



CS1001

Lecture 24

Overview

- Encryption
- Artificial Intelligence
- Homework 4

Reading

- Brookshear, 11.6
- Brookshear, 10

Homework 4

- Check Courseworks
- Problems based on
 - Handout (Smullyan, Natural Deduction)
 - Question from Ch. 10
 - Question from Ch. 11

Some Trivial Schemes

- Caesar cipher: substitution cipher:
 - $A \rightarrow D, B \rightarrow E$
- Captain Midnight Secret Decoder rings:
 - shift variable by n : $IBM \rightarrow HAL$, or :
 - $(\text{letter} + \text{offset}) \bmod 26$
 - only 26 possible ways of secret coding.
- Monoalphabetic cipher:
 - generalization, arbitrary mapping of one letter to another
 - $26!$, approximately 4×10^{26}
 - statistical analysis of letter frequencies
- One-time pad
 - A random sequence of 0's and 1's XORed to plaintext

Definitions

- Process data into unintelligible form, reversible, without data loss
- Usually one-to-one (not compression)
- Other services:
 - Integrity checking: no tampering
 - Authentication: not an imposter
- Plaintext $\xrightarrow{\text{encryption}}$ ciphertext $\xrightarrow{\text{decryption}}$ plaintext

Computational Difficulty

- Algorithm needs to be efficient.
 - Otherwise only short keys can be used.
- Most schemes can be broken: depends on \$\$\$.
 - E.G. Try all possible keys.
- Longer key is often more secure:
 - Encryption $O(N+1)$.
 - Brute-force cryptanalysis: $O(2^{N+1})$, twice as hard with each additional bit.
- Cryptanalysis tools:
 - Special-purpose hardware.
 - Parallel machines.
 - Internet coarse-grain parallelism.

Secret Key vs. Secret Algorithm

- Secret algorithm: additional hurdle
- Hard to keep secret if used widely:
 - Reverse engineering, social engineering
- Commercial: published
 - Wide review, trust
- Military: avoid giving enemy good ideas

Cryptanalysis: Breaking an Encryption Scheme

- Ciphertext only:
 - Exhaustive search until “recognizable plaintext”
 - Need enough ciphertext
- Known plaintext:
 - Secret may be revealed (by spy, time), thus <ciphertext, plaintext> pair is obtained
 - Great for monoalphabetic ciphers
- Chosen plaintext:
 - Choose text, get encrypted
 - Useful if limited set of messages

Models for Evaluating Security

- Unconditional security (perfect secrecy)
 - Observation of ciphertext provides no information
 - Uncertainty/entropy $H(p) = H(p|c)$
- Complexity-theoretic security
- Provable security
 - As difficult to break as solving well-known and *supposedly* difficult problem
- Computational security
- Ad hoc security

Brute Force Attacks

- Number of encryption/sec: 1 million to 1 billion/sec
- 56-bit key broken in 1 week with 120,000 processors (\$6.7m)
- 56-bit key broken in 1 month with 28,000 processors (\$1.6m)
- 64-bit key broken in 1 week with 3.1×10^7 processors (\$1.7b)
- 128-bit key broken in 1 week with 5.6×10^{26} processors

Types of Cryptography

- Hash functions: no key
- Secret key cryptography: one key
- Public key cryptography: two keys - public, private

Secret Key Cryptography

- Same key is used for encryption and decryption
 - Symmetric cryptography
- Ciphertext approximately the same length as plaintext
- Substitution codes, DES, IDEA
- Message transmission:
 - Agree on key (but how?)
 - Communicate over insecure channel
- Secure storage: *crypt*

Secret Key Cryptography (Cont'd)

- Strong authentication: prove knowledge of key without revealing it:
 - Send challenge r , verify the returned encrypted $\{r\}$
 - Fred can obtain chosen plaintext, ciphertext pairs
 - Challenge should be chosen from a large pool
- Integrity check: fixed-length checksum for message
 - Send MIC along with the message

Public Key Cryptography

- Asymmetric cryptography
- Invented/published in 1975
- Two keys: private (d), public (e)
 - Encryption: public key; Decryption: private key
 - Signing: private key; Verification: public key
- Much slower than secret key cryptography

Public Key Cryptography (Cont'd)

- Data transmission:

- Alice encrypts m_a using e_B , Bob decrypts to m_a using d_b .

- Storage:

- Can create a safety copy: using public key of trusted person.

- Authentication:

- No need to store secrets, only need *public* keys.
- Secret key cryptography: need to share *secret* key for every person to

Public Key Cryptography (Cont'd)

- Digital signatures
 - Encrypt *hash* $h(m)$ with private key
 - Authorship
 - Integrity
 - Non-repudiation: can't do with secret key cryptography

Hash Algorithms

- Message digests, one-way transformations
- Length of $h(m)$ much shorter than length of m
- Usually fixed lengths: 48-128 bits
- Easy to compute $h(m)$
- Given $h(m)$, no easy way to find m
- Computationally infeasible to find m_1, m_2 s.t. $h(m_1) = h(m_2)$
- Example: $(m+c)^2$, take middle n digits

Hash Algorithms (Cont'd)

■ Password hashing

- Doesn't need to know password to verify it
- Store $h(p+s)$, s (salt), and compare it with the user-entered p
- Salt makes dictionary attack less convenient

■ Message integrity

- Agree on a password p
- Compute $h(p|m)$ and send with m
- Doesn't require encryption algorithm, so the technology is exportable

Public Key Crypto's Trick

- Consider the Knapsack problem (p482)
- We have a knapsack filled with numbers
- The goal is to select out a series of numbers that adds to some desired number
- How do we do this *efficiently*?

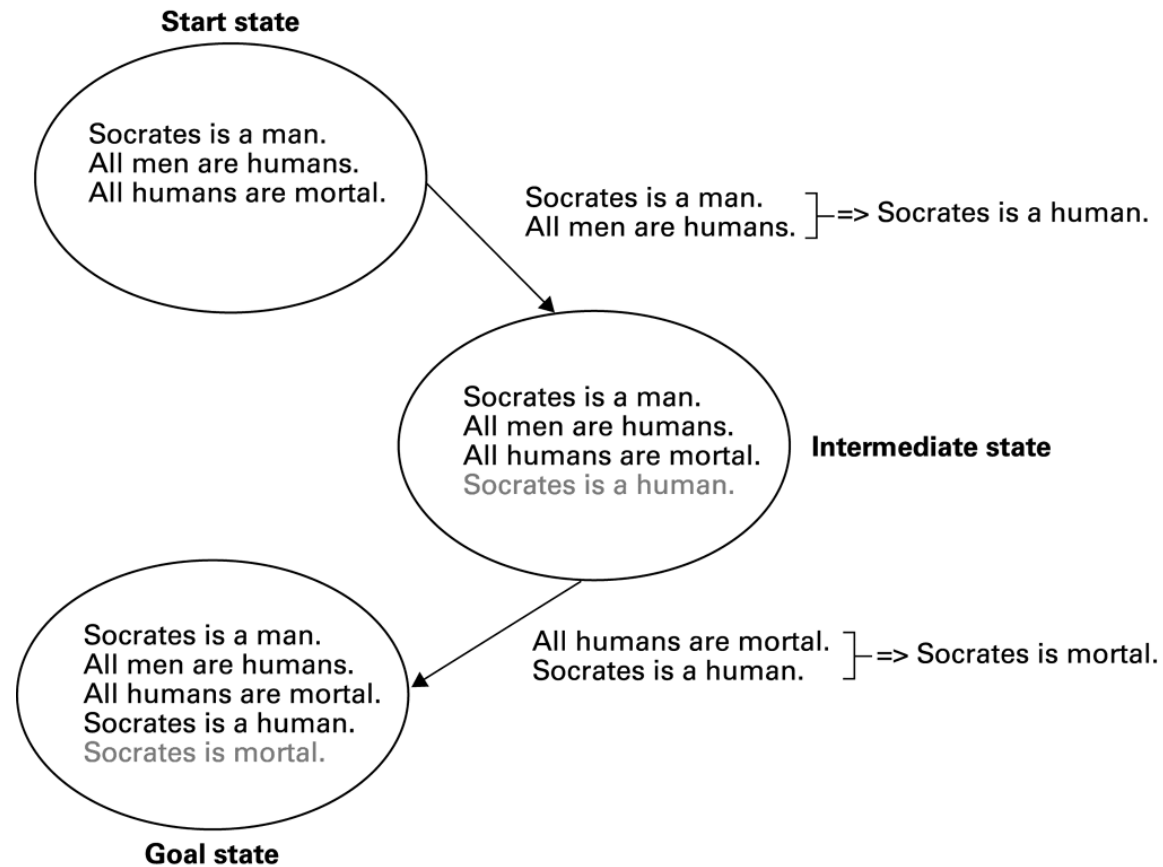
The Trick

- The trick is factoring
- You know ahead of time what certain properties of the number will be. This allows you to reduce the problem to a computable one
- Otherwise, you are dealing with a non-polynomial problem

Artificial Intelligence

- Reasoning (Production Systems)
 - Goal is to *derive* a solution given facts and rules
- Searching
 - You are given facts and rules and *search* all possible combinations to find some desired solution (usually minimum/max)
- Heuristics
 - Operate based on guidelines you know to be true about a problem

A Production System



Artificial Intelligence

- Neural Networks
- Genetic Algorithms
- Machine Learning