * ret_type : return type of function
  *
  type func_decl = {
    fname : string;
    params : lNormal_decl list;
    body : stmt list;
    ret_type : prim_type;
  }
```

type program_stmt =
| Variable of gNormal_decl
| Function of func_decl

type program = program_stmt list

let real_type = function
  | Var -> Var
  | Vector -> Vector
  | Matrix -> Matrix
  | VecSpace -> VecSpace
  | InSpace -> InSpace
  | AffSpace -> AffSpace
  | VarArr -> Var
  | VectorArr -> VectorArr
  | MatrixArr -> MatrixArr
  | VecSpaceArr -> VecSpaceArr
  | InSpaceArr -> InSpaceArr
  | AffSpaceArr -> AffSpaceArr
  | Unit -> Unit

let array_type = function
  | Var -> VarArr
  | Vector -> VectorArr
  | Matrix -> MatrixArr
  | VecSpace -> VecSpaceArr
  | InSpace -> InSpaceArr
  | AffSpace -> AffSpaceArr
  | VarArr -> VarArr
  | VectorArr -> VectorArr
  | MatrixArr -> MatrixArr
  | VecSpaceArr -> VecSpaceArr
  | InSpaceArr -> InSpaceArr
  | AffSpaceArr -> AffSpaceArr
  | Unit -> Unit

Listing 4: translate.ml

open Ast
open Past
open Check
open Translate_env

(* module StringMap = Map.Make(String) *)
(* input : ast operator
* output : past operator
* translate ast operator to python ast operator
* )
let translate_op = function
  Add -> Padd
  Sub -> Psub
  Mul -> Pmult
  Div -> Pdiv
  Add Dot -> Padd Dot
  Sub Dot -> Psub Dot
(* input : ast operator
* output : past operator
* translate ast prim type to python ast prim type *)
let translate_prim_type = function
Var -> Pvar
| Vector -> P_vector
| Matrix -> P_matrix
| VecSpace -> P_vecSpace
| InSpace -> P_inSpace
| VarArr -> P_varArr
| VectorArr -> P_vectorArr
| MatrixArr -> P_matrixArr
| VecSpaceArr -> P_vecSpaceArr
| InSpaceArr -> P_inSpaceArr
| AffSpaceArr -> P_affSpaceArr
| Unit -> P_unit

(* input : ast element
* output : past element
* translate ast element to python ast element , and
* check symbol tables , throw exception if they are not defined
* )
let translate_elem env = function
| Nid(s) ->
  if is_defined var s env then
    P_nid(s)
  else raise (Failure ("undeclared identifier" ~ s))
| Arrayid(s1, s2) ->
  if is_defined var s1 env then
    P_arrayid(s1, s2)
  else raise (Failure ("undeclared identifier" ~ s1))

(* input : env->translate_env and ast expression list
* output : past expression list and updated env
* traverse_exprs works to translate a list of expression
* )
let rec traverse_exprs env = function
| [] -> [] , env
| hd :: tl ->
  let pE, env = translate_expr env hd in
  let pTl, env = traverse_exprs env tl in
  pE : : pTl , env

(* input : ast expression and translate environment
* output : past expression and updated environment
* translate ast expr to python ast expr and do some basic checks
* )
and translate_expr env = function
Literal(l) -> (P_literal(l), env)
Id(e1) -> (P_id(translate_elem env e1), env)
| Binop(e1, o, e2) ->
  let (pE1, env) = translate_expr env e1 in
  let pO = translate_op o in
  let (pE2, env) = translate_expr env e2 in
  (match (type_of env e1, o, type_of env e2) with
  | Matrix, Mult_Dot, Matrix -> (P_matrixMul(pE1, pE2), env)
  | ..., ... -> (P_binop(pE1, pO, pE2), env))
Assign el e -> 
| if not (is_defined_element el env) then
| raise (Failure("undefined identifier"))
| else
| let pE, env = translate_expr env e in
| let pEI = translate_elem env el in
| P_assign(pEI, pE), env

AssignArr el e ->
| if not (is_defined_element el env) then
| raise (Failure("undefined identifier"))
| else
| let pE, env = traverse_exprs env e in
| let pEI = translate_elem env el in
| P_assignArr(pEI, pE), env

Call f el -> 
| if not (is_function f env) then
| raise (Failure("undefined function"))
| else
| let pE, env = traverse_exprs env e in
| (P_call(f, pE), env)

Callbuiltin f el -> (*TODO: check the builtin function types *)
| if (List.length el) == 0 then
| raise (Failure("wrong arguments in builtin function"))
| else
| let pElist, env = traverse_exprs env e in
| (match f with
| | Sqrt -> P_sqrt(List.hd pElist), env
| | Ceil -> P_ceil(List.hd pElist), env
| | Floor -> P_floor(List.hd pElist), env
| | Dim ->
| | let pE = List.hd pElist in
| | let typ = type_of env (List.hd el) in
| | P_dim(translate_prim_type typ, pE), env
| | Size -> P_size(List.hd pElist), env
| | Basis -> P_basis(List.hd pElist), env
| | Image -> P_image(List.hd pElist), env
| | Rank -> P_rank(List.hd pElist), env
| | Trace -> P_trace(List.hd pElist), env
| | Eval -> P_eval(List.hd pElist), env
| | Solve ->
| | if (List.length pElist) <> 2 then
| | raise (Failure("wrong arguments in builtin function"))
| | else P_solve(List.hd pElist, List.nth pElist 1), env
| | Belongs ->
| | if (List.length pElist) <> 2 then
| | raise (Failure("wrong arguments in builtin function"))
| | else P_belongs(List.hd pElist, List.nth pElist 1), env
| | LieBracket ->
| | if (List.length pElist) <> 2 then
| | raise (Failure("wrong arguments in builtin function"))
| | else P_lieBracket(List.hd pElist, List.nth pElist 1), env
| | Inpro ->
| | if (List.length pElist) <> 3 then
| | raise (Failure("wrong arguments in builtin function"))
| | else P_inpro(List.hd pElist, List.nth pElist 1, List.nth pElist 2), env
| | Transpose -> P_transpose(List.hd pElist), env
| | Action ->
| | if (List.length pElist) <> 2 then
| | raise (Failure("wrong arguments in builtin function"))
| | else P_action(List.hd pElist, List.nth pElist 1), env
| | Print -> P_print(List.hd pElist), env)
| | ExprValue v ->
| | let pV, env = translate_prim_value env v in
| | P_exprValue(pV), env
| | Noexpr -> P_noexpr, env

(* input: ast_prim_value and translate environment
* output: past_prim_value and updated environment

49
• translate ast prim_value to past prim_value
• do type checking during translation
and translate prim_value env = function

VValue(s) -> P_Value(s), env
| VecValue(s) -> P_VecValue(s), env
| MatValue(s) -> P_MatValue(s), env
| VecSpValue(eList) ->
let pEList, env = traverse_exps env eList in
if check_list env Vector eList then
  P_VecSpValue(pEList), env
else if (List.length eList == 1) then
  if check_list env VectorArr eList then
    P_VecSpValueArr(pEList), env
else
  raise(Failure("in vsconst fail in type checking"))
else
  raise(Failure("in vsconst fail in type checking"))

| InSpValue(e1, e2) ->
let pE1, env = translate_expr env e1 in
let pE2, env = translate_expr env e2 in
let typ1 = type_of env e1 in
let typ2 = type_of env e2 in
if typ1 <> VectorArr || typ2 <> Matrix then
  raise(Failure("in InSpace construct fail in type checking"))
else
  P_InSpValue(pE1, pE2), env

| AffSpValue(e1, e2) ->
let pE1, env = translate_expr env e1 in
let pE2, env = translate_expr env e2 in
let typ1 = type_of env e1 in
let typ2 = type_of env e2 in
if typ1 <> Vector || typ2 <> VecSpace then
  raise(Failure("in AffSpace construct fail in type checking"))
else
  P_AffSpValue(pE1, pE2), env

| Expression(typ, e) ->
let pExpr, env = translate_expr env e in
let typ' = type_of env e in
if typ' <> typ then
  raise(Failure("in construct fail in type checking"))
else
  P_Expression(pExpr), env

| Notknown -> P_Notknown, env

(* input: ast local declaration and translate environment
* output: past local declaration and updated environment
* translate local variables to python ast variables *)
let translate_local_normal_decl env local_var =
let match local_var with
  | Lvardecl(v) ->
    let p_value, env = translate_prime_value env v.value in
    let p_var = {
        p_vname = v.vname,
        p_value = p_value;
        p_data_type = translate_prime_type v.data_type;
        p_pos = v.pos
    } in
    if (not (is_defined_var v.vname env)) then
      StringMap.add v.vname local_var.env.scope.vars
    else
      raise(Failure("Already defined variable " + v.vname))
    in
    let scope' = {
        env.scope with vars = vars'
    } in
    P_Vardecl(p_var), env

  | Larraydecl(a) ->
    let length = List.length a.elements in
if length <> 0 && length <> a.length then (* length = 0 occurs only when a is function param *)
raise Failure("array length not match")
else
let pExprs, env = traverse_exprs env a.elements in
if not (check_list env (real_type a.data_type) a.elements) then (* check if array elements have right type *)
raise Failure("array elements have wrong type")
else
let parray = { p.aname = a.aname;
               p.elements = pExprs;
               p.data_type = translate_prim_type a.data_type;
               p.length = a.length;
               p.pos = a.pos }
in
let vars' =
if (not (is_defined_var a.aname env)) then
StringMap.add a.aname local_var env.scope.vars
else
raise Failure("Already defined variable " " a.aname")
in
let scope' = { env.scope with vars = vars' } in
let env' = { env with scope = scope' } in
P.Arraydecl(parray), env'

(* input: ast global declaration and translate environment
* output: past global declaration and updated environment
* translate global variables to python ast variables *)
let translate_global_normal_dec env global_var =
match global_var with
| Garraydecl(a) ->
  let length = List.length a.elements in
  if length <> 0 && length <> a.length then (* length = 0 occurs only when a is a function param *)
  raise Failure("array length not match")
  else
    let pExprs, env = traverse_exprs env a.elements in
    if not (check_list env (real_type a.data_type) a.elements) then (* check if each element if it has right type *)
    raise Failure("array elements have wrong type")
    else
      (* for global array, local_vars table is empty *)
      let parray = { p.aname = a.aname;
                    p.elements = pExprs;
                    p.data_type = translate_prim_type a.data_type;
                    p.length = a.length;
                    p.pos = a.pos }
in
      let global_vars' =
        if (not (is_global_var a.aname env)) then
          StringMap.add a.aname global_var env.global_vars
        else
          raise Failure("Already defined variable " " a.aname")
in
      let env' = { env with global_vars = global_vars' } in
P.Arraydecl(parray), env'
(* input : return expression list ,
* function body statements ,
* translate environment
* output : return expression list
* collect all return expressions in function
* *)

let rec find_return_exps env ret_exps body =
match body with
[
] -> ret_exps
| hd :: tl ->
  (match hd with
   Return (e) ->
   let ret_exps' = e :: ret_exps in
   find_return_exps env ret_exps' tl
   | Block(stmts) ->
   let ret_exps1 = find_return_exps env ret_exps stmts in
   find_return_exps env ret_exps1 tl
   | Expr(e) ->
   find_return_exps env ret_exps tl
   | If (e, s1, s2) ->
   let ret_exps1 = find_return_exps env ret_exps s1 in
   let ret_exps2 = find_return_exps env ret_exps s2 in
   find_return_exps env ret_exps2 tl
   | While(e, s) ->
   let ret_exps1 = find_return_exps env ret_exps s in
   find_return_exps env ret_exps1 tl
   | For(v, e1, e2, s) ->
   let ret_exps1 = find_return_exps env ret_exps s in
   find_return_exps env ret_exps1 tl
   | Continue ->
   find_return_exps env ret_exps tl
   | Break ->
   find_return_exps env ret_exps tl
   | Decl(l) ->
   find_return_exps env ret_exps tl
   )

(* input : return expression list ,
* translate environment
* *)

let find_return_type env ret_exps =
if (List.length ret_exps) = 0 then
  Unit
else
  let expr = List.hd ret_exps in
  let ret_typ = type_of env expr in
  if (check_list env ret_typ ret_exps) then
    ret_typ
  else
    raise (Failure "function return type don't match")

(* input : ast statements list
* translate environment
* output : past statements list
* translate a list of statements
* *)

let rec traverse_stmts env = function
[ ] -> [], env
| hd :: tl ->
  let pStmt, env = translate_stmt env hd in
  let pTl, env = traverse_stmts env tl in
  pStmt :: pTl, env

(* input : ast statement
* translate environment
* output : past statement
* translate ast stmt to python ast statement
* *)
* do type checking during translation
* *)

and translate_stmt env= function Block(stmts) ->
  let scope' = { parent = Some(env.scope); vars = StringMap.empty } in
  let env' = { env with scope = scope' } in
  let pStmts, env' = traverse_stmts env' stmts in
  P_block(pStmts), env

| Expr(expr) ->
  let pExpr, env = translate_expr env expr in
  let _ = type_of env expr in
  P_expr(pExpr), env

| Return(expr) ->
  let pExpr, env = translate_expr env expr in
  P_return(pExpr), env

| If(expr, stmt1, stmt2) ->
  let pExpr, env = translate_expr env expr in
  let typ = type_of env expr in
  if typ<>Var then
    raise(Failure("condition in if should be var type"))
  else
    let scope' = { parent = Some(env.scope); vars = StringMap.empty } in
    let pStmts1, _ = traverse_stmts env' stmt1 in
    let pStmts2, _ = traverse_stmts env' stmt2 in
    (let env = { env with return_type = ret_type1 } in *)
    P_if(pExpr, pStmts1, pStmts2), env

| For(id, a1, a2, stmt) ->
  let typ, _ = type_of_id env id in
  if typ<>Var then
    raise(Failure("variable in for should be var type"))
  else
    let pExpr1, env = translate_expr env a1 in
    let pExpr2, env = translate_expr env a2 in
    let typ1 = type_of env a1 in
    let typ2 = type_of env a2 in
    if typ1<>Var || typ2<>Var then
      raise(Failure("condition in for should be var type"))
    else
      let scope' = { parent = Some(env.scope); vars = StringMap.empty } in
      let env' = { env with scope = scope' } in
      let pStmts, _ = traverse_stmts env' stmt in
      P_for(1, pExpr1, pExpr2, pStmts), env

| While(expr, stmt) ->
  let pExpr, env = translate_expr env expr in
  let typ = type_of env expr in
  if typ<>Var then
    raise(Failure("condition in while should be var type"))
  else
    let scope' = { parent = Some(env.scope); vars = StringMap.empty } in
    let env' = { env with scope = scope' } in
    let pStmts, _ = traverse_stmts env' stmt in
    P_while(pExpr, pStmts), env

| Continue ->
  if (not env.in_while) && (not env.in_for) then
    raise(Failure("continue doesn’t appear in a for loop or while loop"))
  else
    P_continue, env

| Break ->
  if (not env.in_while) && (not env.in_for) then
    raise(Failure("continue doesn’t appear in a for loop or while loop"))
  else
    P_break, env

| Decl(d) ->
  let pD, env = translate_local_normal_decl env d in
  P_decl(pD), env

(* translate a list of local variables *)
let rec traverse_local-vars env = function
let p, env = translate_local env hd in
p, env = translate_local env tl in

let p, env = translate_func_decl env fdec1 =
if (not (is_func fdec1.fname env)) then
let pParams, env = translate_local env fdec1.params in
let pStmts, env = translate_local env fdec1.body in
let ret_typ = find_return_type env ret_exps in
let fdec1' = { fdec1 with ret_type = ret_typ } in
let env' = { env with global_funcs = global_funcs' } in
{
  p.fname = fdec1.fname;
  p.params = pParams;
  p.body = pStmts
}, env'
else
  raise(Failure("Already defined function " fdec1.fname))

let translate_program stmt env = function
  Variable(v) -> let variable, env = translate_global env v
in P_Variable(v), env
| Function(f) ->
  let scope' = { parent = Some(Some(None; vars=StringMap.empty); vars=StringMap.empty) } in
  let env' = { env with scope = scope' } in
  let func, env' = translate_func_decl env' f
in P_Function(func), env'

let rec translate_program env = function
  [] -> [], env
| hd::tl ->
  let p, env = translate_program stmt env hd in
  let p, env = translate_program env tl in
p, env in

let scope' = { parent = None; vars=StringMap.empty } in
let env = { scope = scope';
global_vars = StringMap.empty;
global_funcs = StringMap.empty;
in,while = false;
in,for = false;
} in
let p, env = translate_program env program (* give empty global_vars and global_funcs symbol table *)
in
if (not (is_func "main" env')) then
  raise(Failure("no main function"))
else
  p, program
open Ast

module StringMap = Map.Make(String)

(* symbol table used for scope
 * parent: parent scope
 * vars: local variables table
 *)
type symbol_table = { parent : symbol_table option;
                     vars : Normal.decl StringMap.t; }

(* translation environment
 * scope: used for scope rule check
 * global_vars: global variable table
 * global_funcs: defined function table
 * in_while: if it is in a while loop
 * in_for: if it is in a for loop
 *)
type translate_env = {
  scope : symbol_table;
  global_vars : Normal.decl StringMap.t;
  global_funcs : func.decl StringMap.t;
  in_while : bool;
  in_for : bool;
}

(* check if it is a function name *)
let is_func fname env = StringMap.mem fname env.global_funcs

(* find and return function declaration *)
let find_func fname env = StringMap.find fname env.global_funcs

(* check if it is a global variable *)
let is_global_var vname env = StringMap.mem vname env.global_vars

(* find and return variable declaration *)
let find_global_var vname env = StringMap.find vname env.global_vars

(* check if it is a variable defined *)
let rec is_scope_var vname scope =
  if StringMap.mem vname scope.vars then
    true
  else
  (match scope.parent with
   Some(parent) -> is_scope_var vname parent
   | None -> false)

(* check if it is a local variable *)
let is_local_var vname env = is_scope_var vname env.scope

(* find the variable declaration *)
let rec find_scope_var vname scope =
  try StringMap.find vname scope.vars
  with Not_found ->
    match (scope.parent) with
    Some(parent) -> find_scope_var vname parent
    | None -> raise Not_found

(* find the variable declaration *)
let find_local_var vname env = find_scope_var vname env.scope

(* check if the variable is defined *)
let is_defined_var vname env =
  if is_local_var vname env || is_global_var vname env then
    true
  else
    false
(* check if the element if defined *)

let is_defined_element el env =
    match el with
    Nid(s) -> is_defined_var s env
    | Arrayid(s1, s2) -> is_defined_var s1 env

Listing 6: check.ml

open Ast
open Translate

(* input: string of identifier
* translate environment
* output: (type, length)
* if it is an array identifier, return length of array,
* otherwise return 0.
*)

let type_of_id env s =
    if is_local_vars env then
        let decl = find_local_vars env in
        match decl with
        Lvardecl (var) -> (var.data.type, 0)
        | Larraydecl(arr) -> (arr.data.type, arr.length)
    else if is_global_vars env then
        let decl = find_global_vars env in
        match decl with
        Gvardecl (var) -> (var.data.type, 0)
        | Garraydecl(arr) -> (arr.data.type, arr.length)
    else raise (Failure "not defined id")

(* check if s is a valid array index *)

let valid_index env s =
    try int_of_string s
    with Failure "int_of_string" -> -1

(* get the type of element
* if it is an array type, return it real type
*)

let type_of_element env = function
    Nid(s) -> let typ, _ = type_of_id env s in typ
    | Arrayid(s1, s2) ->
        let typ, len = type_of_id env s1 in
        let index = valid_index env s2 in
        if index > (len-1) then raise (Failure "array index is out bound")
        else (match typ with
        VarArr -> Var
        VectorArr -> Vector
        MatrixArr -> Matrix
        VecSpaceArr -> VecSpace
        InSpaceArr -> InSpace
        AffSpaceArr -> AffSpace
        _ -> raise (Failure "wrong array type") )

(* input: a list of expressions
* target type
* translate environment
* output: true or false
* check if a list of expression have same target type *)

let rec check_list env typ = function
    [] -> true
    | hd::tl ->
        let typ' = type_of env hd in
        if typ' <> typ then false
        else check_list env typ tl
and type of env = function

\[\text{Literal}(s) \to \text{Var}\]

\[\text{Id}(el) \to \text{type of element env el}\]

\[\text{Binop}(el, op, e2) \to \]

| match op with
| Add \to (match (type of env el, type of env e2) with
| (Var, Var) \to \text{Var}
| (Vector, Vector) \to \text{Vector}
| (Matrix, Matrix) \to \text{Matrix}
| (VecSpace, VecSpace) \to \text{VecSpace}
| \to \text{raise(Failure("in add(sub) two operands don't have same type"))})
| Sub \to (match (type of env el, type of env e2) with
| (Var, Var) \to \text{Var}
| (Vector, Vector) \to \text{Vector}
| (Matrix, Matrix) \to \text{Matrix}
| \to \text{raise(Failure("in add(sub) two operands don't have same type"))})
| Mult | Div \to (match (type of env el, type of env e2) with
| (Var, Var) \to \text{Var}
| (Vector, Vector) \to \text{Vector}
| (Matrix, Matrix) \to \text{Matrix}
| \to \text{raise(Failure("in * fail in type checking")})
| Add\_Dot | Sub\_Dot | Mul\_Dot | Div\_Dot \to
| (match (type of env el, type of env e2) with
| (Var, Var) \to \text{Var}
| (Vector, Vector) \to \text{Vector}
| (Matrix, Matrix) \to \text{Matrix}
| \to \text{raise(Failure("in +, -, fail in type checking")})
| Equal | Neq | Less | Leq
| Greater | Geq | And | Or \to
| (match (type of env el, type of env e2) with
| (Var, Var) \to \text{Var}
| \to \text{raise(Failure("in comparasion fail in type checking")})
| Assign(el, e) \to
| let el\_type = type of element env el in
| let expr\_type = type of env e in
| if el\_type = expr\_type then
| el\_type
| else
| \text{raise(Failure("in assign fail in type checking")})
| AssignArr(el, eList) \to
| let el\_type = type of element env el in
| if check\_list env el\_type eList then
| el\_type
| else
| \text{raise(Failure("in assign array fail in type checking")})
| Call(fid, eList) \to
| let fdec =
| if is\_func fid env then
| find\_func fid env
| else
| \text{raise(Failure("in call not defined function")})
| in
| let rec check\_two\_lists env list1 list2 fdec =
| match list1, list2 with
| [], [] \to fdec, ret\_type
| let hd1, tl1 = [] \to \text{raise(Failure("in call fail in type checking(not same type")})
| [], hd2, tl2 \to \text{raise(Failure("in call fail in type checking(not same length")})
| hd1, hd2, tl2 \to
| let typ = (match hd1 with

57
Lvardecl(var) -> var.data_type
| Larraydecl(arr) -> arr.data_type

in
let typ2 = type_of env hd2 in
if typ1 <> typ2 then
  raise(Failure("in call fail in type checking(not match")
else
  check_two_lists env t1 t2 fdecl
in
check_two_lists env fdecl.params eList fdecl
| Callbuiltin(f, el) ->
  (match f with
  | Sqrt | Ceil | Floor ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions(type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> Var then
        raise(Failure("in builtin fail in type checking")
      else
        Var
  | Dim ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions (type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> Var && typ <> Vector && typ <> AffSpace && typ <> InSpace then
        raise(Failure("in builtin fail in type checking")
      else
        Var
  | Size ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions(type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> Matrix then
        raise(Failure("in builtin fail in type checking")
      else
        VarArr
  | Basis ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions(type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> VecSpace then
        raise(Failure("in builtin fail in type checking")
      else
        Var
  | Image ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions(type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> Matrix then
        raise(Failure("in builtin fail in type checking")
      else
        VecSpace
  | Rank | Trace ->
    if (List.length el) <> 1 then
      raise(Failure("wrong arguments in builtin functions(type checking")
    else
      let typ = type_of env (List.hd el) in
      if typ <> Matrix then
        raise(Failure("in builtin fail in type checking")
      else
        Var
  | Evalue ->
    if (List.length el) <> 1 then

raise (Failure ("wrong arguments in built-in functions (type checking)"))
else
  let typ = type_of env (List.hd el) in
  if typ <> Matrix then
    raise (Failure ("in built-in fail in type checking"))
  else
    VarArr
| Belongs ->
  if (List.length el) <> 2 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match (type_of env (List.hd el), type_of env (List.nth el 1)) with
      (Vector, VecSpace) -> Var
      | (Vector, AffSpace) -> Var
      | _ -> raise (Failure ("in belongs fail in type checking")))
| LieBracket ->
  if (List.length el) <> 2 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match (type_of env (List.hd el), type_of env (List.nth el 1)) with
      (Matrix, Matrix) -> Matrix
      | _ -> raise (Failure ("in liebracket fail in type checking")))
| Inpro ->
  if (List.length el) <> 3 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match (type_of env (List.hd el), type_of env (List.nth el 1), type_of env (List.nth el 2)) with
      (InSpace, Vector, Vector) -> Var
      | _ -> raise (Failure ("in inner product fail in type checking")))
| Transpose ->
  if (List.length el) <> 1 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match type_of env (List.hd el) with
      Matrix -> Matrix
      | _ -> raise (Failure ("in transpose fail in type checking")))
| Solve ->
  if (List.length el) <> 2 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match (type_of env (List.hd el), type_of env (List.nth el 1)) with
      (Matrix, Vector) -> AffSpace
      | _ -> raise (Failure ("in solve fail in type checking")))
| Action ->
  if (List.length el) <> 2 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    (match (type_of env (List.hd el), type_of env (List.nth el 1)) with
      (Matrix, Vector) -> Vector
      | _ -> raise (Failure ("in action fail in type checking")))
| Print ->
  if (List.length el) <> 1 then
    raise (Failure ("wrong arguments in built-in functions (type checking)"))
  else
    let _ = type_of env (List.hd el) in
    Unit
| ExprValue (v) ->
  let typ = type_of_value env v in
  typ
| Noexpr -> Unit
(* get the type of prim value *)
and type_of_value env = function
  VValue (s) -> Var
  | VecValue (s) -> Vector
  | MatValue (s) -> Matrix
  | VecSpValue (s) -> VecSpace
  |
| 269  | InSpValue(e1, e2) → InSpace  |
| 270  | AffSpValue(e1, e2) → AffSpace |
| 271  | Expression(typ, e) → typ     |
| 272  | Notknown → Unit             |

Listing 7: past.ml

```ml
(* operators *)

type pOp = Padd | Psub | Pmult | Pdiv | Padd_Dot | Psub_Dot | Pmult_Dot |
         | Pdiv_Dot | Pequal | Pneq | Pless | Pleq | Pgreater | Pgeq |
(5)     | Pand     | Por    |

(* element, normal id or array id with index *)

(type pElem =
  | Pnid of string (* normal identifier *)
  | Parrayid of string (* array identifier *)
  | *)

(* primitive types, separate normal types and array types *)

(type pPrim_type =
  | P_var
  | P_vector
  | P_matrix
  | P_vecSpace
  | P_inSpace
  | P_affSpace
  | P_varArr
  | P_vectorArr
  | P_matrixArr
  | P_affSpaceArr
  | P_unit)

(* expression *)

(type pExpr =
  | P_literal of string
  | P_id of pElem
  | P_binop of pExpr + pOp + pExpr
  | P_belongs of pExpr + pExpr
  | P_inpro of pExpr + pExpr
  | P_transpose of pExpr
  | P_assign of pElem + pExpr
  | P_assignArr of pElem + pExpr list
  | P_call of string + pExpr list
  | P_print of pExpr
  | P_exprValue of pPrim_value
  | P_matrixMul of pExpr * pExpr
  | P_dim of pPrim_type + pExpr
  | P_size of pExpr
  | P_basis of pExpr
  | P_trace of pExpr
  | P_image of pExpr
  | P_rank of pExpr
  | P_value of pExpr
  | P_celil of pExpr
  | P_floor of pExpr
  | P_sqrt of pExpr
  | P_solve of pExpr + pExpr
  | P_action of pExpr * pExpr
  | P_noExpr

(* value of primitive type *)

and pPrim_value =

  P_Value of string
```
(* Variable declaration *
   * p_vname : name of variable
   * p_value : value of variable
   * p_data_type : type of variable
   * p_pos : position in original code (not used)
)

```
type pVar_decl = {
  p_vname : string;
  p_value : pPrim_value;
  p_data_type : pPrim_type;
  p_pos : int;
}
```

(* Array declaration *
   * p_aname : name of array identifier
   * p_elements : expression list represents the elements of array
   * p_length : length of the array
   * p_data_type : type of variable
   * p_pos : position in original code (not used)
)

```
type pArray_decl = {
  p_aname : string;
  p_elements : pExpr_list;
  p_data_type : pPrim_type;
  p_length : int;
  p_pos : int;
}
```

(* Combine variable declarations and array declarations *)

```
type pNormal_decl =
  | P_Vardecl of pVar_decl
  | P_Arraydecl of pArray_decl
```

(* Statement *)

```
type pStmt =
  | P_block of pStmt_list
  | P_expr of pExpr
  | P_return of pExpr
  | P_if of pExpr * pStmt_list * pStmt_list
  | P_for of pExpr * pExpr * pExpr * pStmt_list
  | P_while of pExpr * pStmt_list
  | P_continue
  | P_break
  | P_decl of pNormal_decl
```

(* Function declaration *
   * p_fname : name of function
   * p_params : list of local normal declarations
   * p_body : main part of function, a list of statements
   * p_ret_type : return type of function
)

```
type pFunc_decl = {
  p_fname : string;
  p_params : pNormal_decl_list;
  p_body : pStmt_list;
}
```

(* Combine global variable declaration and function declaration *)

```
type pProgram_stmt =
  | P_Variable of pNormal_decl
```
open Past

(* generate code for element *)
let string_of_elem = function
  | P_id (s) -> s
  | P_arrayid (el, s2) -> s1 ^ "[" ^ s2 ^ " ]"

(* generate code for expression *)
let rec string_of_expr = function
  | P_literal (l) -> l
  | P_id (el) -> string_of_elem el
  | P_transpose (e) -> "np.transpose(" ^ string_of_expr e ^ ")"
  | P_binop (el, o, e2) ->
    string_of_expr el ^ "", string_of_expr e2
  | P_padd (-) -> "+" | P_psub (->) -> "-" | P_pmult (->) -> "*" | P_pdiv (->) -> "/"
  | P_padd_dot (-) -> "+.dot" | P_psub_dot (->) -> "-.dot" | P_pmul_dot (->) -> "*dot" | P_ppdiv_dot (->) -> "/dot"
  | P_pless (kle) -> kle ^ "<" | P_pgeq (kle) -> kle ^ ">
  | P_pow (kle) -> kle ^ "**" | P_pgreater (kle) -> kle ^ ">>" | P_pgeq (kle) -> kle ^ ">>="
  | P_floordiv (kle) -> kle ^ "//" | P_pow (kle) -> kle ^ "**" | P_pow (kle) -> kle ^ "**=
  | P_fround (kle) -> kle ^ "round" | P_pow (kle) -> kle ^ "pow" | P_pow (kle) -> kle ^ "pow=
  | P_str (s) -> "string" ^ s
  | P_id (el) -> string_of_expr el

(* built-in functions *)
| P_belongs (el, e2) -> string_of_expr el ^ ".belongs(" ^ string_of_expr el ^ ",")"
| P_lieBracket (el, e2) -> "lieBracket(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_inprod (id, el, e2) -> "np.prod(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_assign (v, e) -> string_of_elem v ^ = "string_of_expr e"
| P_assignArr (v, e) -> string_of_elem v ^ = "string_of_expr e"
| P_lieBracket (el, e2) -> "lieBracket(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_makeProd (v, e) -> "makeProd(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_size (typ, e) -> (match typ with
    | P_vector -> string_of_expr e ^ ".size"
    | P_vecSpace | P_inSpace | P_allSpace -> string_of_expr e ^ ".dim()"
    | "wrong type")
| P_size (typ, e) -> string_of_expr e ^ ".shape"
| P_basis (el) -> string_of_expr el ^ ".basis()"
| P_trace (e) -> "trace(" ^ string_of_expr e ^ ")"
| P_rank (el) -> "rank(" ^ string_of_expr e ^ ")"
| P_image (e) -> "image(" ^ string_of_expr e ^ ")"
| P_eval (e) -> "eval(" ^ string_of_expr e ^ ")"
| P_print (e) -> "print(" ^ string_of_expr e ^ ")"
| P_stdValue (v) -> string_of_prim_value v
| P_action (el, e2) -> "np.tanspose(np.array(" ^ string_of_expr el ^ ")" ^ np.tanspose(np.array(" ^ string_of_expr e2 ^ "))"
| P_matrixMul (el, e2) -> "np.multiply(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"

(* generate code for prim value *)
and string_of_prim_value = function
| P_Value (s) -> s
| P_MatValue (s) -> "np.array([" ^ String_concat ^ "]) ^ "s" ^ "]"
| P_VecValue (s) -> "np.array([" ^ String_concat ^ "]) ^ List.map (fun s -> "([" ^ s ^ "]") ^ List.map (String.concat ^ " ,")
| P_VecSpaceValue (elList) -> "VecSpace([" ^ String_concat ^ "]) ^ List.map string_of_expr elList ^ "]")
| P_VecSpaceArr (elList) -> "VecSpace([" ^ String_concat ^ "]) ^ List.map string_of_expr elList ^ "]")
| P_NameSpaceValue (el, e2) -> "NameSpace(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_AffSpaceValue (el, e2) -> "AffSpace(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"
| P_Expression (el) -> string_of_expr e
| P_Bottom ()
| (match typ with
    | P_vector -> string_of_expr e ^ ".size"
    | P_vecSpace | P_inSpace | P_allSpace -> string_of_expr e ^ ".dim()"
    | "wrong type")
| P_size (typ, e) -> string_of_expr e ^ ".shape"
| P_trace (e) -> "trace(" ^ string_of_expr e ^ ")"
| P_rank (el) -> "rank(" ^ string_of_expr e ^ ")"
| P_image (e) -> "image(" ^ string_of_expr e ^ ")"
| P_eval (e) -> "eval(" ^ string_of_expr e ^ ")"
| P_print (e) -> "print(" ^ string_of_expr e ^ ")"
| P_stdValue (v) -> string_of_prim_value v
| P_action (el, e2) -> "np.tanspose(np.array(" ^ string_of_expr el ^ ")" ^ np.tanspose(np.array(" ^ string_of_expr e2 ^ "))"
| P_matrixMul (el, e2) -> "np.multiply(" ^ string_of_expr el ^ ",", string_of_expr e2 ^ ")"

(* generate code for prim type *)
let string_of_prim_type = function

Listing 8: compile.ml

132 | P_function of PFunc_decl
133
134 (* root of past *)
135 type pProgram = pProgram_stmt_list

62
( * input : declaration  
* number of indent  
* output: python code for declaration  
* )

let string_of_normal_decl num_ident decl =
  let spaces = 4 in
  match decl with
  | P_Vardecl(v) -> ( String.make (num_ident*spaces) ' ' ) ^ v.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Vectordecl(v) -> ( String.make (num_ident*spaces) ' ' ) ^ v.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Arraydecl(a) -> ( String.make (num_ident*spaces) ' ' ) ^ a.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Block(stmts) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( List.map string_of_stmt (num_ident+1) stmts)^ " in "
  | P_If(expr) -> ( String.make (num_ident*spaces) ' ' ) ^ " if " ^ string_of_expr expr ^ " then "
  | P_Else -> ( String.make (num_ident*spaces) ' ' ) ^ " else "
  | P_Return(expr) -> ( String.make (num_ident*spaces) ' ' ) ^ " return " ^ string_of_expr expr ^ " ; "
  | P_Break -> ( String.make (num_ident*spaces) ' ' ) ^ " break "
  | P_Continue -> ( String.make (num_ident*spaces) ' ' ) ^ " continue "
  | P_For (l, a1, a2, a) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " for " ^ " in range(" ^ ( String.make (num_ident*spaces) ' ' ) ^ " string_of_expr a1 " ^ " , " ^ ( String.make (num_ident*spaces) ' ' ) ^ " string_of_expr a2 " ^ " ) ^ " ; "
  | P_ForEach(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( String.make (num_ident*spaces) ' ' ) ^ " in " ^ ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( String.make (num_ident*spaces) ' ' ) ^ " in "
  | P_Return(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " return " ^ string_of_expr expr ^ " ; "
  | P_While(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " while " ^ string_of_expr expr ^ " do "
  | P_Decl(d) -> string_of_normal_decl num_ident d

(* generate code for function parameters *)
let string_of_params = function
  | P_Vardecl(v) -> v.p_name
  | P_Arraydecl(a) -> a.p_name

(* generate code for function declaration *)
let string_of_func_decl fdecl =
  ( " def " ^ ( P_Vardecl(v) -> string_of_normal_decl 0 v
  | P_Function(f) -> string_of_func_decl f

(* generate code for program statement *)
let string_of_program_stmt = function

(* input : statement  
* number of indent  
* output: python code for statement  
* )

let rec string_of_stmt num_ident stmt =
  let spaces = 4 in
  match stmt with
  | P_Vardecl(v) -> ( String.make (num_ident*spaces) ' ' ) ^ v.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Vectordecl(v) -> ( String.make (num_ident*spaces) ' ' ) ^ v.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Arraydecl(a) -> ( String.make (num_ident*spaces) ' ' ) ^ a.p_name ^ "=" ^ ( String.concat " , " ( List.map string_of_expr a.params ) ^ " ; " )
  | P_Block(stmts) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( List.map string_of_stmt (num_ident+1) stmts)^ " in "
  | P_If(expr) -> ( String.make (num_ident*spaces) ' ' ) ^ " if " ^ string_of_expr expr ^ " then "
  | P_Else -> ( String.make (num_ident*spaces) ' ' ) ^ " else "
  | P_Return(expr) -> ( String.make (num_ident*spaces) ' ' ) ^ " return " ^ string_of_expr expr ^ " ; "
  | P_Break -> ( String.make (num_ident*spaces) ' ' ) ^ " break "
  | P_Continue -> ( String.make (num_ident*spaces) ' ' ) ^ " continue "
  | P_For (l, a1, a2, a) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " for " ^ " in range(" ^ ( String.make (num_ident*spaces) ' ' ) ^ " string_of_expr a1 " ^ " , " ^ ( String.make (num_ident*spaces) ' ' ) ^ " string_of_expr a2 " ^ " ) ^ " ; "
  | P_ForEach(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( String.make (num_ident*spaces) ' ' ) ^ " in " ^ ( String.make (num_ident*spaces) ' ' ) ^ " let " ^ ( String.make (num_ident*spaces) ' ' ) ^ " in "
  | P_Return(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " return " ^ string_of_expr expr ^ " ; "
  | P_While(expr) ->
    ( String.make (num_ident*spaces) ' ' ) ^ " while " ^ string_of_expr expr ^ " do "
  | P_Decl(d) -> string_of_normal_decl num_ident d
let compile program =
String.concat "" (List.map string_of_program(stmt program)) 
"main()"

Listing 9: LFLA.ml

open Printf

exception Usage of string

let (=) =
let (in_file, out_file) =
if Array.length Sys.argv == 2 then
  (Sys.argv.(1), "a.out")
else if (Array.length Sys.argv == 4) && (Sys.argv.(2) = "-o") then
  (Sys.argv.(1), Sys.argv.(3))
else raise (Usage("usage: ./LFLA [filename] or ./LFLA [filename] -o [output]
"))
in
let s_length = String.length in_file in
if (String.sub in_file (s_length-3) 3) <> ".la" then
  raise (Usage("input file should have format filename.la"))
else
  (* let length = String.length in_file in *)
  let lexbuf = Lexing.from_channel (open in in_file) in
  (* let in_file_bytes = Bytes.of_string in_file in *)
  (* let out_file = (Bytes.sub_string in_file_bytes 0 (length-2)) "+py" in *)
  let program = Parser.program Scanner.token lexbuf in
  let python_program = Translate.translate program in
  let pyFile = open_out_out_file in
    fprintf pyFile "%s\n" "#!/usr/bin/python"
    fprintf pyFile "%s\n" "import sys"
    fprintf pyFile "%s\n" "sys.path.append('lib')"
    fprintf pyFile "%s\n" "from InSpace import *
    fprintf pyFile "%s\n" "from AffSpace import *
    fprintf pyFile "%s\n" "from Core import *
    fprintf pyFile "%s\n" (Compile.compile python_program)
    close_out pyFile
    Sys.command ("chmod +x " "out_file");