A graph language.

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1 Lexical Elements

1.1 Identifiers

Identifiers are strings used to name variables and functions. The first character of an identifier must be a letter. Identifiers can contain lowercase letters, uppercase letters, digits, and the underscore character \_\_. Identifiers are case-sensitive.

1.2 Keywords

The following keywords are part of dots itself, and as such cannot be used as identifiers:

\texttt{return break continue def for while if else in dict list num bool string graph node INF true false null}

1.3 Literals

Literals are raw numeric or string values. The compiler will automatically determine the type of a literal, unless it is explicitly cast.

1.3.1 String literals

String literals are sequences of characters wrapped in double quotes. They may include any characters but some characters must be represented by escape sequences:

\begin{verbatim}
\texttt{\backslash backslash}
\texttt{\" double quote}
\texttt{\n newline}
\texttt{\r carriage return}
\texttt{\t horizontal tab}
\texttt{\v vertical tab}
\end{verbatim}

For an example, see section 2.1.2 on the string type.

1.3.2 Number literals

Number constants consist of an optional negative sign, an optional sequence of digits, an optional decimal point, and another optional sequence of digits. The second sequence of digits requires the presence of the decimal point. Either the first or second sequence of digits must appear (both is also valid).

1.3.3 Separators

Separators separate tokens. Whitespace characters (', \n, \t\text{etc.}) are separators, but not tokens. The other separators are single-character tokens. They are:

( ) [ ] { } ; , . < >
1.4 Whitespace

In d.o.t.s. whitespace is defined as any of the special characters \r, \n, and \t as well as the character obtained by pressing the spacebar. Whitespace is generally ignored and used as a token delimiter, except for within string literals.

2 Data Types

2.1 Primitive Types

2.1.1 num

The num data type represents all numbers in d.o.t.s. There is no distinction between the traditional data types of int and float from C, which means for example that there is no difference between the values 5 and 5.0. The comparative ordering of nums is the same as that of numbers in mathematics.

```
num x = 5;
num y = 5.0;
num z = x;
num q = 3.14159;
num a, b, c;
```

Listing 1: Declaration of “num” types.

In Listing 1 variables a, b, c, x, y, z, and q are all of the type num. Variables x, y, and z store equivalent values. Variables a, b, and c are all equal to null.

2.1.2 string

A string is a sequence of 0 or more characters. Comparative ordering of strings is determined sequentially by comparing the ASCII value of each character in the two strings from left to right.

```
string a = "alpha";
string empty = "";
string char = "a";
string escape_sequence_example = "And he said, \"Look at this! I have quotes inside my string!\nAnd a newline too!\"";
```

Listing 2: Declaration of “string” types.

2.1.3 bool

The bool type is a logical value which can be either the primitive values true or false or an expression which evaluates to those literals.

```
bool t = true;
bool f = false;
```

Listing 3: Declaration of “bool” types.
2.2 Node and Graph Objects

A node object represents a single vertex in a Graph, and a graph object represents a collection of graphs (which can be empty). *Note:* A node is a graph, but a graph is not a node.

Recursive definition of graph objects:

- An empty graph is a graph.
- A node is a graph.
- A graph added to a graph is a graph.
- A graph subtracted from a graph is a graph.

A graph contains only the field vertices, which is a list of all node objects contained within the graph.

A node contains the fields value, in, out. Internally, a node is uniquely identified by an id number set by the compiler, but this distinction is invisible to the programmer. The value field is a string object, and simply represents some value that the node contains. One possible use of the value field is to allow users to assign a more semantic meaning to nodes (ex. setting the value to the name of a city). The in field is a dict mapping nodes that the current node has edges into to weights. Similarly, the out field is a dict mapping nodes that have edges into the current node to weights. The keys of the two dicts are nodes. An example of accessing the in and out dicts of a node can be seen in Listing 7.

Since node has an *is-a* relationship with graph, it also contains a vertices field, but this is set upon declaration to contain only the node itself, and cannot be altered by the user.

Nodes can be declared in two different ways. In the first, the variable can simply be declared with the node keyword and a variable name. This creates a basic node with an empty value, in_list, and out_list. In the second manner, a node can be declared by giving it an initial value inside parentheses after the variable name (as seen in line 2 of Listing 4). Alternatively, a declared variable can be initialized with the assignment operator “=” to any object of the type node.

As with all other types, graphs can be assigned at the same time as declaration or assigned later. A graph can be assigned any expression that evaluates to something of the type graph. There is also a special graph-creation syntax that can only be used at declaration time of a graph object (as seen in lines 6-9 of Listing 4). This special syntax consists of a comma-separated list of nodes and/or node operations (an example of this syntax can be found in lines 26-32 of Listing 7). Each node referenced in this type of assignment must have been previously declared.

```plaintext
node x;
node y("nyc");

graph g1;
graph g2 = g1;
graph g3 = {
    x,
    y
}; # special graph assignment syntax only available at declaration time
```

Listing 4: Declaration of “node” and “graph” objects.

3 Expressions and Operators

A compound expression has at least one operand and at least one operator. Operators have types including constants, variables, and functions that return values. For example:
3.1 Number and String Operators

Operators are special symbols that are used to perform actions on operands. An operand can be a function, variable, or literal. **Numerical operators** are either arithmetic or comparative operators that operate on the `num` data type.

*Arithmetic Operators*

Arithmetic Operators function exactly like C with primitive data types such as literals, variables and functions. d.o.t.s supports the addition, subtraction, multiplication, division and modular division operators. Similar to C, integer division truncates the resulting value. Ex. `5 / 3 = 1`. Modular division returns the remainder of a given division. Ex. `5 % 3 = 2`

*Comparative Operators*

These operators relate two operands to each other. Some sample comparisons include:

```plaintext
#operators: >,<=,!=, <, ==, >=, ||, &&
3 == 4;  # returns false
(x && 3) || z;  # if x and z are both false, returns false; else returns true
(foo && x)
```

All comparative operators function as they do in C as long as the operands are primitive data types, variables or functions. The result of a comparison operation is a boolean.

3.2 Node Operators

The node operators outlined in Table 1 below are all binary operators which take a node object on the left-hand and right-hand sides of the operator. (Basic Form: `node_var node_op node_var`
<table>
<thead>
<tr>
<th>Operator</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>--</td>
<td>Add undirected edge with no weights between the 2</td>
</tr>
<tr>
<td>--&gt;&lt;</td>
<td>Add directed edge from left node to right node with no weight</td>
</tr>
<tr>
<td>--[num]</td>
<td>Add an undirected edge between 2 nodes with weight num in both directions</td>
</tr>
<tr>
<td>--&gt;&lt;[num]</td>
<td>Add a directed edge from the left node to the right node with weight num</td>
</tr>
<tr>
<td>[num]--[num]</td>
<td>Add edge from left to right with the weight in the right set of brackets, and an edge from right to left with the weight in the left set of brackets</td>
</tr>
</tbody>
</table>

==
Returns whether the internal ids of 2 nodes match

!=
Returns whether the internal ids of 2 nodes do not match

Table 1: Node Operators

![Example Graph showing nodes with different weights and edges.](image)

Figure 1: Example Graph showing nodes with different weights and edges.

```plaintext
node X, Y, Z, Q, R;
X -- Y;
Y -- [.3] Z;
Z -- Q;
Q -- [45] R;
R [.87]-- [.39] X;
R == Q;  # returns false
R != Q;  # returns true
/* accessing edge lists: */
```
3.3 Graph Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>-</td>
<td>Returns a new graph object with the left-hand side graph without any connections dictated on the right-hand side</td>
</tr>
<tr>
<td>+</td>
<td>Returns a graph that contains all of the graphs in the left-hand and right-hand graph</td>
</tr>
<tr>
<td>+=</td>
<td>Adds the graph on the right-hand side of the operator to the graph on the left-hand side.</td>
</tr>
<tr>
<td>-=</td>
<td>Removes the graph on the right-hand side of the operator from the graph on the left-hand side.</td>
</tr>
<tr>
<td>==</td>
<td>Returns whether the two graphs contain the same nodes.</td>
</tr>
</tbody>
</table>

Table 2: Graph Operators

There are two logical operators: == and !=. The first evaluates to true if the left and right-hand operands are equal, while the second evaluates to true if the left and right-hand operands are not equal.

The logical operators == and != are the only logical operators which function on graph operands. Two graph objects are equal if their vertices fields contain the same set of node objects.
3.4 Subscript Notation

3.4.1 Subscript

A subscript is indicated by an id followed by an argument enclosed in brackets. The only two data types which can be subscripted are lists and dicts.

Dict objects are subscripted using a key. The notation D[i], where D is a dict returns the value stored in the dictionary at the key i, where i is evaluated if it it’s a variable. The type of the key used in a dict subscript must be of the same type as that particular dict object’s key type.

List objects are subscripted using an index. The notation L[i] returns the value stored in the list at position/index i. i must evaluate to an integer.

3.5 Operator Precendence

Operator precedence follows traditional mathematical order of operations: parenthesis, exponent, multiply, divide, addition, subtraction

3.6 Member Access

The “.” character, when not part of a num literal, allows access to members of a data type or variable

3.7 Control Flow Statements

In regular expression terms, if / else if* / else? conditional statements are supported, where * represents the Kleene star operator, and “?” means 0 or 1 instances. Semantically, this means you can have if {} statements, if {} else statements, if {} else if {} ...., and if {} else if {} .... else {} statements. Within each “{“ is a statement (which could be the empty statment or a block of expressions, etc.).
if condition {
  /* execute when condition is true */
} else if another_condition {
  /* if another_condition is true go here */
} else if yet_another_condition {
  /* only reached if another_condition is false
  go here if yet_another_condition is true */
} else {
  /* execute when all conditions are false */
} if condition {
  /* execute if condition is true */
} /* continue executing subsequent expression statements */

3.8 Loop Statements

d.o.t.s. supports while and for loops.

3.8.1 While Loops

while statements execute repeatedly the code in the scoped block (delimited by braces following the Boolean expression), while the boolean expression condition evaluates to true.

while condition {
  /* code */
}

3.8.2 For Loops

for statements can only be used on the iterable types list and dict. A for statements iterates through all elements in iterable_var, assigning the current element to var_name. For dicts: the data type of var_name is automatically set to the type of the dict’s keys, and the dict’s keys are iterated over. For lists, the data type of var_name is automatically set to the type of the list, and the elements of the list are iterated over.

for var_name in iterable_var {
  /* code */
}

/* common usage examples */
for node_var in graph_var {
  /* do something with each node */
}
for edge_var in n.out {
  /* do something with each outbound edge from node n */
}

3.9 Other Statements

3.9.1 Break

Used in a loop to exit out of the loop immediately. Continue executing expressions after the loop block as expected.

```bash
num i = 0;
while i < 5 {
  i = i + 1;
  if i == 3 {
    break;
  }
  print(i, " ");
}
/* Prints 1 2 */
print(i, " ");
/* Prints 2 */
```

3.9.2 Continue

Used in a loop to skip the rest of the loop block and execute the next iteration of the loop.

```bash
num i = 0;
while i < 5 {
  i = i + 1;
  if i == 2 {
    continue;
  }
  print(i, " ");
}
/* Prints 1 3 4 5 */
```

3.9.3 Return

Used to exit from a function and dictate the output argument. The output argument must be the same type as specified in the function header. If not, the compiler will throw an error.

```bash
def num foo(num n) {
  if n > 2 {
    return 2;
  }
  return 1;
}

num out1 = foo(10)
print(out1);
```
4 Functions

4.1 Function Declaration and Definition

Before a function can be used, it must be declared and defined. Functions are declared using the `def` keyword, followed by the data type the function will return, followed by the function name, followed by a list of parameters enclosed in parentheses. The function must then be immediately defined within a set of curly braces immediately following the parentheses of the parameter list.

```
* Outline of function declaration and definition.
* `return_type` would be a data type.
*
def return_type function_name () {
  /* function implementation code */
}
```

Listing 9: Function declaration and definition.

4.2 Return Statements

Each function must return a value that matches the declared return type using the `return` keyword. For functions with the `null` return type, indicating that nothing is returned by the function, the return statement can consist either of the keyword `return` as an expression by itself (line 2 of Listing 10), or it can explicitly `return null` (line 6 of Listing 10).

```
def null fnull1 () {
  return;
}
def null fnull2 () {
  return null;
}
def int fint () {
  return 4;
}
```

Listing 10: Return statements of functions.

4.3 Parameter List

The declaration of a function must include a list of required parameters enclosed within parentheses. To define a function which requires no parameters, the contents of the parentheses can be left blank. Otherwise, each parameter requires the data type, followed by a variable name by which the parameter can be referenced within the function definition.
def null no_params () {
    return;
}

def num one_param (num x) {
    num b = x;
    return b;
}

def string multi_params (string s1, num y, string s2) {
    string statement = s1 + " " + " " + y + "s2";
    return statement;
}

Listing 11: Parameters in function declarations.

4.4 Calling Functions

The syntax for calling a function is: the name of the function, followed by a comma-separated list of values or variables to be used in parameter list enclosed within parentheses. Each value or variable passed in to a function call is mapped to the corresponding variable in the declared parameter list of the function.

A function-call expression is considered of the same type as its return type. Because of this, function-call expressions may be used as any other expression. For example a function-call expression can be used in the assignment of variables, as in line 11 of Listing 12.

def num increment (num n, num incr) {
    return n + incr;
}

num x = 4;

\* The following call maps `'x'` to the variable `'n'`, 
* and `'2'` to the variable `'incr'` from the declaration 
* of the `'increment'` function
\*
num y = increment(x, 2);

print("y: ", y); # prints --&gt; `'y: 6'`

Listing 12: Function declaration and definition.

4.5 Variable Length Parameter Lists

The only function in d.o.t.s. that can have a variable number of parameters is the built-in print function. All other functions must be declared with a defined absolute number of 0 or more parameters.

The print function may be called using a comma-separated list of expressions which can be evaluated as or converted to the string type. Each of the built-in types may be used directly as an argument to the print function.

string alpha = "World";
print("Hello", alpha, "\n");
4.6 Built-in Functions

d.o.t.s. comes with two pre-defined functions.
The first, print(...), prints the string representation of a list of expressions to standard output.
The second, range(num min, num max), returns a list <num> consisting of the integers from min to max-1. The arguments to range must be integers.

5 Program Structure and Scope

5.1 Program Structure

A d.o.t.s. program consists of a series of function declarations and expressions. Because d.o.t.s. is a scripting language, there is no main function. Instead, expressions are executed in order from top to bottom. Functions must be declared and defined before use.

5.2 Scope

In d.o.t.s., variables declared in expressions not belonging to functions or for loops have scope outside of function definitions. Variables declared in a function are visible or available to be referenced by name within the body of the function (functional scoping). Variables declared in for loop expressions can be referenced by name within the loop body (lexical scoping). There is no true global scoping as programs are executed from top to bottom. Variable declarations within functions and for loops can mask variables declared outside.
In Listing 15, the declaration of \texttt{n} in the loop scope masks the declaration of \texttt{n} from the top level scope.

## 6 Sample Program

In this section, we demonstrate how two simple path-searching algorithms can be implemented using d.o.t.s.'s syntax. The end-goal of our project is to be able to implement more complex algorithms. But for the purposes of demonstration, we chose to show Dijkstra's Algorithm (Listing 16) and the Breadth-First Search algorithm (Listing 17), as their implementation make use of each collection type and control-flow statement.

**Listing 15: Example of masking**

```plaintext
\* prints
Goodbye world ya ya ya
cool ya ya ya\*
print(n);
\* prints Hello world \*
```

**Listing 16: Dijkstra's Algorithm**

```plaintext
\* Dijkstra’s algorithm: calculates shortest paths starting
* from the source node and returns a dict of the lowest cost
* to destination nodes
*\

\def \dict\langle\node, \num\rangle \relax (\node \u, \dict\langle\node, \num\rangle \w) \{ 
  \for \node \v \in \u.out \{
    \if \w[\v] > \u.out[\v] \{
      \w[\v] = \u.out[\v];
    \}
  \}
  \return \w;
\}

\def \dict\langle\node, \num\rangle \dijkstra (\graph \G, \node \source)\{ 
  \dict\langle\node, \num\rangle \S, \Q;
  \for \node \n \in \G:\n    \Q[\n] = \INF;
    \Q[\source] = 0;
  \while !isEmpty(\Q) \{
    \node \u = min(\Q);
    \num \w = \Q[\u];
    \Q.remove(\u);
    \S[\u] = \w;
    \Q = \relax(\u, \Q);
  \}
  \return \S;
\}
```

**Listing 17: Breadth-First Search with source and dest**

```plaintext
\* Breadth-First-Search with source and dest\*
```
def list<node> bfs(graph G, node source, node dest) {
    list<node> visited = [source];
    dict<node, node> parents;

    node curr;
    bool found = false;
    while !isEmpty(visited) {
        curr = visited.dequeue();
        if curr == dest {
            found = true;
            break;
        }

        for node child in curr.out {
            if !(child in visited) {
                visited.enqueue(child);
                parents[child] = curr;
            }
        }
    }

    if !found {
        return [];
    }

    /* reconstruct path */
    list<node> path = [curr];
    while (curr in parents && parents[curr] != null) {
        path.enqueue(parents[curr]);
        curr = parents[curr];
    }
    return path;
}

Listing 17: Breadth-First Search Algorithm

Now that we have defined the bfs and dijkstra functions, we can use them to find shortest paths in an actual instance of a graph.
Figure 2: Visual representation of graph created in Listing 18.

Listing 18: Using user-defined functions.