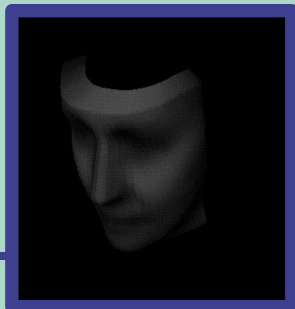


# *Mixtures of Eigenfeatures for Real-Time Structure from Texture*

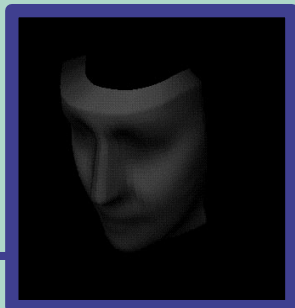
Tony Jebara  
Kenneth Russell  
Alex Pentland

Vision & Modeling  
Perceptual Computing  
M.I.T. Media Laboratory



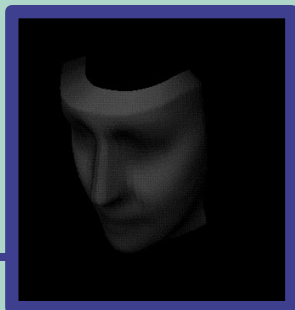
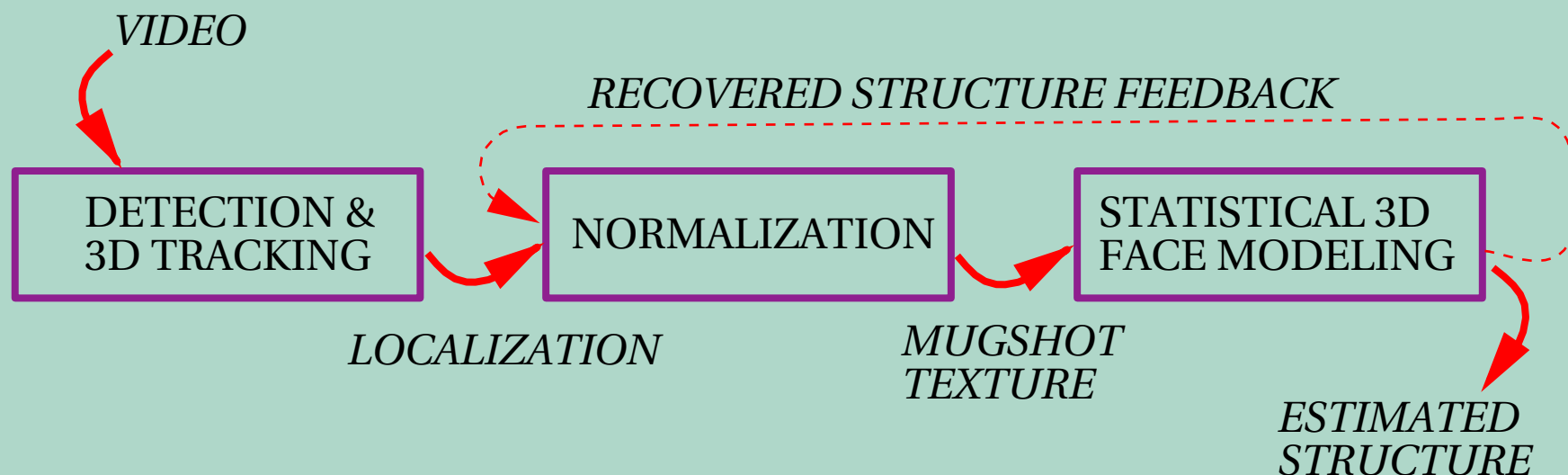
## MOTIVATION

- Recover full 3D information from live video:  
*rotation, translation, focal length, structure, texture*
- Structure is underconstrained from a single frame  
usually constraints / regularization compensate:
  - a) local smoothness (shape from shading)
  - b) motion (structure from motion)
  - c) multiple images (stereo techniques)
  - d) knowledge of a class of objects
  - e) global vs. local structure constraints
- [CVPR 97]: *Real-time feedback 3D tracker with SfM*  
SfM only recovers sparse point field (40 points @ 30Hz)  
(unless many features or optical flow → Not Real Time)
  - How much structure info in a static frame?
  - Real time structure estimation → temporal analysis
  - Fully reconstruct 3D face compactly (video-conf)
  - Can use global linear analysis vs. local non-linear redundancies and regularities in global data



# SYSTEM ARCHITECTURE

- Learn the mapping between texture and structure probabilistically to avoid cumbersome low-level operations and underconstrained formulations
- Use pre-processing and tracking to focus learning resources where needed.

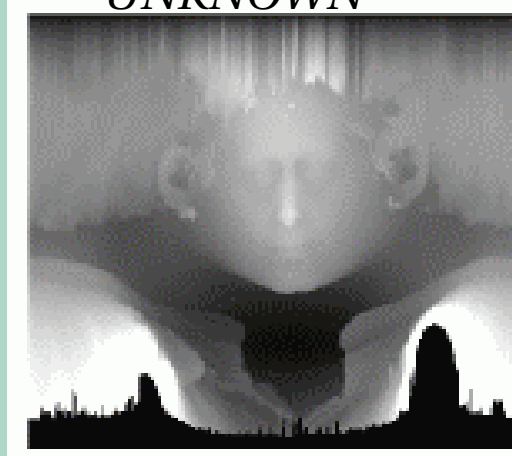


- Want a compact real-time temporal representation of facial 3D pose, translation, structure and texture

## 3D TRAINING DATA

- Knowledge Based Statistical Approach  
Learn mapping between texture and structure from Cyberware 3D face scans.
- 360 Degree Cylindrical (R,G,B,radius) value for each (theta,y) value. (very large dimensionality)
- Database of over 300 Scans:  
Wright Patterson Air Force, Lab Personnel, Headus (Cyberware affiliate), Other...

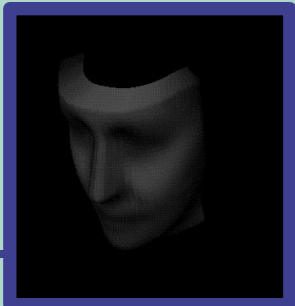
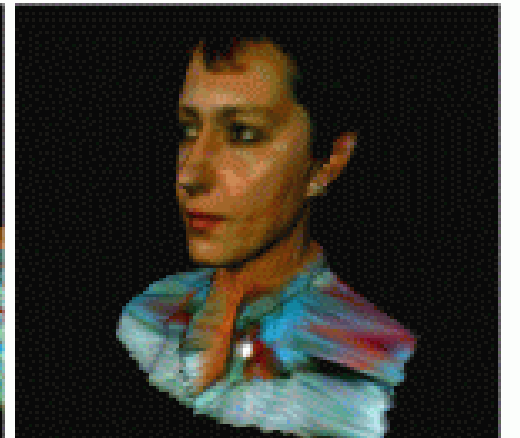
*RANGE MAP  
UNKNOWN*



*TEXTURE MAP  
KNOWN*

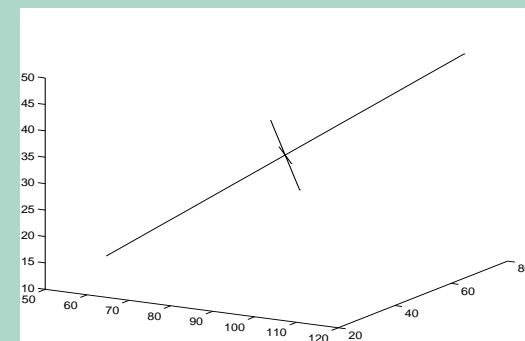
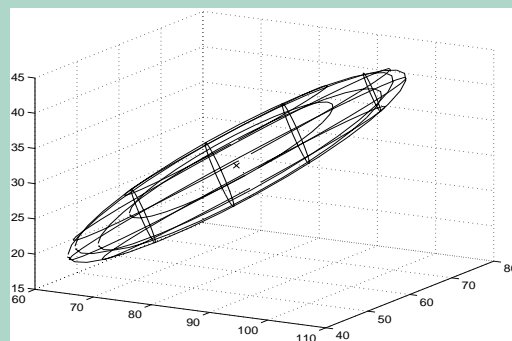
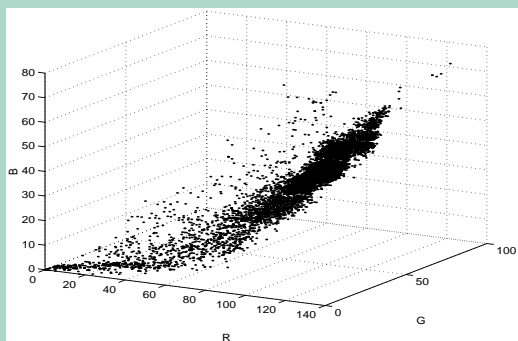


*COMBINED  
& RENDERED*



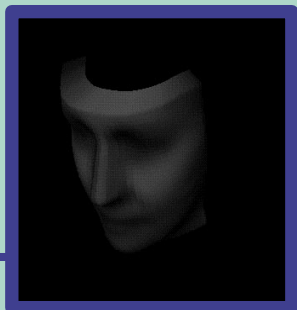
## PRE-PROCESSING

- Remove unwanted variations and non-linearities (such as illumination, background and 3D pose) to uncover interesting correlations between texture & structure
- Segmentation and 3D alignment (semi-rigid transformation)
- Illumination Correction (RGB not independent)  
Eigenspace Basis over facial colors for histogramming



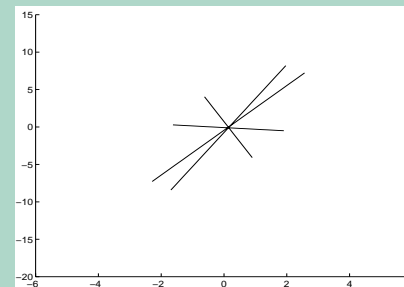
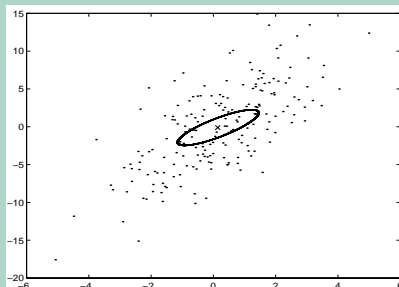
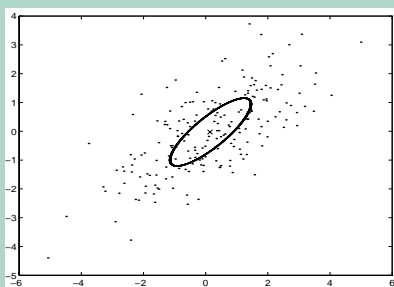
Histogram fitting via cdf's

$$T_{s \rightarrow d}(i) = c_d^{-1}(c_s(i))$$

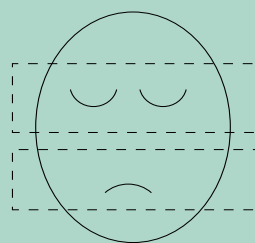


# EIGENFEATURES

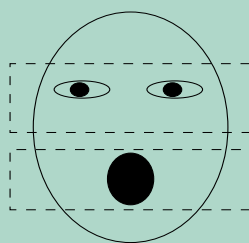
- Form a rank-deficient Gaussian model over the data (of dims  $M \gg N$  samples)
- PCA sensitive to scaling (but not rotation):



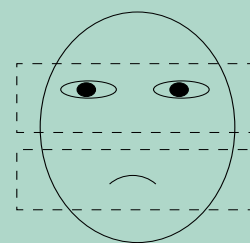
- Focus PCA resources where needed using modular eigenspace with a weight for each pixel



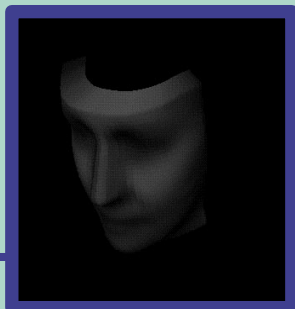
TRAINING  
SAMPLE #1



TRAINING  
SAMPLE #2



MODULAR  
EIGENSPACE



- Estimate several smaller  $M$  using  $N$  samples
- Span a larger space

# MIXTURES OF EIGENFEATURES

- Decouple image spatially into multiple eigenspaces each with its own region of applicability (weight) forms a *mask* for each eigenspace
- Make a more generalizable space than full PCA
- Simple iterative algorithm based on assumption that the Modules are binary and don't overlap

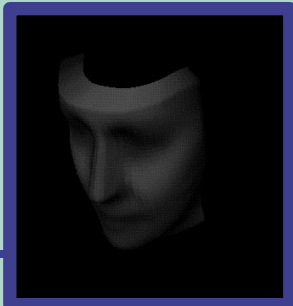
Inject regularizers (blur, epsilon, symmetry)

Estimate eigenspaces over training set

Compute eigenspaces error over x-validation set

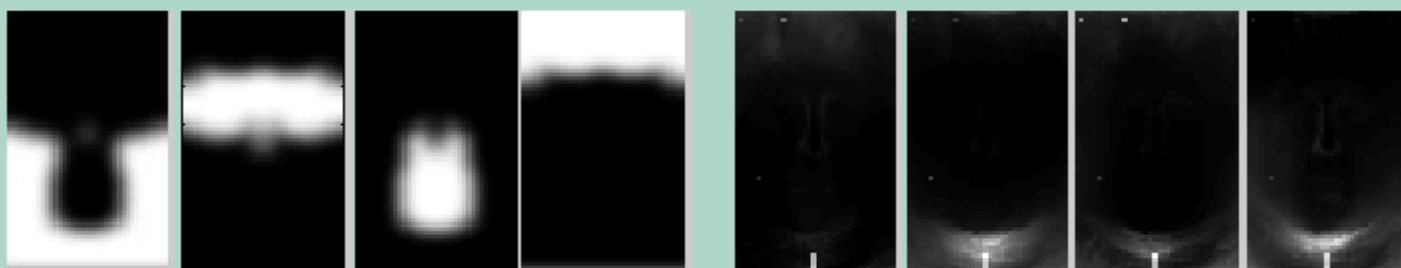
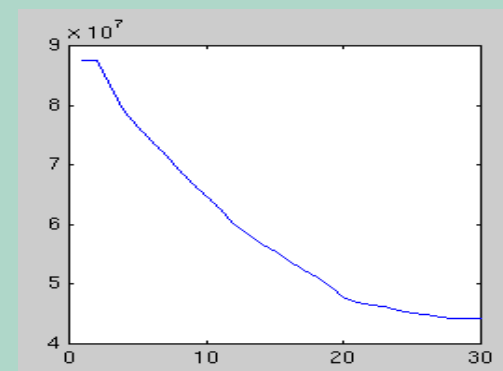
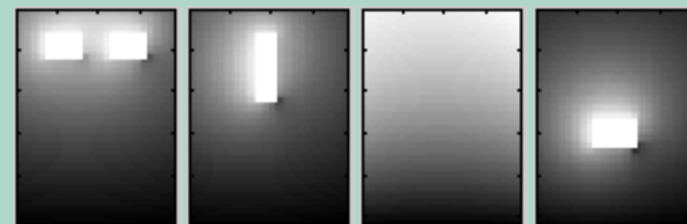
Partition image into modules according to errors

- Initialize the model pseudo-randomly and iterate until convergence (min. cross-validation error)



## FINDING THE EIGENFEATURES

- Decouples face into multiple regions with their own linear models and modes.
- Initialized both *randomly* and *manually* using Laplace's equation for interpolation
- Converges to a local min error, reduces Error up to 70% after 25 iterations
- Resulting Masks & Spatial Errors





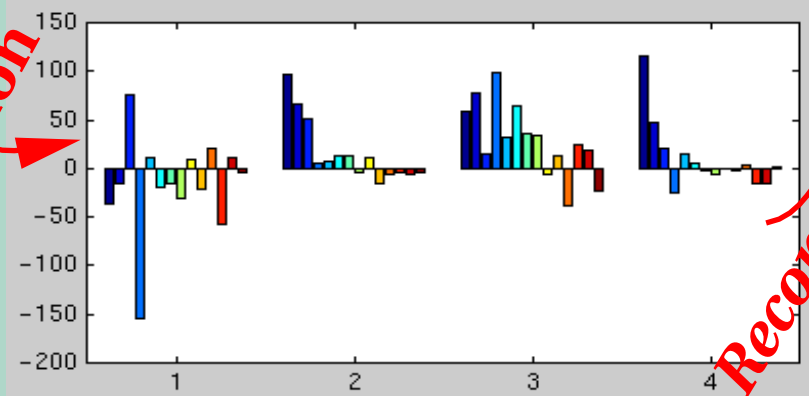
# EIGENVECTORS, PROJECTION & FILTERING

- Modular Eigenvectors resulting from training show coupling over image regions

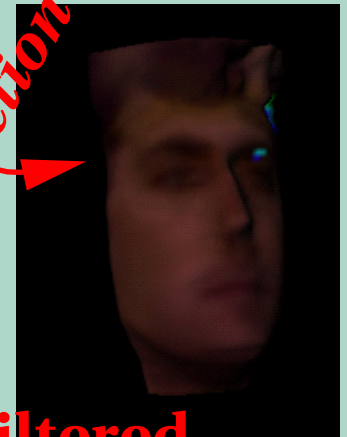


**Original**  
10,000+ DOF

*Projection*

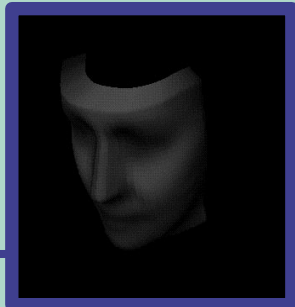


**<100 DOF**



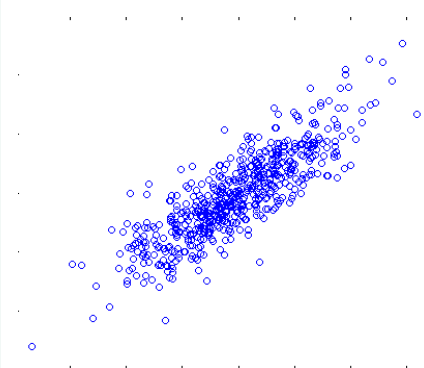
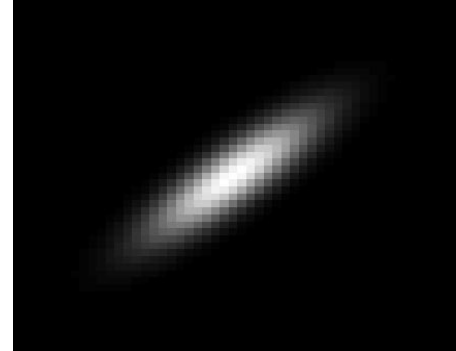
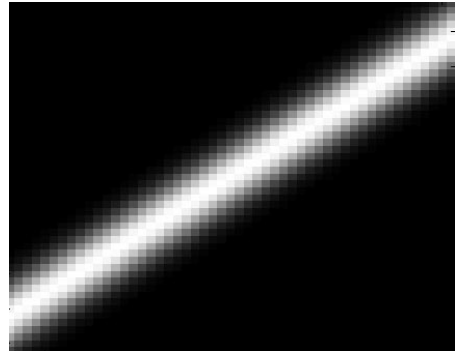
**Filtered**  
10,000+ DOF

*Reconstruction*



**Compact Coefficient Representation**  
4x14 Floats, storage size < 100 bytes

# REGRESSION

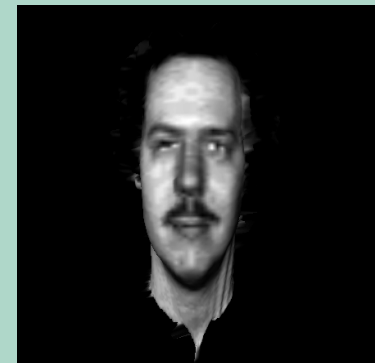
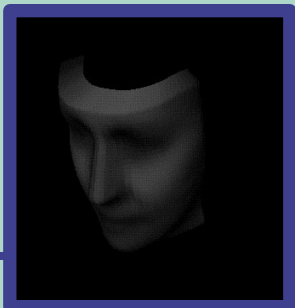




$$p(x_k, x_u) = \frac{\exp\left\{-\frac{1}{2} \begin{bmatrix} x_k \\ x_u \end{bmatrix}^T \begin{bmatrix} \Sigma_{kk} & \Sigma_{uk} \\ \Sigma_{uk} & \Sigma_{uu} \end{bmatrix}^{-1} \begin{bmatrix} x_k \\ x_u \end{bmatrix}\right\}}{(2\pi)^{D/2} \sqrt{\begin{vmatrix} \Sigma_{kk} & \Sigma_{uk} \\ \Sigma_{uk} & \Sigma_{uu} \end{vmatrix}}}$$

$$p(x_u | x_k) \propto \exp\left\{-\frac{1}{2} (x_u - \Sigma_{uk} \Sigma_{kk}^{-1} x_k)^T \times \left(\Sigma_{uu} - \Sigma_{uk} \Sigma_{kk}^{-1} \Sigma_{ku}\right)^{-1} \times (x_u - \Sigma_{uk} \Sigma_{kk}^{-1} x_k)\right\}$$

$$x^* = \begin{bmatrix} x_k \\ \hat{x}_u \end{bmatrix} = \begin{bmatrix} x_k \\ \Sigma_{uk} \Sigma_{kk}^{-1} x_k \end{bmatrix}$$

- Tricky in higher dims due to rank deficiency and cost
- Use trained model, condition on known & estimate unknown



# 3D FACE TRACKING AND SfM

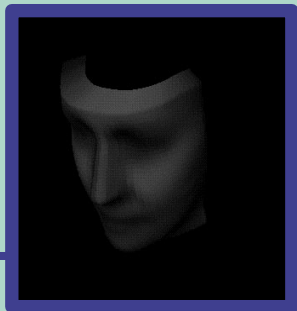
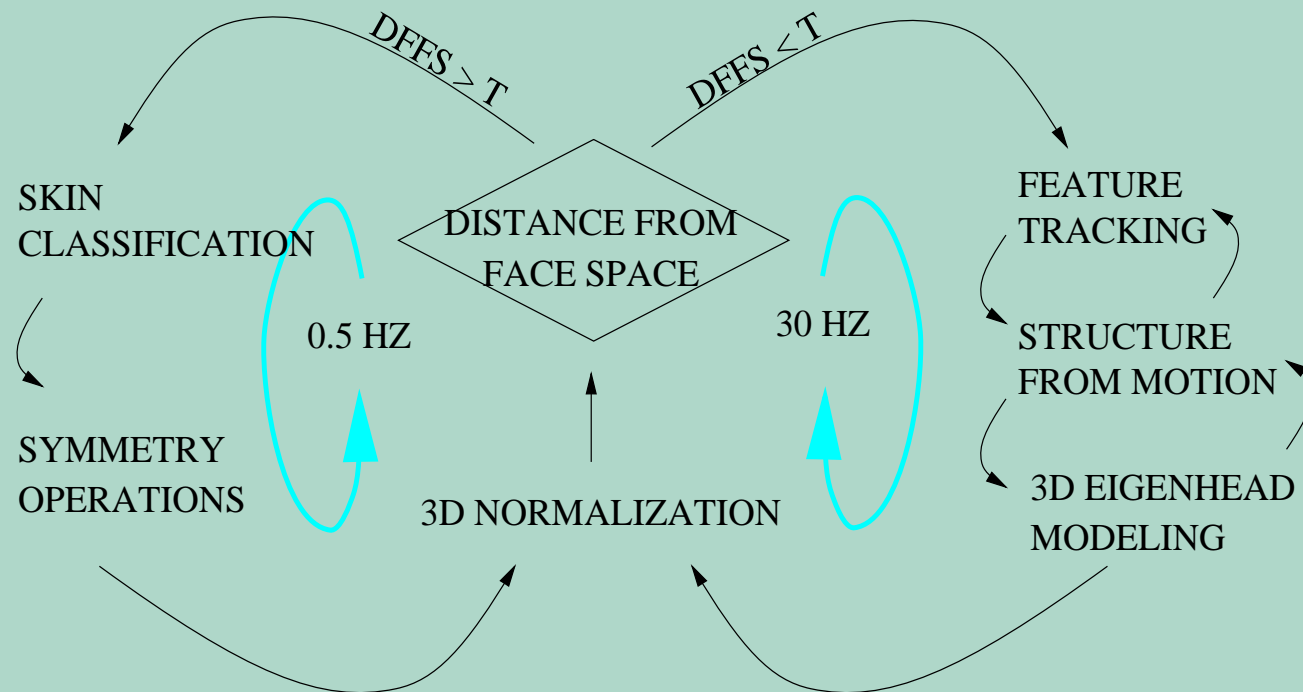
- In Real-Time, Detect, Track and Normalize a face in 3D by computing 3D pose and coarse 3D structure

- 3D GLOBAL ADAPTIVE COUPLING OF 2D FEATURES

Local 2D Feature Tracking  $\leftrightarrow$  Global Rigid 3D Structure Holistic Texture

DETECTION

TRACKING

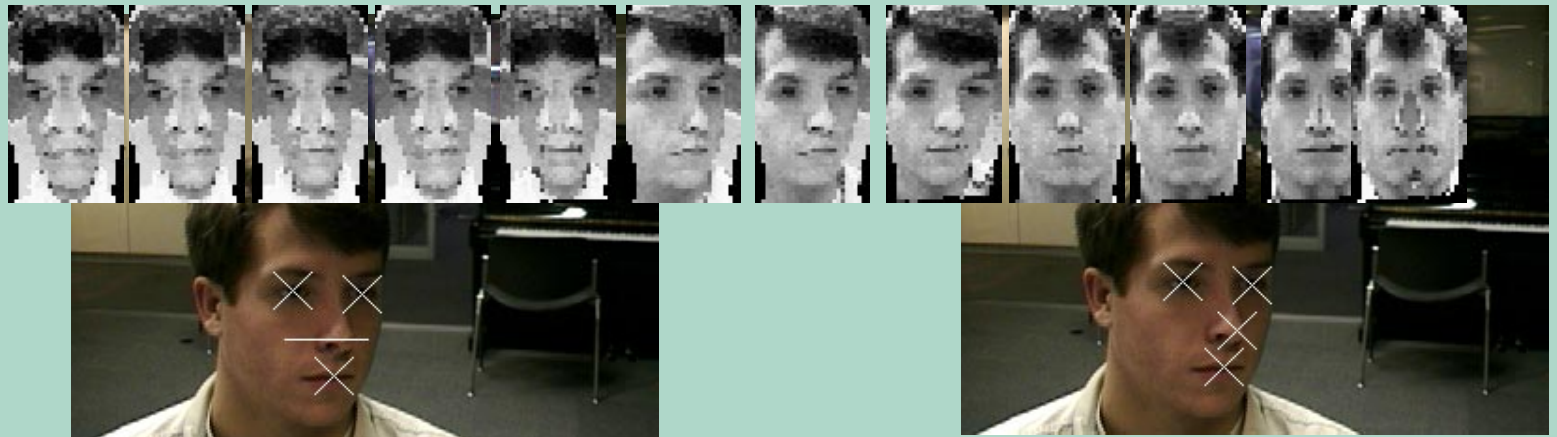


## DETECTION AND DFFS

- YUV Mixture of Gaussians skin color model (EM)
- Symmetry Operations (Radial and Axial)
- Geometric Constraints



- Refining and Pruning initial localization with DFFS on 3D Frontally Warped Mug-Shot Images

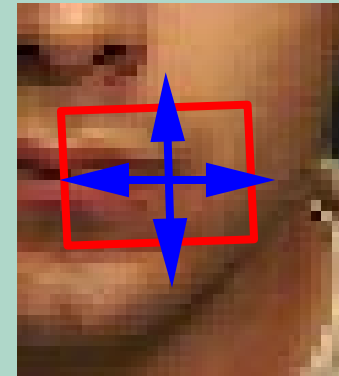


## 2D FEATURE TRACKING



Initialize 8 Local 2D Feature Trackers

SSD NORMALIZED CORRELATION



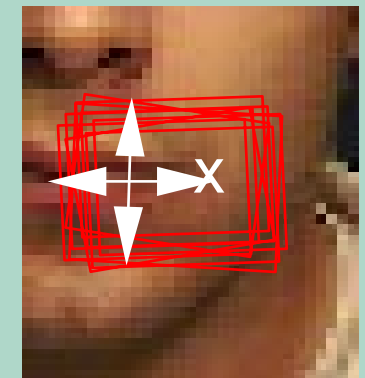
TRANSLATION



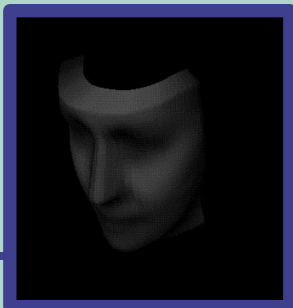
SCALE  
ROTATION

- Get 2D motion,  $u = (T_x, T_y, \theta, \text{scale})$  via linear model of SSD
- 2D motion is also represented as motion of 2 anchor points

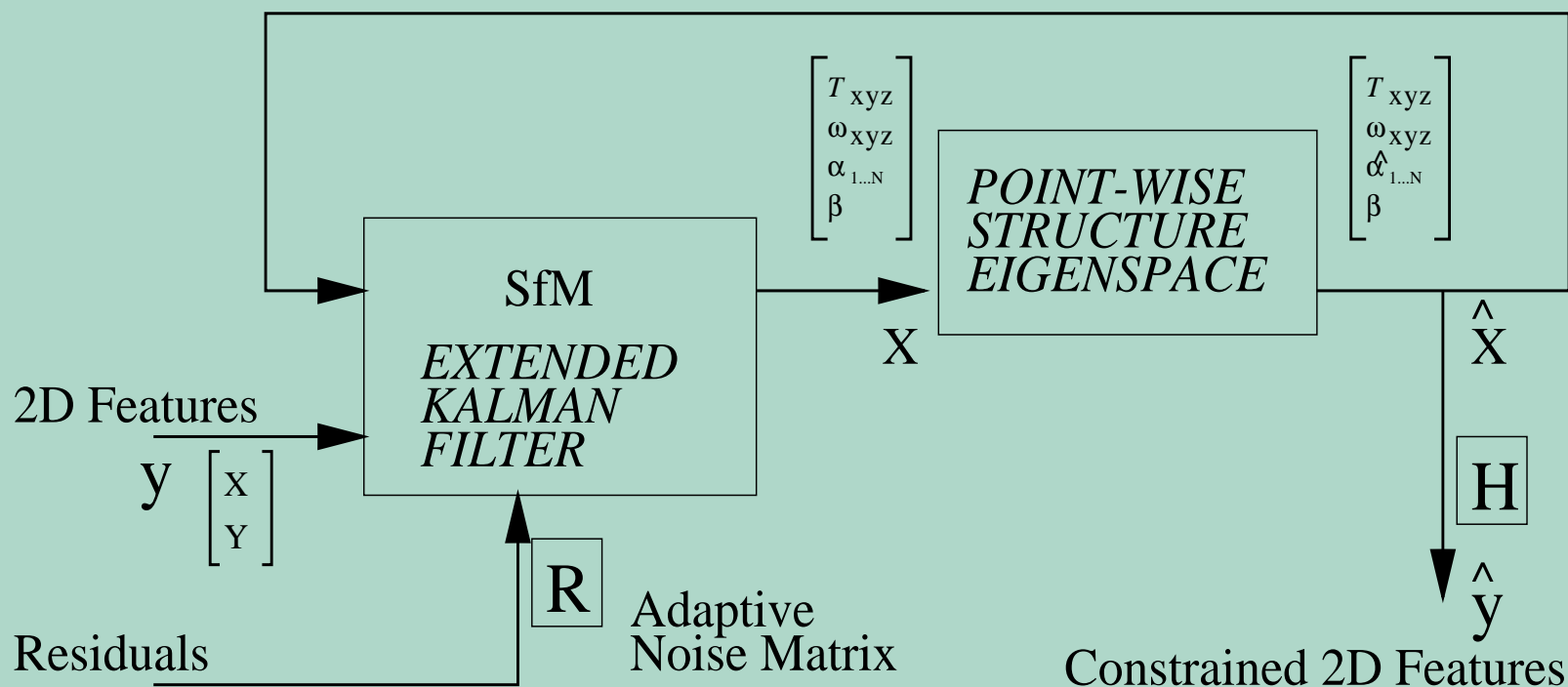
Also get sensitivity of model or 4x4 covariance of  $u$  (over SSD) by artificially perturbing each tracker.



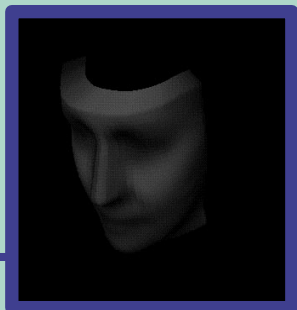
$$C_{4 \times 4} (u, SSD)$$



# FEEDBACK STRUCTURE FROM MOTION



- Get 2D Features from anchor points on each patch
- Form block-diagonal  $R = \text{diag}(C_1, C_2, \dots, C_8)$
- Form pointwise eigenspace of structure ( $\alpha$ ) from Cyberware
  - Use feedback of constrained, rigid SfM to re-initialize the 2D trackers for the next frame.
- GLOBAL ADAPTIVE 3D FUSION OF 2D TRACKERS





# TRACKING ACCURACY & STABILITY

- Robust due to 3D SfM based integration of multiple trackers
- Recover 3D Translation, Rotation, Focal Length  
Point-Wise Structure Estimate (20 points)
- 30 Hz Tracking (1 Hz detection)
- Stable in tracking mode for extended periods of time
- Robust to <65 degrees rot  
large occlusion  
fast motion

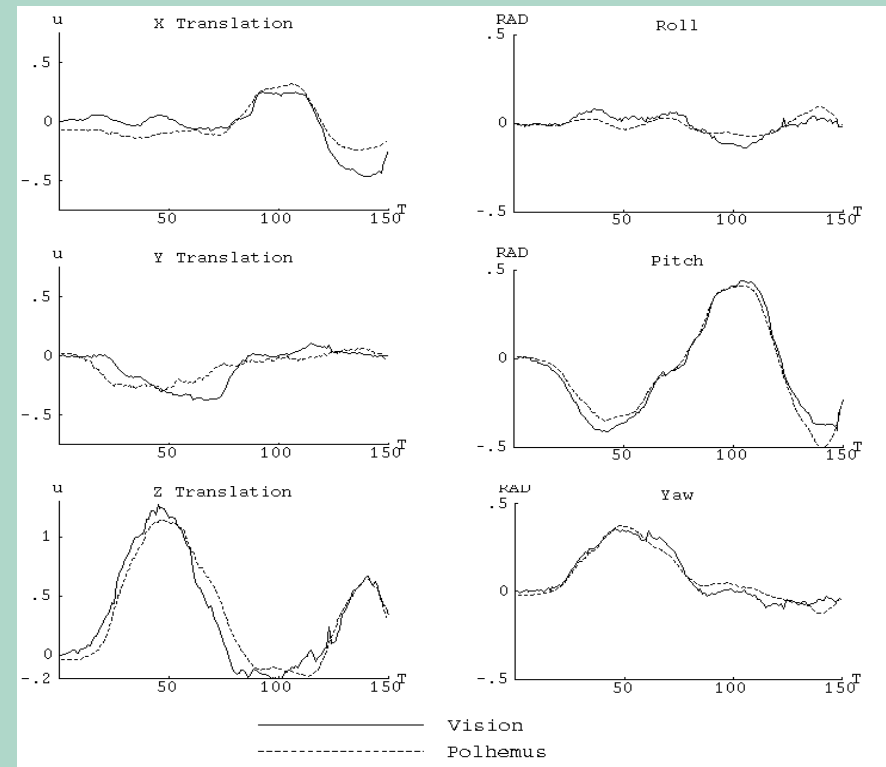
– Vision vs Polhemus Head  
Tracking and Structure Est.

**RMS differences**

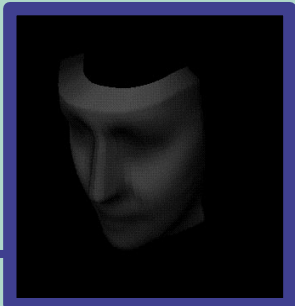
***0.11 units***

***2.35 degrees***

***Scale 10–12cm \* 0.11***

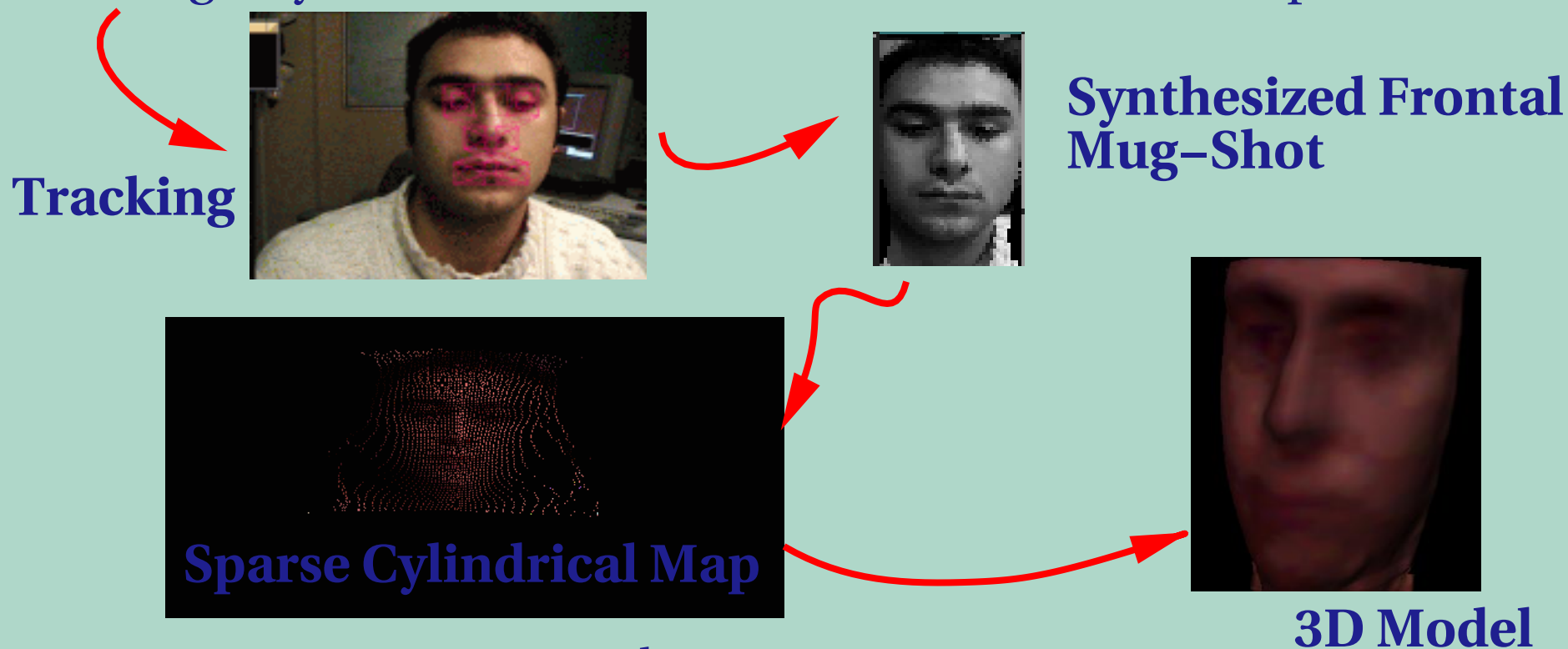


Within polhemus error [Azarbayejani & Pentland, 95]



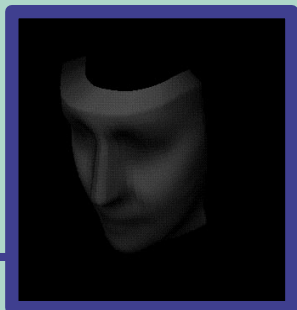
# TEXTURE STABILIZATION & 3D REGRESSION

- Use estimates of  $T_x$ ,  $T_y$ ,  $T_z$  and quaternion to align a average Cyberware head to the face and texture map it



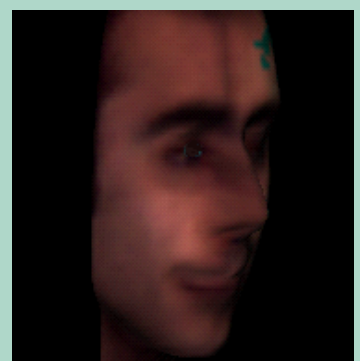
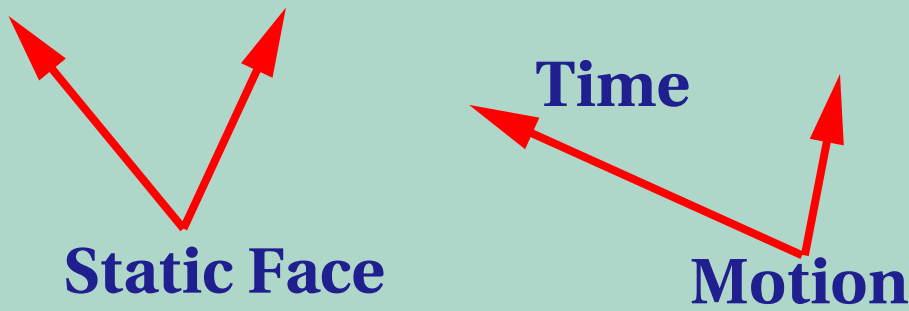
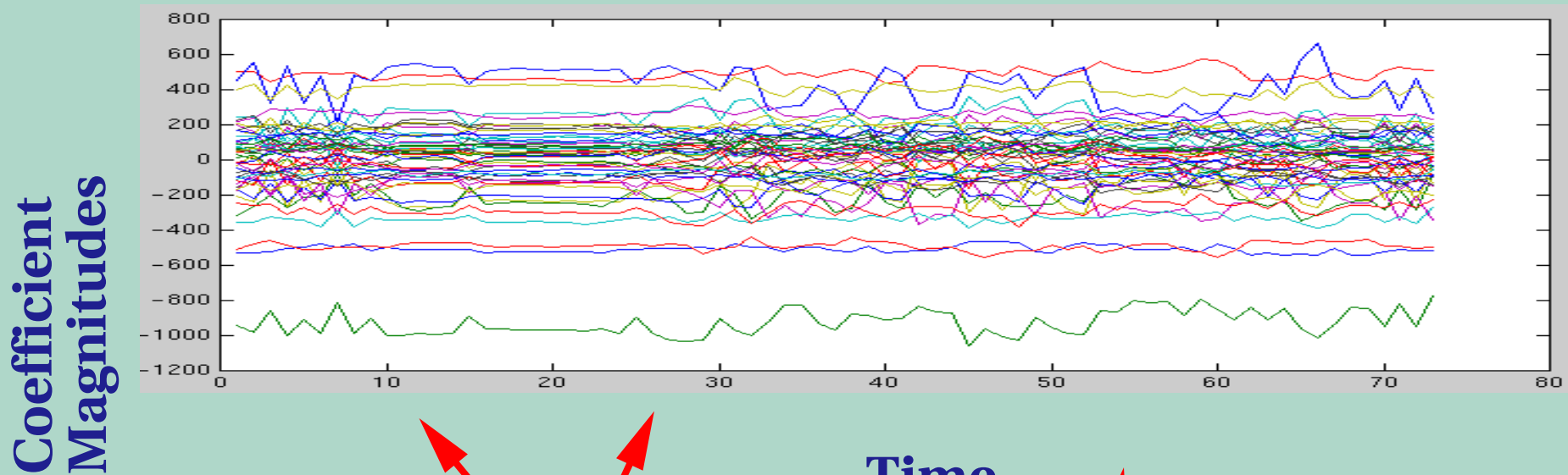
Regress unknown components  
of sparse cylindrical map:

- 1) Continuous Texture (interpolate texture)
- 2) 3D Range Data Structure





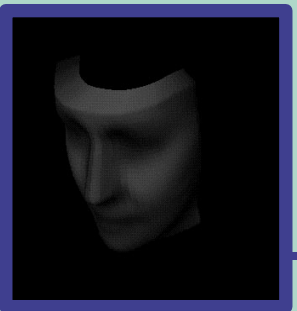
# TEMPORAL DESCRIPTION



During Static Tracking:

Avg %SSD difference  
from Cyberware  
scan (in eigenspace)

= 18 % Magnitude



# SPATIO-TEMPORAL INTEGRATION (KF)

## *CURRENT & FUTURE WORK:*

- Spatial Structure Integration  
Accumulation of texture data over whole cylindrical structure when tracking large pose variations
- Temporal Structure Integration:  
Recursive integration of eigenspace coefficients via Kalman Filter
- More flexible non-linear models
  - More detailed temporal integration and intra-personal & extra-personal analysis

