## Lecture 3, COMS E6998-3: Discriminative Dependency Parsing

Michael Collins

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#### Projects

- First deadline: 1 page project proposal by 5pm, Friday
  February 11th
- The choice of project is up to you, but it should be clearly related to the course material
- Example projects:
  - Design and implementation of a machine-learning model for some NLP task; the write-up would describe the technical details of the model, as well as experimentation with the model on some dataset
  - Implementation of an approach (or approaches) described in one or more papers in the research literature
  - Possibly also purely "theoretical" projects (no experimentation), although these projects will be less common

Group projects are allowed (up to a maximum of 3 people)

We'll expect a 6 page write-up for 1 person projects, 8 pages for 2 person projects, 10 pages for 3 people.

#### Unlabeled Dependency Parses



root is a special root symbol

 Each dependency is a pair (j, k) where j index of a head word, k is the index of a modifier word. In the figures, we represent a dependency (j, k) by a directed edge from word j to word k

▶ Dependencies in the above example are (0,2), (2,1), (2,4) and (4,3). (We take 0 to be the root symbol.)

All Dependency Parses for John saw Mary



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#### Conditions on Dependency Structures



- The dependency arcs form a *directed tree*, with the root symbol at the root of the tree.
- There are no "crossing dependencies".
  Dependency structures with no crossing dependencies are sometimes referred to as **projective** structures.

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#### Notation for Dependency Structures

- Assume  $\underline{x}$  is a sequence of words  $x_1 \dots x_m$
- A dependency structure is a vector y
- ► First, define the *index set* I to be the set of all possible dependencies. For example, for m = 3,

 $\mathcal{I} = \{(0,1), (0,2), (0,3), (1,2), (1,3), (2,1), (2,3), (3,1), (3,2)\}$ 

- ► Then y is a vector of values y(j, k) for all (j, k) ∈ I. y(j, k) = 1 if the structure contains the dependency (j, k), y(j, k) = 0 otherwise.
- $\blacktriangleright$  We use  $\mathcal Y$  to refer to the set of all possible well-formed vectors  $\underline y$

#### Feature Vectors for Dependencies

•  $\underline{\phi}(\underline{x},j,k)$  is a feature vector representing dependency (j,k) for sentence  $\underline{x}$ 

- Example features:
  - Identity of the words  $x_j$  and  $x_k$
  - The part-of-speech tags for words  $x_j$  and  $x_k$
  - The distance between  $x_j$  and  $x_k$
  - Words/tags that surround  $x_j$  and  $x_k$
  - etc. etc.

#### CRFs for Discriminative Dependency Parsing

- ▶ We use  $\underline{\Phi}(\underline{x},\underline{y}) \in \mathbb{R}^d$  to refer to a feature vector for an *entire* dependency structure y
- ▶ We then build a log-linear model, very similar to a CRF

$$p(\underline{y}|\underline{x};\underline{w}) = \frac{\exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x},\underline{y})\right)}{\sum_{\underline{y}' \in \mathcal{Y}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x},\underline{y}')\right)}$$

• How do we define  $\underline{\Phi}(\underline{x}, \underline{y})$ ? Answer:

$$\underline{\Phi}(\underline{x},\underline{y}) = \sum_{(j,k)\in\mathcal{I}} y(j,k)\underline{\phi}(\underline{x},j,k)$$

where  $\phi(\underline{x},j,k)$  is the feature vector for dependency (j,k)

### Decoding

► The decoding problem: find

$$\arg \max_{\underline{y} \in \mathcal{Y}} p(\underline{y}|\underline{x}; \underline{w}) = \arg \max_{\underline{y} \in \mathcal{Y}} \frac{\exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})\right)}{\sum_{\underline{y}' \in \mathcal{Y}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y}')\right)}$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})\right)$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}} \underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}} \underline{w} \cdot \sum_{(j,k) \in \mathcal{I}} y(j,k) \underline{\phi}(\underline{x}, j, k)$$
$$= \arg \max_{\underline{s} \in \mathcal{Y}} \sum_{(j,k) \in \mathcal{I}} y(j,k) \left(\underline{w} \cdot \underline{\phi}(\underline{x}, j, k)\right)$$

• This problem can be solved using dynamic programming, in  $O(m^3)$  time, where m is the length of the sentence

#### Parameter Estimation

- ► To estimate the parameters, we assume we have a set of n labeled examples, {(<u>x</u><sup>i</sup>, <u>y</u><sup>i</sup>)}<sub>i=1</sub><sup>n</sup>. Each <u>x</u><sup>i</sup> is an input sequence x<sup>i</sup><sub>1</sub>...x<sup>i</sup><sub>m</sub>, each <u>y</u><sup>i</sup> is a dependency structure (i.e., y<sup>i</sup>(j, k) = 1 if the i'th structure contains a dependency (j, k)).
- ▶ We then proceed in exactly the same way as for CRFs
- The regularized log-likelihood function is

$$L(\underline{w}) = \sum_{i=1}^{n} \log p(\underline{y}^{i} | \underline{x}^{i}; \underline{w}) - \frac{\lambda}{2} ||\underline{w}||^{2}$$

The parameter estimates are

$$\underline{w}^* = \arg\max_{\underline{w}\in\mathbb{R}^d} \quad \sum_{i=1}^n \log p(\underline{y}^i | \underline{x}^i; \underline{w}) - \frac{\lambda}{2} ||\underline{w}||^2$$

#### Finding the Maximum-Likelihood Estimates

- $\blacktriangleright$  We'll again use gradient-based optimization methods to find  $\underline{w}^*$
- ▶ How can we compute the derivatives? As before,

$$\frac{\partial}{\partial w_l} L(\underline{w}) = \sum_i \Phi_l(\underline{x}^i, \underline{y}^i) - \sum_i \sum_{\underline{y} \in \mathcal{Y}} p(\underline{y} | \underline{x}^i; \underline{w}) \Phi_l(\underline{x}^i, \underline{y}) - \lambda w_l$$

The first term is easily computed, because

$$\sum_{i} \Phi_{l}(\underline{x}^{i}, \underline{y}^{i}) = \sum_{i} \sum_{(j,k)\in\mathcal{I}} y^{i}(j,k)\phi_{l}(\underline{x}^{i}, j, k)$$

► The second term involves a sum over 𝒴, and because of this looks nasty...

# Calculating Derivatives using Dynamic Programming

We now consider how to compute the second term:

$$\sum_{\underline{y}\in\mathcal{Y}} p(\underline{y}|\underline{x}^{i};\underline{w}) \Phi_{l}(\underline{x}^{i},\underline{y}) = \sum_{\underline{y}\in\mathcal{Y}} p(\underline{y}|\underline{x}^{i};\underline{w}) \sum_{(j,k)\in\mathcal{I}} y(j,k) \phi_{l}(\underline{x}^{i},j,k)$$
$$= \sum_{(j,k)\in\mathcal{I}} q^{i}(j,k) \phi_{l}(\underline{x}^{i},j,k)$$

where

$$q^i(j,k) = \sum_{\underline{y} \in \mathcal{Y}: y(j,k) = 1} p(\underline{y} | \underline{x}^i; \underline{w})$$

(for the full derivation see the notes)

▶ For a given i, all q<sup>i</sup>(j,k) terms can be computed simultaneously in O(m<sup>3</sup>) time using dynamic programming.

#### Non-Projective Dependency Parsing



- We can also consider *non-projective* dependency parses, where crossing dependencies are allowed
- ► Define  $\mathcal{Y}_{np}$  to be the set of all non-projective dependency parses
- ► Each dependency parse <u>y</u> ∈ Y<sub>np</sub> is a vector of values y(j, k) for all (j, k) ∈ I. y(j, k) = 1 if the structure contains the dependency (j, k), y(j, k) = 0 otherwise.

#### An Example from Czech



He is mostly not even interested in the new things and in most cases, he has no money for it either.

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#### (figure taken from McDonald et al, 2005)

#### CRFs for Non-Projective Structures

- ▶ We use  $\underline{\Phi}(\underline{x},\underline{y}) \in \mathbb{R}^d$  to refer to a feature vector for an *entire* dependency structure y
- ▶ We then build a log-linear model, very similar to a CRF

$$p(\underline{y}|\underline{x};\underline{w}) = \frac{\exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x},\underline{y})\right)}{\sum_{\underline{y}' \in \mathcal{Y}_{np}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x},\underline{y}')\right)}$$

• How do we define  $\underline{\Phi}(\underline{x}, \underline{y})$ ? Answer:

$$\underline{\Phi}(\underline{x},\underline{y}) = \sum_{(j,k) \in \mathcal{I}} y(j,k) \underline{\phi}(\underline{x},j,k)$$

where  $\underline{\phi}(\underline{x}, j, k)$  is the feature vector for dependency (j, k)Only change from projective parsing: we've replaced the set of projective parses  $\mathcal{Y}$ , with the set of non-projective parses,  $\mathcal{Y}_{np}$ 

#### Decoding in Non-Projective Models

▶ The decoding problem: find

$$\arg \max_{\underline{y} \in \mathcal{Y}_{np}} p(\underline{y} | \underline{x}; \underline{w}) = \arg \max_{\underline{y} \in \mathcal{Y}_{np}} \frac{\exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})\right)}{\sum_{\underline{y}' \in \mathcal{Y}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y}')\right)}$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}} \exp\left(\underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})\right)$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}_{np}} \underline{w} \cdot \underline{\Phi}(\underline{x}, \underline{y})$$
$$= \arg \max_{\underline{y} \in \mathcal{Y}_{np}} \underline{w} \cdot \sum_{(j,k) \in \mathcal{I}} y(j,k) \underline{\phi}(\underline{x}, j, k)$$
$$= \arg \max_{\underline{s} \in \mathcal{Y}_{np}} \sum_{(j,k) \in \mathcal{I}} y(j,k) \left(\underline{w} \cdot \underline{\phi}(\underline{x}, j, k)\right)$$

Only change from projective parsing: we've replaced the set of projective parses  $\mathcal{Y}$ , with the set of non-projective parses,  $\mathcal{Y}_{np}$ 

Decoding in Non-Projective Parsing Models: the Chu-Liu-Edmonds Algorithm



(figure and example from McDonald et al, 2005)

Goal is to find the highest scoring directed spanning tree

### Step 1

► For each word, find the highest scoring incoming edge:



(figure from McDonald et al 2005)

- If the result of this step is a tree, we have the highest scoring spanning tree
- If not, we have at least one cycle. Next step is to pick a cycle, and *contract* the cycle

#### The Result of Contracting the Cycle



- We merge John and saw (the words in the cycle) into a single node c
- The weight of the edge from c to Mary is 30 (because the weight from John to Mary is 3, and from saw to Mary is 30: we take the highest score)
- See McDonald et al 2005 (posted on the class website, under *lectures*) for how the weights from *root* to *c* and *Mary* to *c* are calculated
- ▶ Having created the new graph, we then recurse (return to step 1)

# Step 1 (again)

► For each word, find the highest scoring incoming edge:



- If the result of this step is a tree, we have the highest scoring spanning tree
- This time we have a tree, and we're done (if not, we would repeat step 2 again)
- Retracing the steps taken in contracting the cycle allows us to recover the highest scoring tree:



### Efficiency

► A naive implementation takes O(n<sup>3</sup>) time (n is the number of nodes in the graph, i.e., the number of words in the input sentence)

 $\blacktriangleright$  An improved implementation takes  $O(n^2)$  time

#### Estimating the Parameters

Again, we can choose the parameters that maximize

$$L(\underline{w}) = \sum_{i=1}^{n} \log p(\underline{y}^{i} | \underline{x}^{i}; \underline{w}) - \frac{\lambda}{2} ||\underline{w}||^{2}$$

where  $\{(\underline{x}^i,\underline{y}^i)\}_{i=1}^n$  is the training set

 The gradients can again be calculated efficiently (for example, see Koo, Globerson, Carreras, and Collins, EMNLP 2007)