# Lecture 10: Discriminative Training for MT/ the Brown et al. Word Clustering Algorithm

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#### Discriminative Training for MT

Our original model:

$$f(y) = h(e(y)) + \sum_{k=1}^{L} g(p_k) + \sum_{k=1}^{L-1} \eta \times \delta(t(p_k), s(p_{k+1}))$$

► A discriminative model for translation (Liang et al., 2006):

$$f(y;\underline{w},\alpha,\eta) = \alpha \times h(e(y)) + \sum_{k=1}^{L} \underline{w} \cdot \underline{\phi}(p_k) + \sum_{k=1}^{L-1} \eta \times \delta(t(p_k), s(p_{k+1}))$$

Here  $\alpha \in \mathbb{R}, \, \eta \in \mathbb{R}$  and  $\underline{w} \in \mathbb{R}^d$  are the parameters of the model

 $\blacktriangleright$  Crucial idea:  $\underline{\phi}(p)$  is a feature-vector representation of a phrase p

#### The Learning Set-up

- ► Our training data consists of (x<sup>(i)</sup>, e<sup>(i)</sup>) pairs, for i = 1...n, where x<sup>(i)</sup> is a source language sentence, and e<sup>(i)</sup> is a target language sentence
- $\blacktriangleright$  We use  $\mathcal{Y}^{(i)}$  to denote the set of possible derivations for  $x^{(i)}$
- A complication: for a given (x<sup>(i)</sup>, e<sup>(i)</sup>) pair, there may be many derivations y ∈ Y<sup>(i)</sup> such that e(y) = e<sup>(i)</sup>.

#### A "Bold Updating" Algorithm from Liang et al.

• Initialization: set 
$$\underline{w} = 0$$
,  $\alpha = 1$ ,  $\eta = -1$ 

• 
$$z^* = \operatorname{arg} \max_{z \in \mathcal{Y}^{(i)}} f(z; \underline{w}, \alpha, \eta)$$

• For any phrase 
$$p \in y^*$$
,  $\underline{w} = \underline{w} + \underline{\phi}(p)$ 

 $\blacktriangleright \ \, {\rm For \ any \ phrase} \ \, p\in z^* \text{,} \ \, \underline{w}=\underline{w}-\underline{\phi}(p)$ 

$$\blacktriangleright \ {\sf Set} \ \alpha = \alpha + h(e(y^*)) - h(e(z^*))$$

• Set 
$$\eta = \eta + \ldots - \ldots$$

## A "Local Updating" Algorithm from Liang et al.

▶ Initialization: set  $\underline{w} = 0$ ,  $\alpha = 1$ ,  $\eta = -1$ 

• for 
$$t = 1 \dots T$$
, for  $i = 1 \dots n$ ,

 Define N<sup>i</sup> to be the k highest scoring translations in Y<sup>(i)</sup> under f(y; w, α, η) (easy to generate N<sup>i</sup> using k-best search)

•  $y^*$  is member of  $N^i$  that is "closest" to  $e^{(i)}$ .

• 
$$z^* = \operatorname{arg\,max}_{z \in \mathcal{Y}^{(i)}} f(z; \underline{w}, \alpha, \eta)$$

- For any phrase  $p \in y^*$ ,  $\underline{w} = \underline{w} + \underline{\phi}(p)$
- For any phrase  $p \in z^*$ ,  $\underline{w} = \underline{w} \underline{\phi}(p)$

• Set 
$$\alpha = \alpha + h(e(y^*)) - h(e(z^*))$$

• Set 
$$\eta = \eta + \ldots - \ldots$$

#### The Brown Clustering Algorithm

- Input: a (large) corpus of words
- Output 1: a partition of words into word clusters
- ▶ Output 2 (generalization of 1): a hierarchichal word clustering

### Example Clusters (from Brown et al, 1992)

Friday Monday Thursday Wednesday Tuesday Saturday Sunday weekends Sundays Saturdays June March July April January December October November September August people guys folks fellows CEOs chaps doubters commies unfortunates blokes down backwards ashore sideways southward northward overboard aloft downwards adrift water gas coal liquid acid sand carbon steam shale iron great big vast sudden mere sheer gigantic lifelong scant colossal man woman boy girl lawyer doctor guy farmer teacher citizen American Indian European Japanese German African Catholic Israeli Italian Arab pressure temperature permeability density porosity stress velocity viscosity gravity tension mother wife father son husband brother daughter sister boss uncle machine device controller processor CPU printer spindle subsystem compiler plotter John George James Bob Robert Paul William Jim David Mike anyone someone anybody somebody feet miles pounds degrees inches barrels tons acres meters bytes director chief professor commissioner commander treasurer founder superintendent dean custodian liberal conservative parliamentary royal progressive Tory provisional separatist federalist PQ had hadn't hath would've could've should've must've might've asking telling wondering instructing informing kidding reminding bothering thanking deposing that the theat

head body hands eyes voice arm seat eye hair mouth

# A Sample Hierarchy (from Miller et al., NAACL 2004)

lawyer newspaperman stewardess toxicologist slang babysitter conspirator womanizer mailman salesman bookkeeper troubleshooter bouncer technician janitor saleswoman	1000001101000 1000011010010 1000011010010
mike Maytag Generali Gap Harley-Davidson Enfield genus Microsoft Ventritex Tractebel Synopsys WordPerfect	$\begin{array}{c} 1011011100100101011100\\ 101101100100101011101\\ 10101100100101011101\\ 10101100100101011110\\ 101011100100101011110\\ 1010111001001010111110\\ 1010111001001010111110\\ 10101110010010101101\\ 1010111001001010100\\ 1010111001001011000\\ 10101110010010110010\\ 10101100100101100101\\ 10101100100101100101\\ 10101100100101100101\\ 10101100100101100100\\ 10101100100010$
John Consuelo Jeffrey Kenneth Phillip WILLIAM Timothy Terrence Jerald Harold Frederic Wendell	$\begin{array}{c} 10111001000000000\\ 1011100100000001\\ 1011100100000010\\ 1011100100000001100\\ 1011100100000001101\\ 1011100100000000$

Table 1: Sample bit strings

#### The Formulation

- $\mathcal{V}$  is the set of all words seen in the corpus  $w_1, w_2, \ldots w_T$
- ► Say n(w, v) is the number of times that word w precedes v in our corpus. n(w) is the number of times we see word w.
- Say C: V → {1,2,...k} is a partition of the vocabulary into k classes
- ► The model:

$$p(w_1, w_2, \dots, w_T) = \prod_{i=1}^n p(w_i | C(w_i)) p(C(w_i) | C(w_{i-1}))$$

(note: C(w₀) is a special start state)
More conveniently:

$$\log p(w_1, w_2, \dots, w_T) = \sum_{i=1}^n \log p(w_i | C(w_i)) p(C(w_i) | C(w_{i-1}))$$

#### Measuring the Quality of C

How do we measure the quality of a partition C? (Taken from Percy Liang, MENG thesis, MIT, 2005):

$$\begin{aligned} \text{Quality}(C) &= \frac{1}{n} \sum_{i=1}^{n} \log P(C(w_i) | C(w_{i-1})) P(w_i | C(w_i)) \\ &= \sum_{w,w'} \frac{n(w,w')}{n} \log P(C(w') | C(w)) P(w' | C(w')) \\ &= \sum_{w,w'} \frac{n(w,w')}{n} \log \frac{n(C(w), C(w'))}{n(C(w))} \frac{n(w')}{n(C(w'))} \\ &= \sum_{w,w'} \frac{n(w,w')}{n} \log \frac{n(C(w), C(w'))n}{n(C(w))n(C(w'))} + \sum_{w,w'} \frac{n(w,w')}{n} \log \frac{n(w')}{n} \\ &= \sum_{c,c'} \frac{n(c,c')}{n} \log \frac{n(c,c')n}{n(c)n(c')} + \sum_{w'} \frac{n(w')}{n} \log \frac{n(w')}{n} \end{aligned}$$

#### The Final Equation

Define

$$P(c, c') = \frac{n(c, c')}{n}$$
  $P(w) = \frac{n(w)}{n}$   $P(c) = \frac{n(c)}{n}$ 

▶ Then (again from Percy Liang, 2005):

$$\begin{aligned} \text{Quality}(C) &= \sum_{c,c'} P(c,c') \log \frac{P(c,c')}{P(c)P(c')} + \sum_{w} P(w) \log P(w) \\ &= I(C) - H \end{aligned}$$

The first term I(C) is the mutual information between adjacent clusters and the second term H is the entropy of the word distribution. Note that the quality of C can be computed as a sum of mutual information weights between clusters minus the constant H, which does not depend on C. This decomposition allows us to make optimizations.

### A First Algorithm

- $\blacktriangleright$  We start with  $|\mathcal{V}|$  clusters: each word gets its own cluster
- Our aim is to find k final clusters
- We run  $|\mathcal{V}| k$  merge steps:
  - ► At each merge step we pick two clusters c<sub>i</sub> and c<sub>j</sub>, and merge them into a single cluster
  - We greedily pick merges such that

 $\mathsf{Quality}(C)$ 

for the clustering  $\boldsymbol{C}$  after the merge step is maximized at each stage

► Cost? Naive = O(|V|<sup>5</sup>). Improved algorithm gives O(|V|<sup>3</sup>): still two slow for realistic values of |V|

### A Second Algorithm

• Parameter of the approach is m (e.g., m = 1000)

► Take the top m most frequent words, put each into its own cluster, c<sub>1</sub>, c<sub>2</sub>, ... c<sub>m</sub>

For 
$$i = (m+1) \dots |\mathcal{V}|$$

- ► Create a new cluster, c<sub>m+1</sub>, for the *i*'th most frequent word. We now have m + 1 clusters
- ► Choose two clusters from c<sub>1</sub>...c<sub>m+1</sub> to be merged: pick the merge that gives a maximum value for Quality(C). We're now back to m clusters

• Carry out (m-1) final merges, to create a full hierarchy

Running time:  $O(|\mathcal{V}|m^2 + n)$  where n is corpus length

#### Name Tagging with Word Clusters and Discriminative Training

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BBN Technologies 10 Moulton Street Cambridge, MA 02138 szmiller@bbn.com At a recent meeting, we presented name-tagging technology to a potential user. The technology had performed well in formal evaluations, had been applied successfully by several research groups, and required only annotated training examples to configure for new name classes. Nevertheless, it did not meet the user's needs.

To achieve reasonable performance, the HMM-based technology we presented required roughly 150,000 words of annotated examples, and over a million words to achieve peak accuracy. Given a typical annotation rate of 5,000 words per hour, we estimated that setting up a name finder for a new problem would take four person days of annotation work – a period we considered reasonable. However, this user's problems were too dynamic for that much setup time. To be useful, the system would have to be trainable in minutes or hours, not days or weeks.

- 1. 2. 3. Tag + PrevTag
- Tag + CurWord
- Tag + CapAndNumFeatureOfCurWord
- 4. ReducedTag + CurWord
  - //collapse start and continue tags
- 5. Tag + PrevWord
- 6. Tag + NextWord
- 7. Tag + DownCaseCurWord
- 8. Tag + Pref8ofCurrWord
- 9. Tag + Pref12ofCurrWord
- 10. Tag + Pref16ofCurrWord
- 11. Tag + Pref20ofCurrWord
- Tag + Pref8ofPrevWord 12.
- Tag + Pref12ofPrevWord 13.
- 14. Tag + Pref16ofPrevWord
- 15. Tag + Pref20ofPrevWord
- 16. Tag + Pref8ofNextWord
- 17. Tag + Pref12ofNextWord
- Tag + Pref16ofNextWord 18.
- 19. Tag + Pref20ofNextWord

Table 2: Feature Set



