

# CS 4705

N-Grams and Corpus Linguistics

# Reading

- Today: C. 6 through 6.2, NLP
- Next time: Supervised Machine Learning, C 2.1-2.6, 2.8 NLP

# *Questions from last time?*

- You will receive your HW0 back today.
- Those with grades  $<40$  are being dropped from the class.
- Waitlist students who passed HW0 with grades  $\geq 40$  are being added.

# Electronics Policy

- No laptops in class
- Cell phone allowed for PollEverywhere
- Tablets allowed for note-taking only.

# Download the PollEverywhere App on your Phone

- Enter my user name: kathleenmckeown
- Log in to your Columbia account
- When you respond to a poll, you should get a thank you message from me.
- Check on courseworks that we are getting answers from you.
- Get onto wifi (Columbia)

# New York Times

- Business, 9/5/19
- “A.I. Can Now Handle This 8<sup>th</sup> Grade Test. Can You?”
- In New York State, there is a greater chance of precipitation falling as snow in January than in March, because in January the Northern Hemisphere is tilted
  - Toward the Sun, and temperatures are warmer
  - Toward the Sun, and temperatures are colder
  - Away from the Sun, and temperatures are warmer
  - Away from the Sun, and temperatures are colder

# This class: Language Modeling

- Why is language modeling useful?
- Computing language models
- An example
- Evaluating language models
- Smoothing

- “But it must be recognized that the notion of “probability of a sentence” is an entirely useless one, under any known interpretation of this term.” Noam Chomsky (1969)
- “Anytime a linguist leaves the group the recognition rate goes up.” Fred Jelinek (1988)



## What Americans Have Heard or Read About Hillary Clinton

What specifically do you recall reading, hearing or seeing about Hillary Clinton in the last day or two?



GALLUP DAILY TRACKING  
JULY 17-SEPT 18, 2016

## What Americans Have Heard or Read About Donald Trump

What specifically do you recall reading, hearing or seeing about Donald Trump in the last day or two?



GALLUP DAILY TRACKING  
JULY 17-SEPT 18, 2016

# Next Word Prediction

- *Stocks plunged this ....*
- *Let's meet in Times ....*
- *I took the subway to ....*

# Stocks plunged this morning .....

# Let's meet in Times ....

# I took the subway to ...

# Seinfeld

- I was in the city
- I was on the island
- I got on the train
- I got in the taxi

# Next Word Prediction

- From a NY Times story...
  - Stocks plunged this ....
  - Stocks plunged this morning, despite a cut in interest rates by ...
  - Stocks plunged this morning, despite a cut in interest rates by the Federal Reserve, as Wall ...
  - Stocks plunged this morning, despite a cut in interest rates by the Federal Reserve, as Wall Street began

# Human Word Prediction

- Clearly, at least some of us have the ability to predict future words in an utterance.
- How?
  - Domain knowledge
  - Syntactic knowledge
  - Lexical knowledge



# Claim

- A useful part of the knowledge needed to allow **Word Prediction** can be captured using simple statistical techniques
- We'll rely on the notion of the **probability** of a sequence (of letters, words,...)
- Formula:
  - $P(w_n | w_1 w_2 w_3 \dots w_{n-1})$

# Applications

- Speech recognition
  - $P(\text{"recognize speech"}) > P(\text{"wreck a nice beach"})$
- Text generation
  - $P(\text{"three houses"}) > P(\text{"three house"})$
- Spelling correction
  - $P(\text{"my cat eats fish"}) > P(\text{"my xat eats fish"})$
- Machine Translation
  - $P(\text{"the blue house"}) > P(\text{"the house blue"})$
- Other uses
  - OCR
  - Summarization
  - Document classification

# N-Gram Models of Language

- Markov assumption: Use the previous N-1 words in a sequence to predict the next word
- Language Model (LM)
  - unigrams, bigrams, trigrams,...
- How do we **train** these models?
  - Very large corpora

# Corpora

- Corpora are online collections of text and speech
  - Brown Corpus
  - Wall Street Journal
  - AP newswire
  - Hansards
  - DARPA/NIST text/speech corpora (Call Home, ATIS, switchboard, Broadcast News, TDT, Communicator)
  - TRAINS, Radio News

# Google 1-T Corpus

## *1 trillion word tokens*

- Number of tokens – 1,024,908,267,229
- Number of sentences – 95,119,665,584
- Number of unigrams – 13,588,391
- Number of bigrams – 314,843,401
- Number of trigrams – 977,069,902
- Number of fourgrams – 1,313,818,354
- Number of fivegrams – 1,176,470,663

# Google N-Gram Release

- serve as the incoming 92
- serve as the incubator 99
- serve as the independent 794
- serve as the index 223
- serve as the indication 72
- serve as the indicator 120
- serve as the indicators 45
- serve as the indispensable 111
- serve as the indispensable 40
- serve as the individual 234

# Counting Words in Corpora

- What is a word?
  - e.g., are **cat** and **cats** the same word?
  - **September** and **Sept**?
  - **zero** and **oh**?
  - Is **\_** a word? **\*** ? **'** ?
  - How many words are there in **don't** ? **Gonna** ?
  - In Japanese and Chinese text -- how do we identify a word?

# Terminology

- **Sentence:** unit of written language
- **Utterance:** unit of spoken language
- **Word Form:** the inflected form as it actually appears in the corpus
- **Lemma:** an abstract form, shared by word forms having the same **stem**, part of speech, and word sense – stands for the class of words with **stem**
- **Types:** number of distinct words in a corpus (vocabulary size)
- **Tokens:** total number of words



# Simple N-Grams

- Assume a language has  $T$  word types in its lexicon, how likely is word  $x$  to follow word  $y$ ?
  - Simplest model of word probability:  $1/T$
  - Alternative 1: estimate likelihood of  $x$  occurring in new text based on its general frequency of occurrence estimated from a corpus (**unigram** probability)  
*popcorn* is more likely to occur than *unicorn*
  - Alternative 2: condition the likelihood of  $x$  occurring in the context of previous words (bigrams, trigrams,...)  
*mythical unicorn* is more likely than *mythical popcorn*

# Computing the Probability of a Word Sequence

- Compute the product of component conditional probabilities?
  - $P(\text{the mythical unicorn}) = P(\text{the}) * P(\text{mythical} | \text{the}) * P(\text{unicorn} | \text{the mythical})$
- The longer the sequence, the less likely we are to find it in a training corpus

*P(Most biologists and folklore specialists believe that in fact the mythical unicorn horns derived from the narwhal)*
- Solution: approximate using n-grams

# Bigram Model

- Approximate  $P(w_n | w_1^{n-1})$  by  $P(w_n | w_{n-1})$ 
  - $P(\text{unicorn} | \text{the mythical})$  by  $P(\text{unicorn} | \text{mythical})$
- **Markov assumption**: the probability of a word depends only on the probability of a limited history
- **Generalization**: the probability of a word depends only on the probability of the  $n$  previous words
  - trigrams, 4-grams, ...
  - the higher  $n$  is, the more data needed to train. Thus **backoff** models...

# Using N-Grams

- For N-gram models

- $P(w_n | w_1^{n-1}) \approx P(w_n | w_{n-N+1}^{n-1})$

- $P(w_{n-1}, w_n) = P(w_n | w_{n-1}) P(w_{n-1})$

- By the Chain Rule we can decompose a joint probability, e.g.  $P(w_1, w_2, w_3)$

$$P(w_1, w_2, \dots, w_n) = P(w_1 | w_2, w_3, \dots, w_n) P(w_2 | w_3, \dots, w_n) \dots P(w_{n-1} | w_n) P(w_n)$$

For bigrams then, the probability of a sequence is just the product of the conditional probabilities of its bigrams

$$P(\text{the, mythical, unicorn}) = P(\text{unicorn} | \text{mythical}) * P(\text{mythical} | \text{the}) * P(\text{the} | \langle \text{start} \rangle)$$

$$P(w_1^n) \approx \prod_{k=1}^n P(w_k | w_{k-1})$$

# Training and Testing

- N-Gram probabilities come from a **training corpus**
  - overly narrow corpus: probabilities don't **generalize**
  - overly general corpus: probabilities don't **reflect task or domain**
- A separate **test corpus** is used to **evaluate** the model, typically using standard **metrics**
  - held out test set; development (dev) test set
  - cross validation
  - results tested for statistical significance – how do they differ from a baseline? Other results?

# A Simple Example

- $P(\text{I want to eat Chinese food}) = P(\text{I} \mid \langle \text{start} \rangle)$   
 $P(\text{want} \mid \text{I}) P(\text{to} \mid \text{want}) P(\text{eat} \mid \text{to}) P(\text{Chinese} \mid \text{eat})$   
 $P(\text{food} \mid \text{Chinese}) P(\langle \text{end} \rangle \mid \text{food})$

# A Bigram Grammar Fragment from BERP

Eat on	.16	Eat Thai	.03
Eat some	.06	Eat breakfast	.03
Eat lunch	.06	Eat in	.02
Eat dinner	.05	Eat Chinese	.02
Eat at	.04	Eat Mexican	.02
Eat a	.04	Eat tomorrow	.01
Eat Indian	.04	Eat dessert	.007
Eat today	.03	Eat British	.001

<start> I	.25	Want some	.04
<start> I'd	.06	Want Thai	.01
<start> Tell	.04	To eat	.26
<start> I'm	.02	To have	.14
I want	.32	To spend	.09
I would	.29	To be	.02
I don't	.08	British food	.60
I have	.04	Chinese food	.75
Want to	.65	British cuisine	.01
Want a	.05	British lunch	.01



- $P(\text{I want to eat British food}) = P(\text{I} | \langle \text{start} \rangle) P(\text{want} | \text{I}) P(\text{to} | \text{want}) P(\text{eat} | \text{to}) P(\text{British} | \text{eat}) P(\text{food} | \text{British}) = .25 * .32 * .65 * .26 * .001 * .60 = .000080$

- Suppose  $P(\langle \text{end} \rangle | \text{food}) = .2$ ?

- vs.  $P(\text{I want to eat Chinese food}) = ?$

*What is the formula for this sentence? You can answer in numbers only.*

**I want to eat Chinese food.**

# Solution

- $$P(\text{I want to eat British food}) = P(\text{I} | \langle \text{start} \rangle) \\
P(\text{want} | \text{I}) P(\text{to} | \text{want}) P(\text{eat} | \text{to}) P(\text{British} | \text{eat}) \\
P(\text{food} | \text{British}) = .25 * .32 * .65 * .26 * .001 * .60 = .000080$$

- Suppose  $P(\langle \text{end} \rangle | \text{food}) = .2$ ?

- vs. *I want to eat Chinese food* = ?

- What is the formula for this sentence? You can answer in numbers only.*

- Probabilities roughly capture ``syntactic'' facts, ``world knowledge''

- eat** is often followed by an NP

- British food is not too popular

- N-gram models can be trained by **counting** and **normalization**

We can compute bigram probabilities  
using corpus counts

## BERP Bigram Counts

	I	Want	To	Eat	Chinese	Food	lunch
I	8	1087	0	13	0	0	0
Want	3	0	786	0	6	8	6
To	3	0	10	860	3	0	12
Eat	0	0	2	0	19	2	52
Chinese	2	0	0	0	0	120	1
Food	19	0	17	0	0	0	0
Lunch	4	0	0	0	0	1	0

# BERP Bigram Probabilities

- **Maximum Likelihood Estimation (MLE):** relative frequency of e.g.  $\frac{freq(w_1, w_2)}{freq(w_1)}$
- Normalization: divide each row's counts by appropriate unigram counts for  $w_{n-1}$

I	Want	To	Eat	Chinese	Food	Lunch
3437	1215	3256	938	213	1506	459

- Computing the bigram probability of **I I**
  - $P(I|I) = C(I,I)/C(\text{all } I)$
  - $p(I|I) = 8 / 3437 = .0023$

# *What is the probability of “want to”?*

	I	Want	To	Eat	Chinese	Food	lunch
I	8	1087	0	13	0	0	0
Want	3	0	786	0	6	8	6
To	3	0	10	860	3	0	12
Eat	0	0	2	0	19	2	52
Chinese	2	0	0	0	0	120	1
Food	19	0	17	0	0	0	0
Lunch	4	0	0	0	0	1	0

I	Want	To	Eat	Chinese	Food	Lunch
3437	1215	3256	938	213	1506	459

**What is the probability of "want to"?**



# Solution

# What do we learn about the language?

- *What's being captured with ...*
  - $P(\text{to} \mid \text{want}) = .65$
  - $P(\text{eat} \mid \text{to}) = .26$
  - $P(\text{food} \mid \text{Chinese}) = .56$
  - $P(\text{lunch} \mid \text{eat}) = .055$
- *What about...*
  - $P(I \mid I) = .0023$
  - $P(I \mid \text{want}) = .0025$
  - $P(I \mid \text{food}) = .013$

- $P(I \mid I) = .0023$  I I I I want
- $P(I \mid \text{want}) = .0025$  I want I want
- $P(I \mid \text{food}) = .013$  the kind of food I want is ...

# Approximating Shakespeare

- As we increase the value of  $N$ , the accuracy of an  $n$ -gram model increases, since choice of next word becomes increasingly constrained
- Generating sentences with random unigrams...
  - *Every enter now severally so, let*
  - *Hill he late speaks; or! a more to leg less first you enter*
- With bigrams...
  - *What means, sir. I confess she? then all sorts, he is trim, captain.*
  - *Why dost stand forth thy canopy, forsooth; he is this palpable hit the King Henry.*

- Trigrams

- *Sweet prince, Falstaff shall die.*
- *This shall forbid it should be branded, if renown made it empty.*

- Quadrigrams

- *What! I will go seek the traitor Gloucester.*
- *Will you not tell me who I am?*

- There are 884,647 tokens, with 29,066 word form types, in an approximately one million word Shakespeare corpus
- Shakespeare produced 300,000 bigram types out of 844 million possible bigrams: so, 99.96% of the possible bigrams were never seen (have zero entries in the table)
- Quadrigrams: What's coming out looks like Shakespeare because it *is* Shakespeare

# N-Gram Training Sensitivity

- If we repeated the Shakespeare experiment but trained our n-grams on a Wall Street Journal corpus, what would we get?
- This has major implications for corpus selection or design

# The wall street journal is *not* shakespeare

*unigram:* Months the my and issue of year foreign new exchange's september were recession exchange new endorsed a acquire to six executives

*bigram:* Last December through the way to preserve the Hudson corporation N. B. E. C. Taylor would seem to complete the major central planners one point five percent of U. S. E. has already old M. X. corporation of living on information such as more frequently fishing to keep her

*trigram:* They also point to ninety nine point six billion dollars from two hundred four oh six three percent of the rates of interest stores as Mexico and Brazil on market conditions



# Some Important Concepts

- **Smoothing and Backoff** : how do you handle unseen n-grams?
- **Perplexity and entropy**: how do you estimate how well your language model fits a corpus once you're done?

# Perplexity

- Information theoretic metric
  - Useful in measuring how well a **grammar** or **language model (LM)** models a natural language or a corpus

**Perplexity:** A function of the probability that a language model assigns to the test corpus.

$$P(W) = P(w_1, w_2 \dots w_N)^{-1/N}$$

or  $2^{-L(w)/M}$

Lower perplexity is good

What perplexity does a LM(1) assign to the sentences of a test corpus, compared to another LM(2)?

# Some examples

- Given a well-smoothed 5-gram language model
  - Penn Treebank: 141
  - Neural LSTM: 80

# Some Useful Empirical Observations

- A small number of events occur with high frequency
- A large number of events occur with low frequency
- You can quickly collect statistics on the high frequency events
- You might have to wait an arbitrarily long time to get valid statistics on low frequency events
- Some of the zeroes in the table are really zeros  
But others are simply low frequency events you haven't seen yet. How to address?

# Smoothing

- Words follow a Zipfian distribution
  - Small number of words occur very frequently
  - A large number are seen only once
  - Zipf's law: a word's frequency is approximately inversely proportional to its rank in the word distribution list
- Zero probabilities on one bigram cause a zero probability on the entire sentence

# Smoothing is like Robin Hood: Steal from the rich and give to the poor (in probability mass)

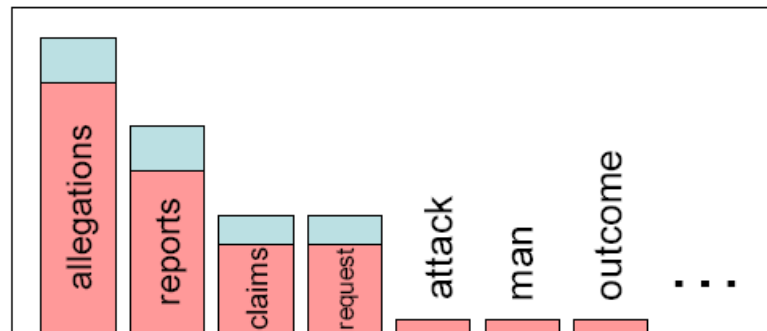
- We often want to make predictions from sparse statistics:

$P(w \mid \text{denied the})$   
3 allegations  
2 reports  
1 claims  
1 request  
7 total



- Smoothing flattens spiky distributions so they generalize better

$P(w \mid \text{denied the})$   
2.5 allegations  
1.5 reports  
0.5 claims  
0.5 request  
**2 other**  
7 total



- Very important all over NLP, but easy to do badly!

# Smoothing Techniques

- Every n-gram training matrix is sparse, even for very large corpora
- Solution: estimate the likelihood of unseen n-grams
- Problems: how do you adjust the rest of the corpus to accommodate these 'phantom' n-grams?

# Smoothing Methods

- Add-one smoothing (easy, but inaccurate)
  - Add 1 to every word count
  - Increment normalization factor by Vocabulary size:  $N$  (tokens) +  $V$  (types) :

$$p_i^* = \frac{c_i + 1}{N + V}$$

- Backoff models
  - When a count for an n-gram is 0, back off to the count for the (n-1)-gram
  - These can be weighted

$$c^*(i, j) = c(i, j) - d \quad [6.15]$$

$$P_{\text{Katz}}(i | j) = \begin{cases} \frac{c^*(i, j)}{c(j)} & \text{if } c(i, j) > 0 \\ \alpha(j) \times \frac{P_{\text{unigram}}(i)}{\sum_{i': c(i', j)=0} P_{\text{unigram}}(i')} & \text{if } c(i, j) = 0. \end{cases} \quad [6.16]$$

- Class-based smoothing
  - For certain types of n-grams, back off to the count of its syntactic class
  - E.g., Count ProperNouns in place of names (e.g., Obama)



- Class-based smoothing
  - For certain types of n-grams, back off to the count of its syntactic class
  - E.g., Count ProperNouns in place of names (e.g., Obama)
- Good-Turing
  - Re-estimate amount of probability mass for zero (or low count) ngrams by looking at ngrams with higher counts
  - Estimate

$$c^* = (c + 1) \frac{N_{c+1}}{N_c}$$

# Summary

- N-gram probabilities can be used to *estimate* the likelihood
  - Of a word occurring in a context (N-1)
  - Of a sentence occurring at all
- Smoothing techniques deal with problems of unseen words in corpus
- Entropy and perplexity can be used to evaluate the information content of a language and the goodness of fit of a LM or grammar

*Questions?*

# Homework 0