1. (True or False). Wordnet contains relations that constitute a class inheritance hierarchy over the words.

True

2. Give examples of three different types of structural ambiguities and say why they are ambiguous.

**PP attachment**
John ate the fish from a paper box. Did he eat from a paper box? Or, did he choose the fish from the paper box?

**Coordination**
John likes red cars and toys. Are the toys red?

**NP bracketing**
Spanish language teachers: Do the teachers teach Spanish or do they speak Spanish?

3. In each of the following sentences, identify the semantic roles selecting from agent, patient, theme, experiencer, stimulus, goal, recipient, benefactive, source, instrument, location, temporal. Justify your choice.

The company wrote me a letter.
Agent: the company, recipient: me, patient: letter

Jack opened the lock with a paper clip.
Agent: Jack, patient: lock, instrument: paper clip
4. Consider the following (inelegant) grammar rules from the Penn Treebank:

   VP \rightarrow VBD PP \\
   VP \rightarrow VBD PP PP \\
   VP \rightarrow VBD PP PP PP \\
   VP \rightarrow VBD PP PP PP PP \\
   ...

   a) (5 points) Give two rules that can be used to replace these four (and all the ensuing ... rules).

   \[
   VP \rightarrow VBD PP \\
   VP \rightarrow VP PP
   \]

6. Assuming the grammar below, show the parse tree for the sentence *The big yellow dog sat under the house.*

   S \rightarrow NP VP \\
   VP \rightarrow VP PP \\
   VP \rightarrow verb NP \\
   VP \rightarrow verb \\
   NP \rightarrow DET NOM \\
   NOM \rightarrow ADJ NOM \\
   NOM \rightarrow NOUN \\
   PP \rightarrow PREP NP \\
   DET \rightarrow the \\
   ADJ \rightarrow big \\
   ADJ \rightarrow yellow \\
   NOUN \rightarrow dog \\
   VERB \rightarrow sat \\
   PREP \rightarrow under \\
   NOUN \rightarrow house

   (S ((NP (DET the) (NOM ((ADJ big) (NOM ((ADJ yellow) (NOM (NOUN dog))))))) \\
   (VP ((VERB sat) (PP ((PREP under)(NP (DET the) (NOM (NOUN house))))))))

7. Show how you would have to modify the grammar above to handle the sentence *The dog in the white hat ran under the house.*

   NOM \rightarrow NOM PP
8. **Hidden Markov Models:** You are given the sentence below and the tables of probabilities show in Table 3a (this page) and Table 3b (next page).

*I promise to back the bill.*

a. Describe how the Table 3a probabilities would be obtained using the Penn Treebank.

\[ \text{count(word,POS)/count(POS). E.g., count(Promise as a VB)/Count(VB)} \]

b. A hidden markov model includes states, observations, transition probabilities, observation likelihoods. Describe what each one of these would correspond to when using an HMM for POS tagging.

states = POS tags
observations = words
transition probabilities = probability of next tag given previous tag
Observation likelihoods = probably of word given a tag.

c. Given the sentence `I promise to back the bill.` show how you would compute the probability of `back` as a verb versus the probability of `back` as a noun using the probabilities in Tables 3a and 3b using the Viterbi algorithm. You are given the values for the third column of the Viterbi table which correspond to observation 3 or `to`. They are VB: 0, TO: .00000018, NN: 0, PPSS: 0. Thus, you will show two computations both of which will use these values. You do not need to do the arithmetic; just show the formula that would be computed.

Answer: Take the max of four different computations for each current state. We are interested here in the values for two current states: VB and NN. For each of these, three computations will be 0 since the observations from the three (VB, NN, PPSS) previous states are 0.

For VB, the computation for the remaining path from TO is: 

\[ v_{i-1}(i) a_{ij} b(j|o_i) = .00000018 \times .83 \times .0008 \]

For NN, the computation for the remaining path from TO is: 

\[ .00000018 \times .00047 \times .00068 \]

If we multiply out, we see that probability as VB is greater. For VB, .0000000011952. For NN, .00000000000006.
<table>
<thead>
<tr>
<th></th>
<th>I</th>
<th>promise</th>
<th>to</th>
<th>back</th>
</tr>
</thead>
<tbody>
<tr>
<td>VB</td>
<td>0</td>
<td>.0093</td>
<td>0</td>
<td>.00008</td>
</tr>
<tr>
<td>TO</td>
<td>0</td>
<td>0</td>
<td>.99</td>
<td>0</td>
</tr>
<tr>
<td>NN</td>
<td>0</td>
<td>.0085</td>
<td>0</td>
<td>.00068</td>
</tr>
<tr>
<td>PPSS</td>
<td>.37</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 3a: Observation Likelihoods

<table>
<thead>
<tr>
<th></th>
<th>VB</th>
<th>TO</th>
<th>NN</th>
<th>PPSS</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;s&gt;</td>
<td>.019</td>
<td>.0043</td>
<td>.041</td>
<td>.067</td>
</tr>
<tr>
<td>VB</td>
<td>.0038</td>
<td>.035</td>
<td>.047</td>
<td>.0070</td>
</tr>
<tr>
<td>TO</td>
<td>.83</td>
<td>0</td>
<td>.00047</td>
<td>0</td>
</tr>
<tr>
<td>NN</td>
<td>.0040</td>
<td>.016</td>
<td>.087</td>
<td>.0045</td>
</tr>
<tr>
<td>PPSS</td>
<td>.23</td>
<td>.00079</td>
<td>.0012</td>
<td>.00014</td>
</tr>
</tbody>
</table>

Table 3b: Tag transition probabilities. The rows are labeled with the conditioning event. Thus, $P(VB|<s>) = .019$.

9. Consider the sentences *President George Bush has re-invigorated the economy by providing a bail-out program for failing Wall Street firms.* and *President George Bush has caused a disastrous economic situation by failing to provide regulations on Wall Street firms.* You’d like to compute the likelihood of these sentences given a corpus of NY Times, Wall Street Journal and the New York Post gathered over the last year. You develop a bi-gram language model.
Describe how you would: 1. Build the language model, 2. Compute the likelihood of these sentences and 3. Evaluate your language model.

I would build the language model by computing the probability of each bigram (pair of words) in the corpus. To do this, I would count the frequency of each pair of words w1 and w2 and I would then normalize by the count of the first word in the bigram: Count(w1 w2)/ Count(w1). I would do this for each pair of words that appears consecutively in the corpus. Once I had the language model, I would compute the likelihood of each sentence by determining the probability of each bigram in the sentence (including the probability of start followed by word-1) and multiplying. So, for example, Prob(start President) * (President George) * Prob (George Bush) * Prob (Bush has). etc. This must be done for both sentences. There are several ways to evaluate the language model.

8. Given the following three-layer neural network, where $A_{in}$ is the input to the network; $y$ is the gold outputs; $Z_i$ is the $i^{th}$ hidden state; $A_i$ is the $i^{th}$ activation, $b_i$ is the $i^{th}$ bias term, $f_i$ is the $i^{th}$ activation function...

$$
\begin{align*}
Z_1 &= W_1 A_{in} + b_1 \\
A_1 &= f_1(Z_1) \\
Z_2 &= W_2 A_1 + b_2 \\
A_2 &= f_2(Z_2) \\
Z_{out} &= W_{out} A_2 + b_{out} \\
A_{out} &= f_{out}(Z_{out}) \\
Loss &= f_{loss}(A_{out}, y)
\end{align*}
$$

Suppose you know the following: Your inputs are one-hot word vectors with a vocabulary of 15,000; your batch size is 200; the hidden dimension of the first layer is 512; the hidden dimension of the second layer is 256; and your outputs are vectors of length 10. What are the dimensions of the following?

- $A_{in}$ (answer: 15,000 x 200)
- $W_1$ (answer: 512 x 15,000)
- $b_1$ (answer: 512 x 1)
- $A_1$ (answer: 512 x 200)
- $W_2$ (answer: 256 x 512)
- $b_2$ (answer: 256 x 1)
- $W_{out}$ (answer: 10 x 256)
- $A_{out}$ (answer: 10 x 200)