

Summer intern project presentation

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Outline

➤ Why – motivation?

- ➤ What abstract model?
- ➤ How algorithms?
- ➤ How good simulation results?

➤ Summary

Motivation

Real-timely monitoring the network performance and service availability requires measurement techniques

Measure end-to-end delay, packet loss, and the impact on service quality

- Service-specific *probes* are active probes that closely mimic the service traffic such that they receive the same treatment from the network as the actual service traffic
- Evaluating their impact of network impairments on service can be performed by end-to-end probes

Measurement Methods

Previous/related work

- 1. SNMP-based or link-level measurements cannot be used to model network services for link failure or availability only
- 2. Measured data should be correlated with topology information: traceroute
 - One-packet (pathchar): estimate link bandwidths
 - Packet-pair (ICMP): estimate available bandwidths and the bottleneck link rate
- 3. IPMP: measure one-way delay using the path-record field in the IPMP packet; differently treated from normal service traffic

Source-routed Probes

Source-routed probes mimic different network services

- 1. Complete knowledge of the network topology
- 2. Combined with the miscreant-link detection algorithm (Parthasarathy, Rastogi, & Thottan, Bell Labs Technical Memo, 2005) (to isolate the links contributing to the performance degradation)
- 3. Source-routed probe mechanism avoids the correlation problem
- 4. Network support for source-routing mechanism, such as MPLS.

Design Source-routed Probes

- \gg In designing a set of probes, our goals are:
 - 1. To minimize the cost of the probe traffic, while obtaining the maximum (resp. full) coverage of all (resp. interesting) links
 - \Rightarrow Optimizing the total cost of the probe traffic
 - \Rightarrow Optimizing the maximal-cost of a probe
 - 2. To minimize probe installation costs and maintenance costs
 - \Rightarrow Optimizing the number of probes
 - ★ We do not consider minimizing the number of *terminals* in the context of this talk



Our contributions

Theoretical results:

- 1. An exact algorithm for minimizing the total probe traffic
- 2. A 2-approximation algorithm for minimizing the maximal-cost of a probe, in case the number of probes is bounded
 - Getting the exact solution is NP-hard
- 3. A 2-approximation algorithm for minimizing the number of probes, in case the maximal-cost of a probe is bounded
 - Getting the exact solution is NP-hard
- Simulation results:

For most ISP topologies: just 5% of the nodes as *terminals* to cover more than 98% of the edges \implies increasing the number of terminals does not help much in minimizing the total probe traffic

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Abstract model

Model the network as an undirected graph G = (V, E)
 A set of specific nodes as *terminals* T ⊆ V; a set of interesting edges S ⊆ E
 A *path* is a set of concatenated edges between 2 nodes in V; an *elementary path* is a path without loops
 A *probe* is an elementary path from one terminal to another terminal
 Why: eliminating loops is necessary for practical implementation – a path with loops will be rejected by the routers

> A cost function $w_e \in \mathbb{R}^+$ over each edge $e \in E$

The cost of a probe P is $w(P) := \sum_{e \in P} w_e$

> Our target: find a set of probes, such that \ldots

Abstract model

 \blacktriangleright Find a set of probes \mathcal{P} , such that $\forall e \in S$, there exists at least one probe $P \in \mathcal{P}, e \in P$ Link-covering problem (LCP) : $\min \sum w(P)$ $P \in \mathcal{P}$ $\min(\max_{P \in \mathcal{P}} w(P))$ Primal link-cover problem (**PLP**) : subject to: $|\mathcal{P}| \leq k$ $\min k$ Dual link-cover problem (**DLP**) : subject to: $|\mathcal{P}| = k$ $w(P) \leq l_{max}, \forall P \in \mathcal{P}$





➤ Why – motivation?

- ➤ What abstract model?
- \gg How algorithms?
 - 1. LCP
 - 2. $\ensuremath{\mathbf{PLP}}$ and its hardness
 - 3. \mathbf{DLP} and its hardness
- ➤ How good simulation results?

➤ Summary



```
Indexing all terminals;
```

for each edge e do

for each terminal do

Find a shortest path from one end of e to one terminal in G, ties broken;

Remove all intermediate nodes and associated edges;

On the remaining graph, find the shortest path from the other end of e to one terminal;

end for

end for

```
Choose the minimal-cost probe P_e for edge e;

Remove all interesting edges \in P_e; mark e and them as Y to P_e if edges \notin P_i,

\forall i \neq e; else mark as N to P_e;

for each probe P_i do

if \forall f \in P_i, f is marked N to P_i or shared edge(s) are marked N to P_i then

Remove probe P_i or concatenate unshared part at the joint point;

Update edge status;

end if

end for
```

Optimality Proof

- 1. Optimal for divide (single edge) and conquer (combine)
- 2. Contradiction method used to prove for the single edge case
- 3. Any 2 probes have no shared nodes (crossing points), but (possibly) shared edges
- 4. No cross-link terminals \Rightarrow end nodes of end edges act as terminals with associated gain \Rightarrow Disjoint probes can be combined if cost is reduced





NP-hardness for **PLP** and **DLP**

 $\min(\max_{P \in \mathcal{P}} w(P))$, subject to: $|\mathcal{P}| \leq k$

 $\min k$, subject to: $|\mathcal{P}| = k$, and $w(P) \leq l_{max}$, $\forall P \in \mathcal{P}$

Reduced from Minimal Makespan Problem

Reduced from Bin-packing Problem





Approximation Algorithms for **PLP** and **DLP**

```
\min(\max_{P \in \mathcal{P}} w(P)), subject to: |\mathcal{P}| \leq k
```

- ➤ Two-stages for PLP
 - 1. Find a probe for each edge; end nodes of end edge act as terminals
 - 2. Merge $2 \ {\rm probes} \ {\rm with} \ {\rm minimal-cost} \ {\rm between} \ 2 \ {\rm terminals}$
- Binary search for the solution to DLP
- ➤ Analysis

Feasibility: merging still results elementary probe when no shared edges (proved in the paper)

Performance: 2-approximation, similar to the bin-packing algorithm's proof (see the paper for details)

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Simulation Set-up

- 1. ISP topologies from RocketFuel project
- 2. The largest 5 topologies: Telstra (Australia), Sprintlink (US), Verio (US), Level3 (US), and AT&T (US)
- 3. The terminals are chosen from the backbone nodes: 5%, 10%, and 15% of |V|
- 4. The interesting edges are randomly selected: 25%, 50%, 75%, and 100% of |E|

| Name | V | E | used T (as $\%$) | covered E (as $\%$) | probe cost total | probe cost average | probe cost maximal | # of probes |
|----------------------|-----|------|---------------------|------------------------|---------------------|-----------------------|-----------------------|-------------|
| Telestra (Australia) | 351 | 784 | 17 (5%) | 392 (50%) | 802 | 3.46 | 8 | 232 |
| | | | | 769 (98.1%) | 1436 | 3.25 | 9 | 442 |
| | | | 52 (15%) | 392 (50%) | 635 | 2.56 | 5 | 248 |
| | | | | 769 (98.1%) | 1262 | 2.58 | 5 | 490 |
| Sprintlink (US) | 604 | 2279 | 30 (5%) | 1139 (50%) | 3290 | 3.91 | 10 | 842 |
| | | | | 2277 (99.9%) | 6323 | 3.85 | 10 | 1643 |
| | | | 90 (15%) | 1139 (50%) | 2495 | 2.77 | 5 | 902 |
| | | | | 2277 (99.9%) | 4852 | 2.77 | 5 | 1751 |
| Verio (US) | 972 | 2839 | 48 (5%) | 1419 (50%) | 3671 | 3.72 | 12 | 987 |
| | | | | 2839 (100%) | 6782 | 3.88 | 19 | 1749 |
| | | | 145 (15%) | 1419 (50%) | 2979 | 2.70 | 8 | 1103 |
| | | | | 2839 (100%) | 5240 | 2.66 | 8 | 1967 |
| Level3 (US) | 624 | 5301 | 31 (5%) | 2650 (50%) | 7588 | 3.29 | 8 | 2304 |
| | | | | 5301 (100%) | 15124 | 3.27 | 8 | 4621 |
| | | | 93 (15%) | 2650 (50%) | 6460 | 2.72 | 11 | 2378 |
| | | | | 5301 (100%) | 12951 | 2.72 | 11 | 4753 |
| AT&T (US) | 631 | 2078 | 31 (5%) | 1039 (50%) | 2889 | 3.93 | 11 | 736 |
| | | | | 2078 (100%) | 5356 | 3.85 | 11 | 1392 |
| | | | 94 (15%) | 1039 (50%) | 2281 | 2.94 | 8 | 776 |
| | | | | 2078 (100%) | 4432 | 2.89 | 8 | 1534 |

Simulation Results on Telestra

| $used\ T$ | covered E | probe cost | probe cost | probe cost | # of probes |
|------------|-------------|------------|------------|------------|-------------|
| (as $\%$) | (as %) | total | average | maximal | |
| 17 (5%) | 196 (25%) | 558 | 3.44 | 7 | 162 |
| | 392 (50%) | 802 | 3.46 | 8 | 232 |
| | 588 (75%) | 1435 | 3.30 | 7 | 435 |
| | 769 (98.1%) | 1436 | 3.25 | 9 | 442 |
| 38 (10%) | 196 (25%) | 519 | 3.00 | 5 | 173 |
| | 392 (50%) | 911 | 2.99 | 5 | 305 |
| | 588 (75%) | 1492 | 3.33 | 5 | 452 |
| | 769 (98.1%) | 1490 | 3.13 | 5 | 476 |
| 52 (15%) | 196 (25%) | 457 | 2.77 | 5 | 165 |
| | 392 (50%) | 630 | 2.50 | 5 | 248 |
| | 588 (75%) | 1390 | 3.00 | 5 | 463 |
| | 769 (98.1%) | 1262 | 2.58 | 5 | 490 |
| 88 (25%) | 196 (25%) | 337 | 2.88 | 3 | 117 |
| | 392 (50%) | 946 | 2.92 | 4 | 324 |
| | 588 (75%) | 1371 | 2.77 | 4 | 495 |
| | 769 (98.1%) | 1520 | 2.87 | 4 | 530 |

Simulation Results on Approximation Algorithms

Simulation of PLP algorithm using 15% of nodes as terminals, and covering all edges, and k is 1/2 of the probes of LCP.

| Name | V | average degree | $ \mathcal{T} $ | # maximal-cost | # maximal-cost |
|------------|-----|----------------|-----------------|----------------|----------------|
| | | | | before merge | after merge |
| Telstra | 351 | 2.336 | 52 | 5 | 9 |
| Sprintlink | 604 | 3.77 | 90 | 5 | 10 |
| Verio | 972 | 2.92 | 145 | 8 | 10 |
| Level3 | 625 | 8.41 | 93 | 11 | 11 |
| AT&T | 631 | 3.29 | 94 | 8 | 10 |

Simulation

- 1. Not all edges randomly selected can be covered by a probe
- 2. The number of hops accounts for the cost of a probe
- 3. Terminals resides in backbone nodes





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Future Work

- 1. Consider the location and/or number of terminals, see related work (Bejerano & Rastogi INFOCOM'03)
- 2. $(1 + \epsilon)$ -approximation algorithms for **PLP** and **DLP**, based on the PTAS solutions to the Minimal Makespan Problem & Bin-packing Problem ?
- 3. 2-criteria optimization problem (probe traffic, # of terminals), the Pareto optimality?
- 4. Topological issues should be taken into account
- 5. Online version of this topic