

# Fundamentals of Computer Systems

Thinking Digitally

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Spring 2016

# The Subjects of this Class

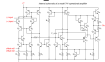
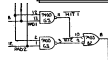
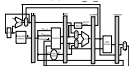
0

1

# Computer Systems Work Because of Abstraction



```
;; voice 1 wave select
ld a, (#CH1_W_NUM)
and a
ld a, (#CH1_W_SEL)
jr nz, #00b4
ld a, (#CH1_E_TABLE0)
```



Application Software

Operating Systems

Architecture

Micro-Architecture

Logic

Digital Circuits

Analog Circuits

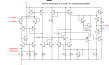
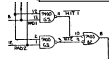
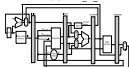
Devices

Physics

# Computer Systems Work Because of Abstraction



```
;; voice 1 wave select
ld      a, (#CH1_W_NUM)
and
ld      a, (#CH1_W_SEL)
jr      nz, #00b4
ld      a, (#CH1_E_TABLE0)
```



Application Software    COMS 3157, 4156, et al.

Operating Systems      COMS W4118

Architecture            Second Half of 3827

Micro-Architecture      Second Half of 3827

Logic                     First Half of 3827

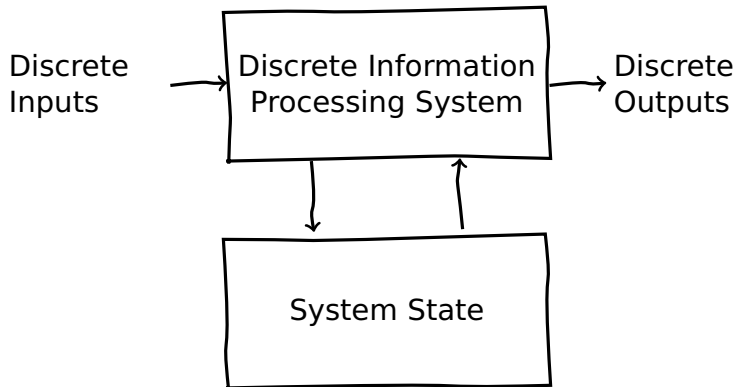
Digital Circuits         First Half of 3827

Analog Circuits         ELEN 3331

Devices                  ELEN 3106

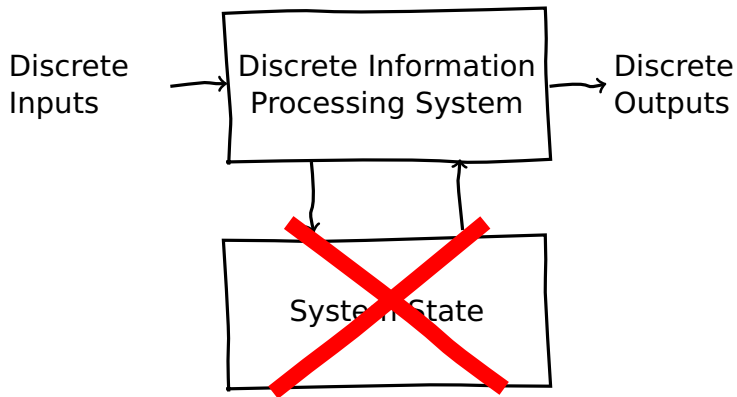
Physics                  ELEN 3106 et al.

# Simple information processing system

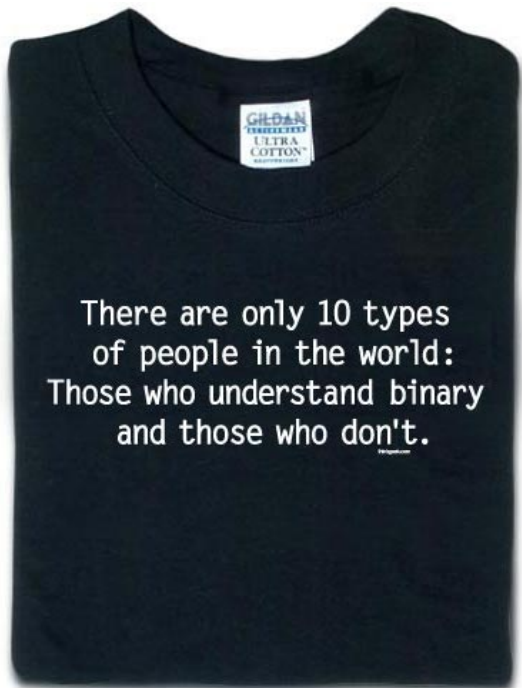


First half of the course

# Simple information processing system



First **quarter** of the course



thinkgeek.com

# The Decimal Positional Numbering System

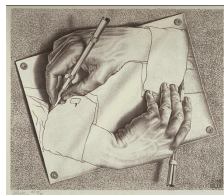


Ten figures: 0 1 2 3 4 5 6 7 8 9

$$7 \times 10^2 + 3 \times 10^1 + 0 \times 10^0 = 730_{10}$$

$$9 \times 10^2 + 9 \times 10^1 + 0 \times 10^0 = 990_{10}$$

Why base ten?



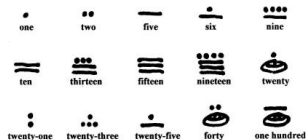


# Which Numbering System Should We Use?

## Some Older Choices:



Roman: I II III IV V VI VII VIII IX X



Mayan: base 20, Shell = 0

|    |           |    |            |    |             |    |              |    |               |    |                |
|----|-----------|----|------------|----|-------------|----|--------------|----|---------------|----|----------------|
| 1  | ∩         | 11 | ∩∩         | 21 | ∩∩∩         | 31 | ∩∩∩∩         | 41 | ∩∩∩∩∩         | 51 | ∩∩∩∩∩∩         |
| 2  | ∩∩        | 12 | ∩∩∩        | 22 | ∩∩∩∩        | 32 | ∩∩∩∩∩        | 42 | ∩∩∩∩∩∩        | 52 | ∩∩∩∩∩∩∩        |
| 3  | ∩∩∩       | 13 | ∩∩∩∩       | 23 | ∩∩∩∩∩       | 33 | ∩∩∩∩∩∩       | 43 | ∩∩∩∩∩∩∩       | 53 | ∩∩∩∩∩∩∩∩       |
| 4  | ∩∩∩∩      | 14 | ∩∩∩∩∩      | 24 | ∩∩∩∩∩∩      | 34 | ∩∩∩∩∩∩∩      | 44 | ∩∩∩∩∩∩∩∩      | 54 | ∩∩∩∩∩∩∩∩∩      |
| 5  | ∩∩∩∩∩     | 15 | ∩∩∩∩∩∩     | 25 | ∩∩∩∩∩∩∩     | 35 | ∩∩∩∩∩∩∩∩     | 45 | ∩∩∩∩∩∩∩∩∩     | 55 | ∩∩∩∩∩∩∩∩∩∩     |
| 6  | ∩∩∩∩∩∩    | 16 | ∩∩∩∩∩∩∩    | 26 | ∩∩∩∩∩∩∩∩    | 36 | ∩∩∩∩∩∩∩∩∩    | 46 | ∩∩∩∩∩∩∩∩∩∩    | 56 | ∩∩∩∩∩∩∩∩∩∩∩    |
| 7  | ∩∩∩∩∩∩∩   | 17 | ∩∩∩∩∩∩∩∩   | 27 | ∩∩∩∩∩∩∩∩∩   | 37 | ∩∩∩∩∩∩∩∩∩∩   | 47 | ∩∩∩∩∩∩∩∩∩∩∩   | 57 | ∩∩∩∩∩∩∩∩∩∩∩∩   |
| 8  | ∩∩∩∩∩∩∩∩  | 18 | ∩∩∩∩∩∩∩∩∩  | 28 | ∩∩∩∩∩∩∩∩∩∩  | 38 | ∩∩∩∩∩∩∩∩∩∩∩  | 48 | ∩∩∩∩∩∩∩∩∩∩∩∩  | 58 | ∩∩∩∩∩∩∩∩∩∩∩∩∩  |
| 9  | ∩∩∩∩∩∩∩∩∩ | 19 | ∩∩∩∩∩∩∩∩∩∩ | 29 | ∩∩∩∩∩∩∩∩∩∩∩ | 39 | ∩∩∩∩∩∩∩∩∩∩∩∩ | 49 | ∩∩∩∩∩∩∩∩∩∩∩∩∩ | 59 | ∩∩∩∩∩∩∩∩∩∩∩∩∩∩ |
| 10 | ∩         | 20 | ∩∩         | 30 | ∩∩∩         | 40 | ∩∩∩∩         | 50 | ∩∩∩∩∩         |    |                |

Babylonian: base 60

# Hexadecimal, Decimal, Octal, and Binary

| Hex | Dec | Oct | Bin  |
|-----|-----|-----|------|
| 0   | 0   | 0   | 0    |
| 1   | 1   | 1   | 1    |
| 2   | 2   | 2   | 10   |
| 3   | 3   | 3   | 11   |
| 4   | 4   | 4   | 100  |
| 5   | 5   | 5   | 101  |
| 6   | 6   | 6   | 110  |
| 7   | 7   | 7   | 111  |
| 8   | 8   | 10  | 1000 |
| 9   | 9   | 11  | 1001 |
| A   | 10  | 12  | 1010 |
| B   | 11  | 13  | 1011 |
| C   | 12  | 14  | 1100 |
| D   | 13  | 15  | 1101 |
| E   | 14  | 16  | 1110 |
| F   | 15  | 17  | 1111 |

# Binary and Octal



DEC PDP-8/I, c. 1968

| Oct | Bin |
|-----|-----|
| 0   | 000 |
| 1   | 001 |
| 2   | 010 |
| 3   | 011 |
| 4   | 100 |
| 5   | 101 |
| 6   | 110 |
| 7   | 111 |

$$\begin{aligned} \text{PC} &= 0 \times 2^{11} + 1 \times 2^{10} + 0 \times 2^9 + 1 \times 2^8 + 1 \times 2^7 + 0 \times 2^6 + \\ & 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ &= 2 \times 8^3 + 6 \times 8^2 + 7 \times 8^1 + 5 \times 8^0 \\ &= 1469_{10} \end{aligned}$$

# Hexadecimal Numbers

Base 16: 0 1 2 3 4 5 6 7 8 9 A B C D E F

Instead of groups of 3 bits (octal), Hex uses groups of 4.

$$\begin{aligned} \text{CAFEF00D}_{16} &= 12 \times 16^7 + 10 \times 16^6 + 15 \times 16^5 + 14 \times 16^4 + \\ &\quad 15 \times 16^3 + 0 \times 16^2 + 0 \times 16^1 + 13 \times 16^0 \\ &= 3,405,705,229_{10} \end{aligned}$$

|  |                                  |  |   |  |   |  |   |  |   |  |   |  |   |  |   |  |        |  |   |  |   |  |       |
|--|----------------------------------|--|---|--|---|--|---|--|---|--|---|--|---|--|---|--|--------|--|---|--|---|--|-------|
|  | C                                |  | A |  | F |  | E |  | F |  | 0 |  | 0 |  | D |  | Hex    |  |   |  |   |  |       |
|  | 11001010111111101111000000001101 |  |   |  |   |  |   |  |   |  |   |  |   |  |   |  | Binary |  |   |  |   |  |       |
|  | 3                                |  | 1 |  | 2 |  | 7 |  | 7 |  | 5 |  | 7 |  | 0 |  | 0      |  | 1 |  | 5 |  | Octal |

# Computers Rarely Manipulate True Numbers

Infinite memory still very expensive

Finite-precision numbers typical

32-bit processor: naturally manipulates 32-bit numbers

64-bit processor: naturally manipulates 64-bit numbers

How many different numbers can you

represent with 5 

|             |         |
|-------------|---------|
| binary      |         |
| octal       |         |
| decimal     | digits? |
| hexadecimal |         |

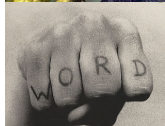
# Jargon



Bit Binary digit: 0 or 1



Byte Eight bits



Word Natural number of bits for the processor, e.g., 16, 32, 64



LSB Least Significant Bit (“rightmost”)



MSB Most Significant Bit (“leftmost”)

# Decimal Addition Algorithm

$$\begin{array}{r} 434 \\ +628 \\ \hline \end{array}$$

$$4 + 8 = 12$$

| +  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|----|----|----|----|----|----|----|----|----|----|----|
| 0  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 2  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 |
| 3  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 |
| 4  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 |
| 5  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 |
| 6  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| 7  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |

# Decimal Addition Algorithm

$$\begin{array}{r} 1 \\ 434 \\ +628 \\ \hline 2 \end{array}$$

$$4 + 8 = 12$$

$$1 + 3 + 2 = 6$$

| +  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|----|----|----|----|----|----|----|----|----|----|----|
| 0  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 2  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 |
| 3  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 |
| 4  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 |
| 5  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 |
| 6  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| 7  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |



# Decimal Addition Algorithm

$$\begin{array}{r} 1 \\ 434 \\ +628 \\ \hline 62 \end{array}$$

$$4 + 8 = 12$$

$$1 + 3 + 2 = 6$$

$$4 + 6 = 10$$

| +  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|----|----|----|----|----|----|----|----|----|----|----|
| 0  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 2  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 |
| 3  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 |
| 4  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 |
| 5  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 |
| 6  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| 7  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |

# Decimal Addition Algorithm

$$\begin{array}{r} 1\ 1 \\ 434 \\ +628 \\ \hline 062 \end{array}$$

$$4 + 8 = 12$$

$$1 + 3 + 2 = 6$$

$$4 + 6 = 10$$

| +  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|----|----|----|----|----|----|----|----|----|----|----|
| 0  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 2  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 |
| 3  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 |
| 4  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 |
| 5  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 |
| 6  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| 7  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |

# Decimal Addition Algorithm

$$\begin{array}{r} 1\ 1 \\ 434 \\ +628 \\ \hline 1062 \end{array}$$

$$4 + 8 = 12$$

$$1 + 3 + 2 = 6$$

$$4 + 6 = 10$$

| +  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|----|----|----|----|----|----|----|----|----|----|----|
| 0  | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 2  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 |
| 3  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 |
| 4  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 |
| 5  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 |
| 6  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| 7  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |

# Binary Addition Algorithm

$$\begin{array}{r} 10011 \\ +11001 \\ \hline \end{array}$$

$$1 + 1 = 10$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |

# Binary Addition Algorithm

$$\begin{array}{r} \phantom{0}1 \\ 10011 \\ +11001 \\ \hline 0 \end{array}$$

$$\begin{array}{l} 1 + 1 = 10 \\ 1 + 1 + 0 = 10 \end{array}$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |

# Binary Addition Algorithm

$$\begin{array}{r} \phantom{00}11 \\ 10011 \\ +11001 \\ \hline \phantom{00}00 \end{array}$$

$$\begin{aligned} 1 + 1 &= 10 \\ 1 + 1 + 0 &= 10 \\ 1 + 0 + 0 &= 01 \end{aligned}$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |

# Binary Addition Algorithm

$$\begin{array}{r} 011 \\ 10011 \\ +11001 \\ \hline 100 \end{array}$$

$$\begin{array}{l} 1 + 1 = 10 \\ 1 + 1 + 0 = 10 \\ 1 + 0 + 0 = 01 \\ 0 + 0 + 1 = 01 \end{array}$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |

# Binary Addition Algorithm

$$\begin{array}{r} 0011 \\ 10011 \\ +11001 \\ \hline 1100 \end{array}$$

$$\begin{array}{l} 1 + 1 = 10 \\ 1 + 1 + 0 = 10 \\ 1 + 0 + 0 = 01 \\ 0 + 0 + 1 = 01 \\ 0 + 1 + 1 = 10 \end{array}$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |



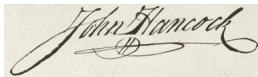
# Binary Addition Algorithm

$$\begin{array}{r} 10011 \\ 10011 \\ +11001 \\ \hline 101100 \end{array}$$

$$\begin{array}{l} 1 + 1 = 10 \\ 1 + 1 + 0 = 10 \\ 1 + 0 + 0 = 01 \\ 0 + 0 + 1 = 01 \\ 0 + 1 + 1 = 10 \end{array}$$

| +  | 0  | 1  |
|----|----|----|
| 0  | 00 | 01 |
| 1  | 01 | 10 |
| 10 | 10 | 11 |

# Signed Numbers: Dealing with Negativity

A rectangular image showing a handwritten signature in cursive script. The signature reads "John Hancock" and is written in dark ink on a light-colored, aged paper background. The signature is highly stylized, with large, sweeping loops and a prominent flourish at the end.

How should both positive and negative numbers be represented?

# Signed Magnitude Numbers

You are most familiar with this:  
negative numbers have a leading –

In binary, a  
leading 1 means  
negative:

$$0000_2 = 0$$

$$0010_2 = 2$$

$$1010_2 = -2$$

$$1111_2 = -7$$

$$1000_2 = -0?$$

Can be made to work, but addition is  
annoying:

If the signs match, add the magnitudes  
and use the same sign.

If the signs differ, subtract the smaller  
number from the larger; return the  
sign of the larger.

# One's Complement Numbers

Like Signed Magnitude, a leading 1 indicates a negative One's Complement number.

To negate a number, complement (flip) each bit.

$$0000_2 = 0$$

$$0010_2 = 2$$

$$1101_2 = -2$$

$$1000_2 = -7$$

$$1111_2 = -0?$$

Addition is nicer: just add the one's complement numbers as if they were normal binary.

Really annoying having a  $-0$ : two numbers are equal if their bits are the same or if one is 0 and the other is  $-0$ .



**NOT ALL  
ZEROS  
ARE CREATED  
EQUAL**

**ZERO CALORIES. MAXIMUM PEPSI™ TASTE.**



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## Two's Complement Numbers



Really neat trick: make the most significant bit represent a *negative* number instead of positive:

$$1101_2 = -8 + 4 + 1 = -3$$

$$1111_2 = -8 + 4 + 2 + 1 = -1$$

$$0111_2 = 4 + 2 + 1 = 7$$

$$1000_2 = -8$$

Easy addition: just add in binary and discard any carry.

Negation: complement each bit (as in one's complement) then add 1.

Very good property: no  $-0$

Two's complement numbers are equal if all their bits are the same.

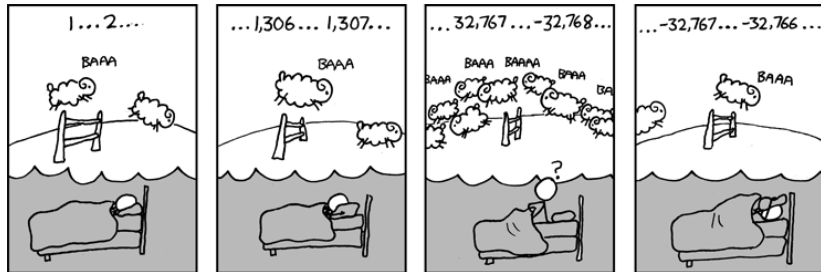
# Number Representations Compared

| Bits | Binary | Signed<br>Mag. | One's<br>Comp. | Two's<br>Comp. |
|------|--------|----------------|----------------|----------------|
| 0000 | 0      | 0              | 0              | 0              |
| 0001 | 1      | 1              | 1              | 1              |
| ⋮    |        |                |                |                |
| 0111 | 7      | 7              | 7              | 7              |
| 1000 | 8      | -0             | -7             | -8             |
| 1001 | 9      | -1             | -6             | -7             |
| ⋮    |        |                |                |                |
| 1110 | 14     | -6             | -1             | -2             |
| 1111 | 15     | -7             | -0             | -1             |

Smallest number

Largest number

# Two's Complement, In Summary



<https://xkcd.com/571/>



# Fixed-point Numbers



How to represent fractional numbers? In decimal, we continue with negative powers of 10:

$$31.4159 = 3 \times 10^1 + 1 \times 10^0 + 4 \times 10^{-1} + 1 \times 10^{-2} + 5 \times 10^{-3} + 9 \times 10^{-4}$$

The same trick works in binary:

$$\begin{aligned} 1011.0110_2 &= 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 + \\ &\quad 0 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-3} + 0 \times 2^{-4} \\ &= 8 + 2 + 1 + 0.25 + 0.125 \\ &= 11.375 \end{aligned}$$

## Need a bigger range? Try Floating Point Representation.

Floating point can represent very large numbers in a compact way.

A lot like scientific notation,  $-7.776 \times 10^3$ , where you have the *mantissa* ( $-7.776$ ) and *exponent* (3).

But for this course, think in binary:  $-1.10 \times 2^{0111}$

The bits of a 32-bit word are separated into fields. The IEEE 754 standard specifies

- ▶ which bits represent which fields (bit 31 is sign, bits 30-23 are 8-bit exponent, bits 22-00 are 23-bit fraction)
- ▶ how to interpret each field

# Characters and Strings? ASCII.

## The ASCII code

American Standard Code for Information Interchange

[www.theasciicode.com.ar](http://www.theasciicode.com.ar)

| ASCII control characters |     |                            |
|--------------------------|-----|----------------------------|
| DEC                      | HEX | Símbolo ASCII              |
| 00                       | 00h | NULL (carácter nulo)       |
| 01                       | 01h | SOH (inicio encabezado)    |
| 02                       | 02h | STX (inicio texto)         |
| 03                       | 03h | ETX (fin de texto)         |
| 04                       | 04h | EOT (fin transmisión)      |
| 05                       | 05h | ENQ (enquiry)              |
| 06                       | 06h | ACK (acknowledgement)      |
| 07                       | 07h | BEL (timbre)               |
| 08                       | 08h | BS (retroceso)             |
| 09                       | 09h | HT (tab horizontal)        |
| 10                       | 0Ah | LF (salto de línea)        |
| 11                       | 0Bh | VT (tab vertical)          |
| 12                       | 0Ch | FF (form feed)             |
| 13                       | 0Dh | CR (retorno de carro)      |
| 14                       | 0Eh | SO (shift Out)             |
| 15                       | 0Fh | SI (shift In)              |
| 16                       | 10h | DL (data link escape)      |
| 17                       | 11h | DC1 (device control 1)     |
| 18                       | 12h | DC2 (device control 2)     |
| 19                       | 13h | DC3 (device control 3)     |
| 20                       | 14h | DC4 (device control 4)     |
| 21                       | 15h | NAK (negative acknowledge) |
| 22                       | 16h | SYN (synchronous idle)     |
| 23                       | 17h | ETB (end of trans. block)  |
| 24                       | 18h | CAN (cancel)               |
| 25                       | 19h | EM (end of medium)         |
| 26                       | 1Ah | SUB (substitute)           |
| 27                       | 1Bh | ESC (escape)               |
| 28                       | 1Ch | FS (file separator)        |
| 29                       | 1Dh | GS (group separator)       |
| 30                       | 1Eh | RS (record separator)      |
| 31                       | 1Fh | US (unit separator)        |
| 127                      | 20h | DEL (delete)               |

| ASCII printable characters |     |         |     |     |         |     |     |         |
|----------------------------|-----|---------|-----|-----|---------|-----|-----|---------|
| DEC                        | HEX | Símbolo | DEC | HEX | Símbolo | DEC | HEX | Símbolo |
| 32                         | 20h | espacio | 64  | 40h | @       | 96  | 60h | `       |
| 33                         | 21h | !       | 65  | 41h | A       | 97  | 61h | a       |
| 34                         | 22h | "       | 66  | 42h | B       | 98  | 62h | b       |
| 35                         | 23h | #       | 67  | 43h | C       | 99  | 63h | c       |
| 36                         | 24h | \$      | 68  | 44h | D       | 100 | 64h | d       |
| 37                         | 25h | %       | 69  | 45h | E       | 101 | 65h | e       |
| 38                         | 26h | &       | 70  | 46h | F       | 102 | 66h | f       |
| 39                         | 27h | '       | 71  | 47h | G       | 103 | 67h | g       |
| 40                         | 28h | (       | 72  | 48h | H       | 104 | 68h | h       |
| 41                         | 29h | )       | 73  | 49h | I       | 105 | 69h | i       |
| 42                         | 2Ah | *       | 74  | 4Ah | J       | 106 | 6Ah | j       |
| 43                         | 2Bh | +       | 75  | 4Bh | K       | 107 | 6Bh | k       |
| 44                         | 2Ch | ,       | 76  | 4Ch | L       | 108 | 6Ch | l       |
| 45                         | 2Dh | .       | 77  | 4Dh | M       | 109 | 6Dh | m       |
| 46                         | 2Eh | -       | 78  | 4Eh | N       | 110 | 6Eh | n       |
| 47                         | 2Fh | _       | 79  | 4Fh | O       | 111 | 6Fh | o       |
| 48                         | 30h | 0       | 80  | 50h | P       | 112 | 70h | p       |
| 49                         | 31h | 1       | 81  | 51h | Q       | 113 | 71h | q       |
| 50                         | 32h | 2       | 82  | 52h | R       | 114 | 72h | r       |
| 51                         | 33h | 3       | 83  | 53h | S       | 115 | 73h | s       |
| 52                         | 34h | 4       | 84  | 54h | T       | 116 | 74h | t       |
| 53                         | 35h | 5       | 85  | 55h | U       | 117 | 75h | u       |
| 54                         | 36h | 6       | 86  | 56h | V       | 118 | 76h | v       |
| 55                         | 37h | 7       | 87  | 57h | W       | 119 | 77h | w       |
| 56                         | 38h | 8       | 88  | 58h | X       | 120 | 78h | x       |
| 57                         | 39h | 9       | 89  | 59h | Y       | 121 | 79h | y       |
| 58                         | 3Ah | :       | 90  | 5Ah | Z       | 122 | 7Ah | z       |
| 59                         | 3Bh | ;       | 91  | 5Bh | [       | 123 | 7Bh | {       |
| 60                         | 3Ch | <       | 92  | 5Ch | \       | 124 | 7Ch |         |
| 61                         | 3Dh | =       | 93  | 5Dh | ]       | 125 | 7Dh | }       |
| 62                         | 3Eh | >       | 94  | 5Eh | ^       | 126 | 7Eh | ~       |
| 63                         | 3Fh | ?       | 95  | 5Fh | -       |     |     |         |

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| Extended ASCII characters |     |         |     |      |         |     |     |         |     |      |         |
|---------------------------|-----|---------|-----|------|---------|-----|-----|---------|-----|------|---------|
| DEC                       | HEX | Símbolo | DEC | HEX  | Símbolo | DEC | HEX | Símbolo | DEC | HEX  | Símbolo |
| 128                       | 80h | Ç       | 160 | A0h  | á       | 192 | C0h | À       | 224 | E0h  | Ò       |
| 129                       | 81h | ü       | 161 | A1h  | â       | 193 | C1h | Á       | 225 | E1h  | Ó       |
| 130                       | 82h | é       | 162 | A2h  | í       | 194 | C2h | Â       | 226 | E2h  | Ô       |
| 131                       | 83h | à       | 163 | A3h  | ô       | 195 | C3h | Ã       | 227 | E3h  | Õ       |
| 132                       | 84h | á       | 164 | A4h  | ñ       | 196 | C4h | Ä       | 228 | E4h  | Ö       |
| 133                       | 85h | â       | 165 | A5h  | ï       | 197 | C5h | Å       | 229 | E5h  | Ø       |
| 134                       | 86h | ã       | 166 | A6h  | ª       | 198 | C6h | Ä       | 230 | E6h  | Ù       |
| 135                       | 87h | ç       | 167 | A7h  | «       | 199 | C7h | Å       | 231 | E7h  | Ú       |
| 136                       | 88h | è       | 168 | A8h  | »       | 200 | C8h | Æ       | 232 | E8h  | Û       |
| 137                       | 89h | é       | 169 | A9h  | ¼       | 201 | C9h | Ç       | 233 | E9h  | Ü       |
| 138                       | 8Ah | ê       | 170 | AAh  | ½       | 202 | CAh | È       | 234 | EAh  | Ý       |
| 139                       | 8Bh | ë       | 171 | ABh  | ¾       | 203 | CBh | É       | 235 | Ebh  | ÿ       |
| 140                       | 8Ch | ì       | 172 | ACH  | ¸       | 204 | CAh | Ê       | 236 | ECh  | ÿ       |
| 141                       | 8Dh | í       | 173 | ADh  | ¹       | 205 | CDh | Ë       | 237 | EDh  | ÿ       |
| 142                       | 8Eh | â       | 174 | AEh  | º       | 206 | CEh | Ì       | 238 | Eeh  | ÿ       |
| 143                       | 8Fh | Á       | 175 | AFh  | »       | 207 | CFh | Í       | 239 | Efh  | ÿ       |
| 144                       | 90h | Ê       | 176 | B0h  | ¼       | 208 | DOh | Î       | 240 | F0h  | ÿ       |
| 145                       | 91h | Ë       | 177 | B1h  | ½       | 209 | D1h | Ï       | 241 | F1h  | ±       |
| 146                       | 92h | Ì       | 178 | B2h  | ¾       | 210 | D2h | Ð       | 242 | F2h  | ±       |
| 147                       | 93h | Ó       | 179 | B3h  | ¸       | 211 | D3h | Ñ       | 243 | F3h  | ¼       |
| 148                       | 94h | Ô       | 180 | B4h  | ¹       | 212 | D4h | Ò       | 244 | F4h  | ½       |
| 149                       | 95h | Õ       | 181 | B5h  | º       | 213 | D5h | Ó       | 245 | F5h  | ¾       |
| 150                       | 96h | Ö       | 182 | B6h  | »       | 214 | D6h | Ô       | 246 | F6h  | ¸       |
| 151                       | 97h | Ù       | 183 | B7h  | ¼       | 215 | D7h | Õ       | 247 | F7h  | ¹       |
| 152                       | 98h | Ú       | 184 | B8h  | ½       | 216 | D8h | Ö       | 248 | F8h  | º       |
| 153                       | 99h | Û       | 185 | B9h  | ¾       | 217 | D9h | ×       | 249 | F9h  | »       |
| 154                       | 9Ah | Ü       | 186 | BAh  | ¸       | 218 | DAh | ¸       | 250 | FAh  | ¼       |
| 155                       | 9Bh | Ý       | 187 | BBh  | ¹       | 219 | DBh | ¹       | 251 | FBh  | ½       |
| 156                       | 9Ch | Ë       | 188 | BCh  | º       | 220 | DCh | º       | 252 | FDh  | ¾       |
| 157                       | 9Dh | Ø       | 189 | B Dh | »       | 221 | DDh | »       | 253 | F Dh | ¸       |
| 158                       | 9Eh | ×       | 190 | BEh  | ¼       | 222 | DEh | ¼       | 254 | FEh  | ¹       |
| 159                       | 9Fh | ƒ       | 191 | BFh  | ½       | 223 | DFh | ½       | 255 | FFh  | º       |