

Computer Graphics - Week 8



Bengt-Olaf Schneider
IBM T.J. Watson Research Center

Questions about Last Week ?



Comments about the Assignment

- ▶ **Deadline for 2nd assignment extended to Friday March 12 at 5:30 pm**
 - Regular rules for late submission apply
- ▶ **Post-mortem about 1st assignment**
 - We will subtract points for bad Readme files
 - Programs have to run !!
At least tell us they don't work.
 - Programming should involve some upfront thinking
 - Drawing each planet separately is somewhat inelegant
 - Formatting and Comments !!!
 - Questions are encouraged ...
but read the assignment and read our answers to your questions
 - If not explicitly stated otherwise, teamwork is **not** permitted



Overview of Week 3

- ▶ **Aliasing and Anti-aliasing**
- ▶ **Summary of raster graphics pipeline**

- ▶ **VRML**



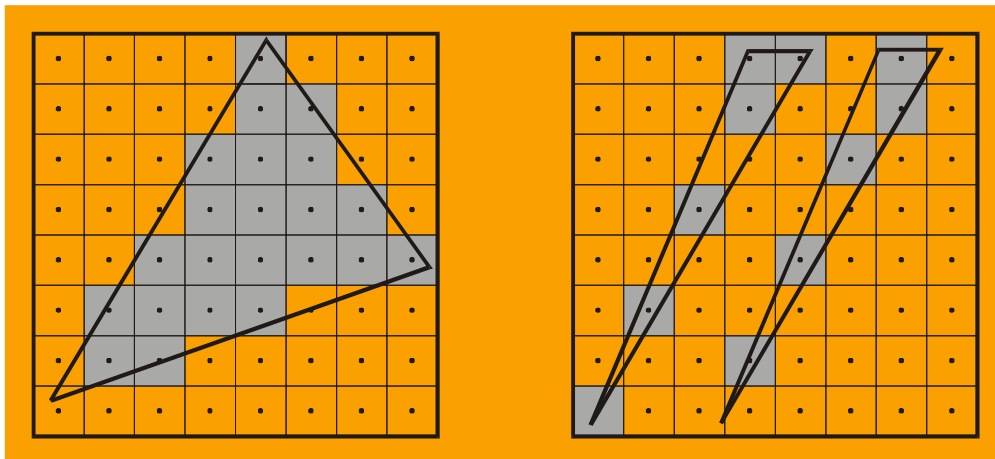
Anti-aliasing

- ▶ Aliasing are artifacts introduced by sampling the object geometry, e.g. staircasing, broken up polygons, blinking objects in animations etc.
- ▶ First, a short overview of sampling theory to further the understanding of sampling artifacts
- ▶ Then, we will study different techniques to limit or eliminate aliasing effects: anti-aliasing
- ▶ Last, we will look at implementation techniques to implement anti-aliasing, e.g. using the alpha channel



Aliasing: Examples

- ▶ Staircasing
- ▶ Broken-up objects
- ▶ Blinking (missed) objects



Aliasing: Root Cause

- ▶ **Aliasing is caused by sampling objects with insufficient sampling frequency**
 - Shannon's sampling theorem states that reconstruction of a sampled signal can only be accomplished if the signal is sampled with a frequency at least with twice the highest frequency component of the signal.
 - In practice, even higher sampling frequency is necessary.
- ▶ **Most objects in computer graphics contain infinite frequency components**
 - At the edges the signal changes instantaneously
 - Therefore, aliasing is a ubiquitous problem in graphics



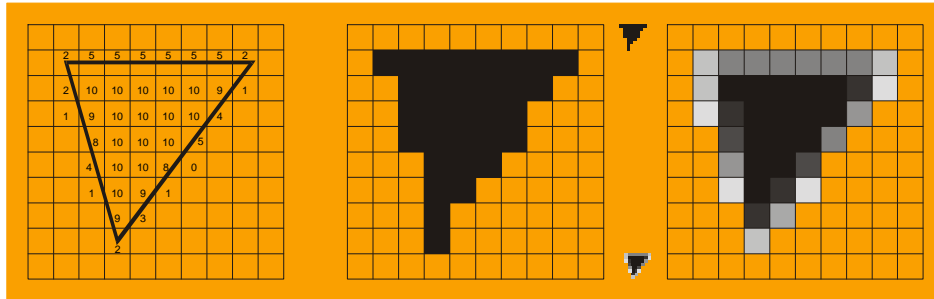
Anti-aliasing: Super-sampling

- ▶ **An obvious remedy to aliasing is to increase the sampling frequency**
 - This means to render images at a higher pixel resolution
 - Yet, super-sampling is still a point sampling process
- ▶ **Obviously, this will alleviate but not solve the problem**
 - Super-sampling misses fewer objects + creates smaller staircases
 - However it does not ensure proper sampling of all features



Anti-aliasing: Area Sampling (1)

- ▶ Point sampling is a hit-or-miss proposition
- ▶ Instead of that binary decision, we prefer to have a sliding scale that indicates how much an object contributes to a pixel
- ▶ This approach is called area sampling



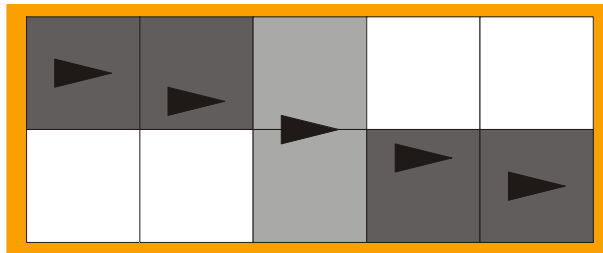
Anti-aliasing: Area Sampling (2)

- ▶ **Compute the contribution an object makes to a pixel**
 - Primitives are assumed to cover a finite area, even points and lines
- ▶ **Computation either analytical and by oversampling**
 - Analytical approaches
 - Compute the exact pixel area covered by a primitive for all pixels contributing to the anti-aliasing filter
 - Weight the area by that filter function
 - Write the pixel
 - Oversampling, approximates true area-sampling
 - Sample the image at a higher frequency
 - Compute a weighted average of all subpixels within the filter area
 - Write the pixel



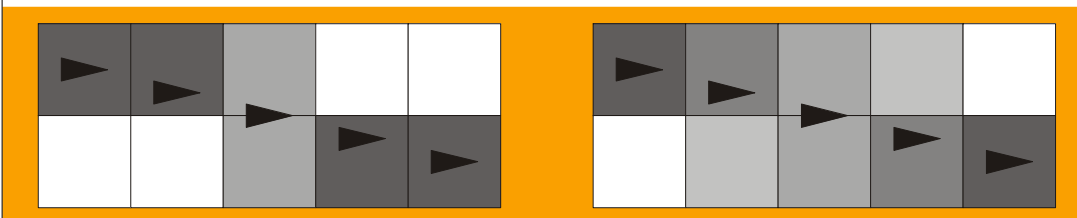
Anti-aliasing: Filtering (1)

- ▶ Once the primitives contribution to the pixel has been determined, it must be translated into a pixel intensity
- ▶ The simplest approach is to simply use the coverage percentage as a scale factor for the object's intensity
 - Creates non-linear transitions between pixels
 - Distance of the object from the pixel center is ignored
 - Box filter



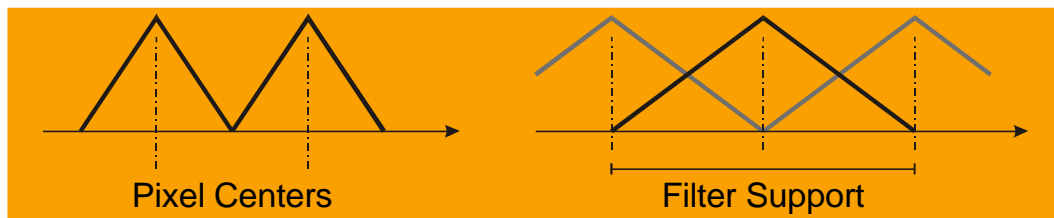
Anti-aliasing: Filtering (2)

- ▶ For a given pixel, the contributions of objects in a neighborhood around the pixel must be combined using a weighted average
- ▶ The averaging method must satisfy several criteria
 - This neighborhood is larger than 1 pixel
 - An object contributes less if it is farther away from the pixel center
 - The total contribution of an object to all affected pixels is constant



Anti-aliasing: Filtering (3)

- ▶ Filter shapes with a fall-off away from the pixel center and extending beyond the pixel borders satisfy these criteria



Anti-aliasing: Filtering (4)

- ▶ Different filter shapes satisfy these criteria
 - Triangular filter, Gaussian filters, ...
- ▶ However the actual image quality still differs between these filters
 - In general the more complicated the filter, the better the results
- ▶ This observation is explained by sampling theory



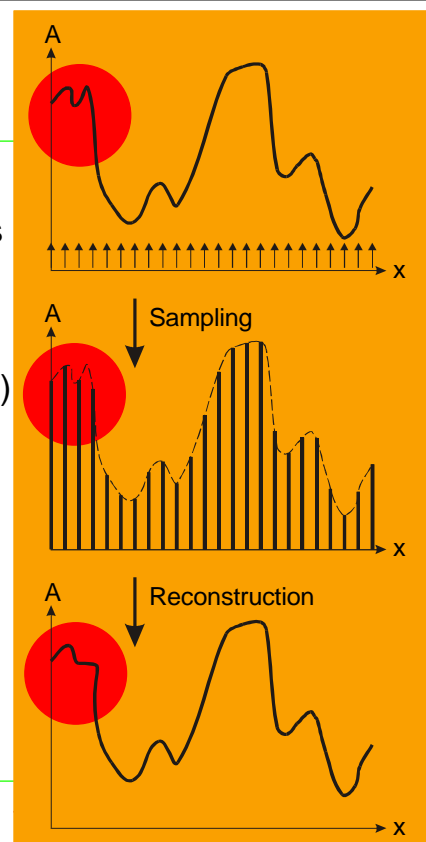
Sampling Theory: Overview

- ▶ **Sampling theory investigates and describes the effects of sampling continuous signals**
- ▶ **Examples of signals**
 - Time-variant, e.g. sound
 - Space-variant, e.g. images
 - One-dimensional, e.g. scanline
 - Two-dimensional, e.g. image
- ▶ **The signal is considered either in the time/spatial domain of the frequency domain**



Sampling Theory: Sampling Process

- ▶ **Signal sampled at intervals**
 - The size of these intervals determines the sampling frequency
 - The signal is multiplied by a comb function, consisting of several pulses (a.k.a. Dirac function or Delta function)
- ▶ **The sampled signal consists of unconnected (discrete) values**
- ▶ **The reconstructed signal constructs a new signal that approximates the original signal**
 - Reconstruction is done using a filter applied to the sampled signal



Sampling Theory: Scan Conversion

► Scan Conversion samples the input geometry

- Determine the visible object and its attributes at the pixel center
- Pixel centers form a two-dimensional array of Delta functions



Sampling Theory: Frequency Domain

► Fourier Analysis allows to decompose a signal into a mix of contributing sine waves

- Each sine wave has amplitude and phase
- For periodic signals:
Fourier series, i.e. (infinite) sum of discrete frequencies
- For aperiodic signals:
Fourier transformation, i.e. (infinite) integral various frequencies

► The total of all frequencies forming a signal is called the spectrum



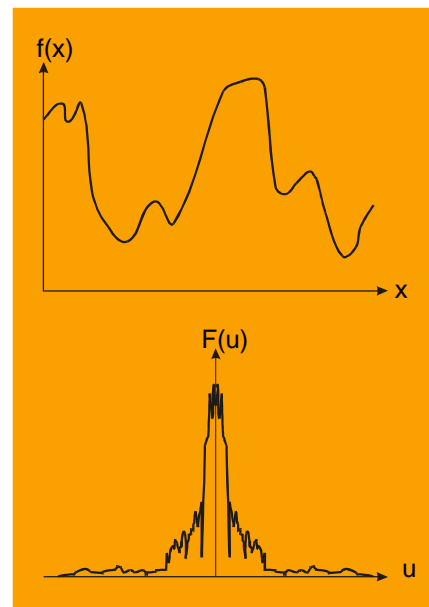
Sampling Theory: Notation

- ▶ **We denote the signal with lower case letters**
 - For example, $f(x)$ or $g(x,y)$
- ▶ **The Fourier transform is shown in capital letters**
 - For example, $F(u)$ or $G(u,v)$
 - The variable u is the frequency



Sampling Theory: Signal and Spectrum

- ▶ **Fourier transformation connects signal and frequency domain**
 - Fourier transform returns amplitude and phase
 - Often, only the amplitude spectrum is of interest
 - DC value is $F(0)$
- ▶ **Typically spectrum falls off rapidly towards high frequencies**
 - Higher frequencies indicate higher energy



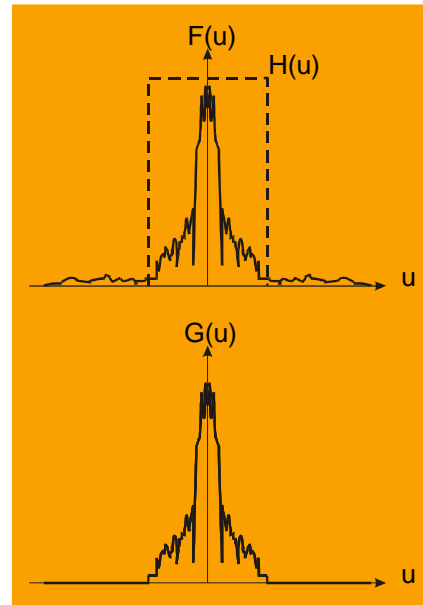
Sampling Theory: Filters

► A Filter modifies the frequency spectrum

- Scales every component of the spectrum
- $G(u) = F(u) * H(u)$

► Several filters are frequently used

- Low-pass, eliminate high frequencies
- High-pass, eliminate/reduce low frequencies
- Band-pass, attenuate all frequencies outside a certain range

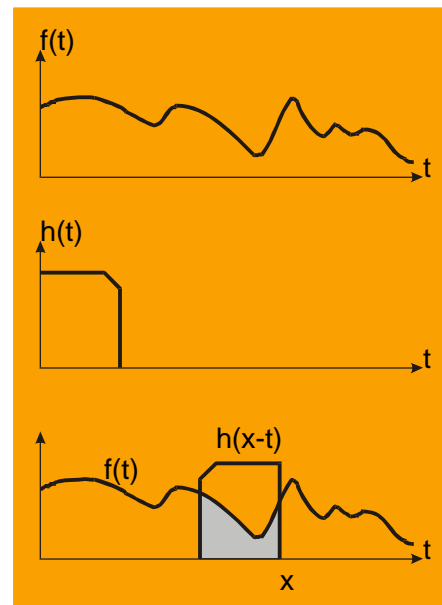


Sampling Theory: Convolution (1)

► Fourier transformation relates multiplication in one domain with convolution in the other domain

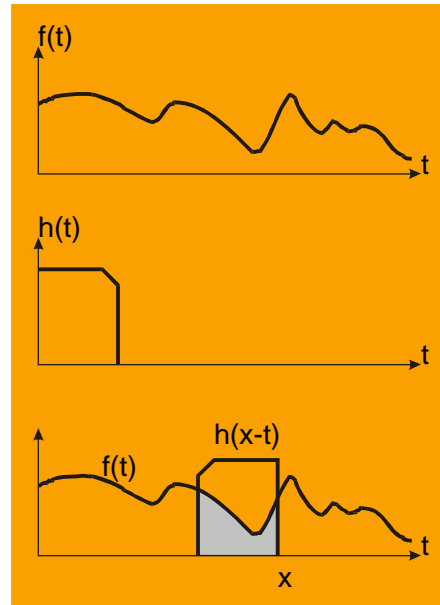
► Convolution of signal f and filter h at a point x is the product of f and h centered at x .

$$g(x) = f(x) * h(x) = \int_{-\infty}^{\infty} f(t) \cdot h(x-t) \cdot dt$$



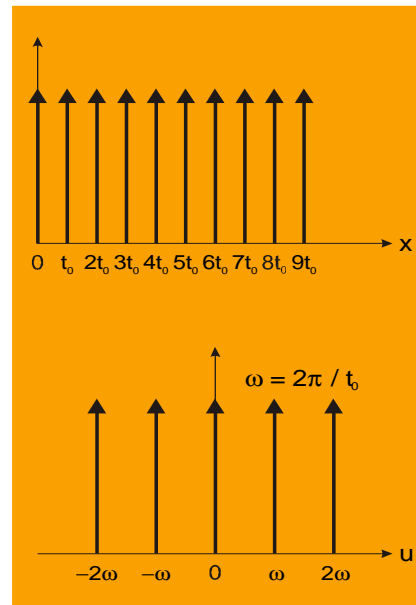
Sampling Theory: Convolution (2)

- Convolution computes an average of the signal f around x weighted by the filter function h



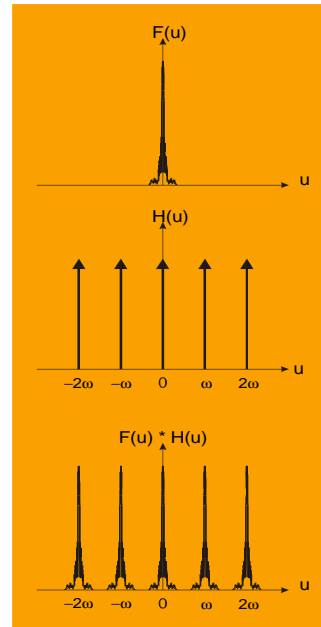
Sampling Theory: Sampling (1)

- Sampling is multiplying the original signal with a comb function
- This corresponds to a convolution of the signal with Fourier transform of the comb function.
- The Fourier transform of a comb function is another comb function
 - The distance between the Dirac pulses is determined by the sampling frequency



Sampling Theory: Sampling (2)

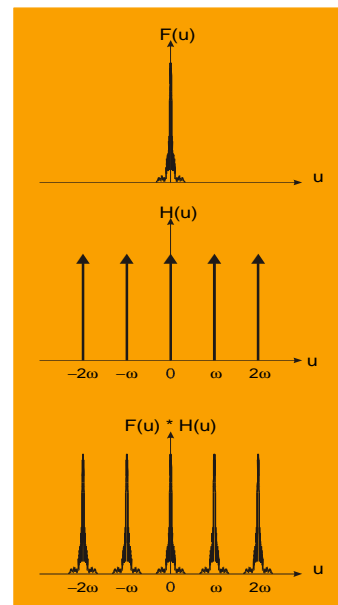
- ▶ Convoluting the signal with a comb function replicates the spectrum of the signal centered around the Dirac pulses.
- ▶ If the sampling frequency is too low, the replicated spectra overlap. This generates aliasing.



Sampling Theory: Nyquist Frequency

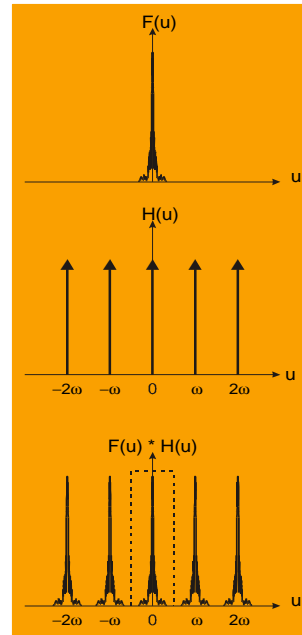
- ▶ Nyquist frequency is the minimum sampling frequency where spectra do not overlap
- ▶ Therefore:

$$f_0 = \frac{1}{t_0} \geq 2 \cdot f_{\max}$$



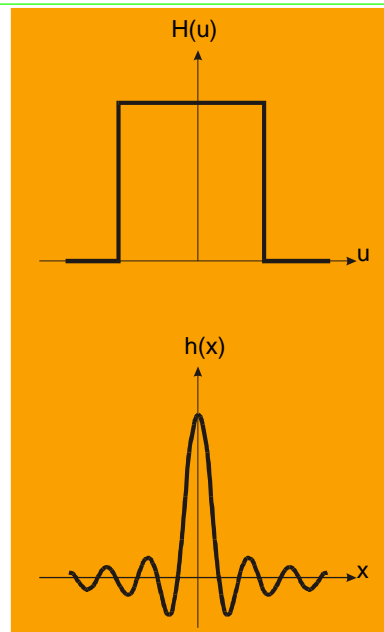
Sampling Theory: Low-pass Filter (1)

- ▶ In order to eliminate the extra copies of the spectrum, a low-pass filter is applied.
- ▶ If the copies of the spectrum do not overlap, the signal can be fully reconstructed
- ▶ Otherwise, the signal is only approximated
 - High frequencies are lost and the signal appears blurred



Sampling Theory: Low-pass Filter (2)

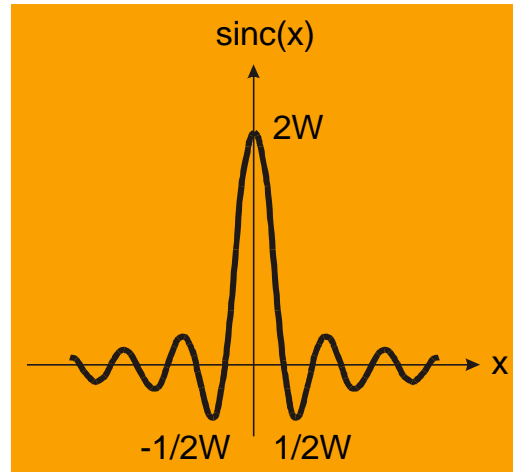
- ▶ **Filtering**
 - Multiplication in the frequency domain
 - Convolution in spatial domain
- ▶ **Ideal low-pass filter**
 - A.k.a. box filter
 - Sharp cut-off frequency
 - Corresponds to sinc function in the spatial domain
 - $\text{sinc}(x) = \sin(x) / x$



Sampling Theory: Sinc function

- ▶ **Amplitude A and zero crossings of the sinc function are determined by the sampling frequency W**

- $A = 2W$ will preserve the energy of the signal
- Lower sampling frequency widens the sinc function and reduces its amplitude



- ▶ **Sinc is problematic**

- Very wide non-zero support
- Negative lobes



Sampling Theory: Other Filters (1)

- ▶ **Box filter**

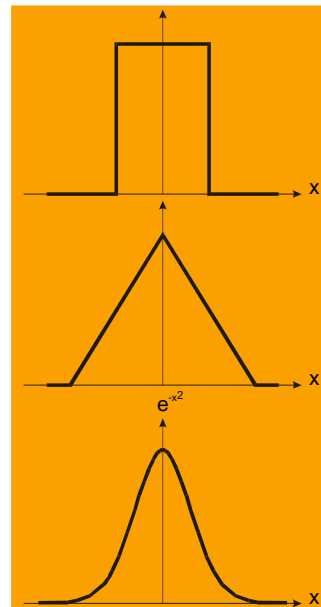
- Sinc in frequency domain
- Wide non-zero, negative support
- Unweighted average, very simple, but large errors

- ▶ **Triangular filter**

- sinc^2 in frequency domain
- Smaller, positive support
- Weighted average, fairly simple

- ▶ **Gaussian filter**

- Gaussian in frequency domain
- Small, positive support
- Better weighted average
- Computationally expensive



Sampling Theory: Other Filters (2)

► Windowed filters

- E.g. windowed sinc function, i.e.

$$sw(x) = \begin{cases} \text{sinc}(x) & \text{if } |x| < \text{const.} \\ 0 & \text{if } |x| \geq \text{const.} \end{cases}$$

► Requirements for any filter functions

- The integral over the filter function is 1.
This ensures that the signal is not attenuated or amplified
- The filter function should have finite support in the spatial domain.
This makes it practical to compute the filter function.



Sampling Theory: Summary

- **Scan conversion forms a sampling process with subsequent reconstruction**
- **Sampling theory tells us that reconstruction of a sample signal can only be accomplished if the sampling frequency is above the Nyquist frequency**
 - Then the copies of the signals spectrum do not overlap
 - To meet this condition, the signal must be band-limited
- **Reconstruction is accomplished with a low-pass filter**
 - Low-pass filtering means to compute a weighted average in the spatial domain
 - The spatial domain is larger than one pixel !
 - Different low-pass filters can be used.



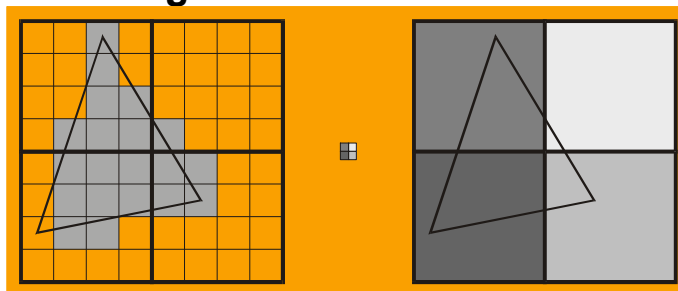
Anti-aliasing: Implementation

- ▶ Proper filtering of the rendered primitives can be difficult and computationally expensive
- ▶ Various techniques approximate the proper calculation of the area contributions
 - Super-sampling
 - Alpha channel for image compositing
- ▶ Additional problems arise if hidden-surface removal is combined with anti-aliasing
 - How much does the object cover the pixel ?
 - How much of the object is visible in the pixel ?



Anti-aliasing: Super-sampling (1)

- ▶ The area covered by the object is computed by point sampling the pixel itself
 - Sample locations are known as sub-pixels
 - Sub-pixel coverage approximates the true coverage
 - Simple to compute, applicable to all primitive types
- ▶ Filtering weights and combines the sub-pixel values according to the filter function to the final pixel value



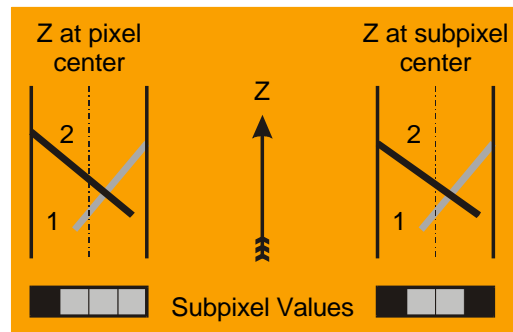
Anti-aliasing: Super-sampling (2)

► Determine visibility only at pixel center

- Creates wrong results if visibility changes in the pixel
- Requires only standard z-buffer and frame buffer

► Determine visibility at every sub-pixel

- Proper resolution of visibility within the pixel
- Adjust depth value to sub-pixel location
- Requires high-resolution z-buffer for sub-pixel color / z



Anti-aliasing: Compositing (1)

► Compositing was developed for combining images

- Images are combined pixel by pixel
- First described by Porter & Duff in 1984

► At every pixel we store in the alpha channel the current coverage information

► For a new fragment we compute new color and alpha information based on pixel and fragment color/alpha

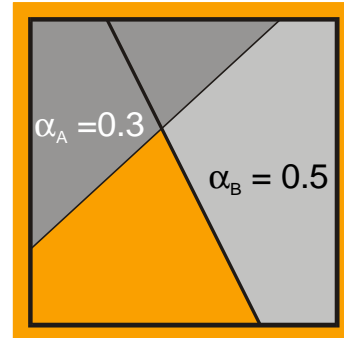
► We will now look at compositing two frgements, each of which has only one edge crossing its pixel area

- More edges per pixel are rare cases and not treated explicitly
- No edges are covered by setting $\alpha = 1$



Anti-aliasing: Compositing (2)

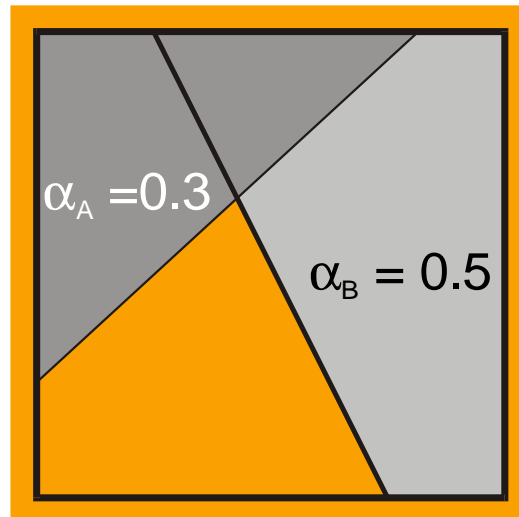
- ▶ The alpha value does not provide information about how the object is oriented within a pixel
 - There is no clear definition on how to combine current pixel value and new fragment value
 - Several possibilities for how two fragments might interact
- ▶ For image synthesis and anti-aliasing only one is relevant: **A over B**
 - See Foley et al. chapter 17.6 for other operations



Anti-aliasing: Compositing (3)

- ▶ **A over B**
 - Determine which objects is in front of the other (visibility)
 - Both fragments contribute
 - Assume random orientation of edges within the pixel
 - Then, on average $(1-\alpha_A)$ of fragment B is visible

$$C = a_A \cdot A + (1 - a_A) \cdot a_B \cdot B$$
$$a = (1 - a_A) \cdot (1 - a_B)$$



Anti-aliasing: Compositing (4)

- ▶ Notice, that the fragment colors A and B are always used weighted by the coverage values **a**

$$C = a_A \cdot A + (1 - a_A) \cdot a_B \cdot B$$
$$a = (1 - a_A) \cdot (1 - a_B)$$

- ▶ To avoid computing the term **a*A** at every pixel, colors are stored premultiplied by **a**

- Instead of (R,G,B, α)
we store ($\alpha R, \alpha G, \alpha B, \alpha$)



Anti-aliasing: OpenGL (1)

- ▶ Anti-aliasing in OpenGL may differ for different OpenGL implementations
 - Quality of anti-aliasing controlled via "hints" (glHint)
- ▶ Point and Line anti-aliasing
 - glEnable(GL_POINT_SMOOTH) + glEnable(GL_LINE_SMOOTH)
- ▶ Polygon anti-aliasing
 - If drawn as points or lines, point/line anti-aliasing applies
 - Otherwise, glEnable(GL_POLYGON_SMOOTH). This will generate coverage information in a fragment's alpha value
 - Then setup the alpha-blending function to blend between incoming fragment and stored pixel value



Anti-aliasing: OpenGL (2)

- ▶ **Supersampling is supported in OpenGL via the Accumulation Buffer**
- ▶ **The accumulation buffer is a very deep frame**
- ▶ **Successive rendering passes are accumulated in the accumulation buffer**
- ▶ **At the end the pixel values are divided by the number rendering passes (averaging)**
- ▶ **Supersampling is implemented by jittering the scene position slightly (subpixel distance) between passes**



Anti-aliasing: Summary

- ▶ **Aliasing result of under-sampling the primitives**
 - Geometric primitives introduce infinite frequencies along edges
- ▶ **Sampling theory indicates that the signal must be band-limited before sampling to allow full reconstruction of the signal**
 - The ideal low-pass filter is hard to implement
 - Approximations mean the computation of a weighted average of the pixel area covered by a primitive (area sampling)
- ▶ **Area sampling is hard to perform accurately**
 - Supersampling and compositing approximate correct area sampling and resolution of visibility between several fragments partially covering into a pixel



VRML



VRML

- ▶ **VRML = Virtual Reality Modeling Language**
 - Derived from SGI's OpenInventor
 - Version 2.0 has been adopted by ISO as VRML'97 standard
- ▶ **VRML was designed for definition, interaction and transmission of 3D models in a web-environment**
 - Based on a scene-graph model
 - Supports several non-graphics constructs to build virtual worlds, e.g. audio, event routing, customizable nodes (prototypes), concept of time, scripting interface
- ▶ **We will focus here on the graphics-specific elements of VRML, i.e. scene graphs and basic event processing**
 - Also see paper handed out in class



VRML: Overview

- ▶ **Scenes are constructed by building a scene-graph**
 - Basically identical to the model hierarchies we discussed earlier
 - Different nodes represent objects, transformations, attributes and grouping semantics
 - More formally nodes are classified as geometry (shape) nodes, appearance nodes, geometric property nodes and grouping nodes
- ▶ **Each node has none, one or several fields that set relevant node parameters**
 - Each node field has a name and a default value
 - Fields not explicitly set will assume their default value



VRML: Files

- ▶ **VRML files have the extension ".wrl" for "world"**
- ▶ **VRML files**
 - Very brief header
 - Description of the world

```
#VRML V2.0 utf8

Shape
{
  appearance Appearance
  {
    material Material
    {
      diffuseColor 1.0 0.0 0.0
      specularColor 1.0 1.0 1.0
      shininess 10
    }
  }

  geometry Cone
  {
    bottomRadius 1.0
    height 2.0
  }
}
```



VRML: Nodes

► Nodes compose the scene graph describing the world

► Syntax

- Unnamed nodes:
 <nodeType> { <body> }
- Named nodes:
 DEF <name> <nodeType> {<body>}
- Named nodes can be instantiated anywhere a node is expected:
 USE <name>
- The body of a node specifies the values of its fields and events it can send and receive

```
#VRML V2.0 utf8

Shape
{
  appearance Appearance
  {
    material Material
    {
      diffuseColor 1.0 0.0 0.0
      specularColor 1.0 1.0 1.0
      shininess 10
    }
  }

  geometry Cone
  {
    bottomRadius 1.0
    height 2.0
  }
}
```



VRML: Fields

► Fields set a node's parameters

- All fields have default values
- Default values are used if no specific value is assigned

► Syntax

- Single valued field (prefix SF)
 <fieldName> <fieldValue>
- Multi-valued field (prefix MF)
 <fieldName> [<fieldValues>]
- Multiple values are separated by commas
- The brackets may be omitted if only one value is assigned

```
#VRML V2.0 utf8

Shape
{
  appearance Appearance
  {
    material Material
    {
      diffuseColor 1.0 0.0 0.0
      specularColor 1.0 1.0 1.0
      shininess 10
    }
  }

  geometry Cone
  {
    bottomRadius 1.0
    height 2.0
  }
}
```



VRML: Field Types

- ▶ **Every field can only assume values of a specific type**
- ▶ **Types include**
 - Bool, Int32, Float, Vec2f, Vec3f, String,
 - Color, Image, Time, Rotation
 - Node
- ▶ **Most node types are available as single-valued and multi-valued versions (except Bool and Image)**



VRML: Node Types (1)

- ▶ **Shapes and Geometry**
 - Box, Cone, Coordinate, Cylinder, ElevationGrid, Extrusion, IndexedFaceSet, IndexedLineSet, Normal, PointSet, Shape, Sphere, Text
- ▶ **Appearance**
 - Appearance, Color, FontStyle, ImageTexture, Material, MovieTexture, PixelTexture, TextureCoordinate, TextureTransform
- ▶ **Grouping**
 - Anchor, Billboard, Collision, Group, Inline, LOD, Switch, Transform
- ▶ **Environment**
 - AudioClip, Background, DirectionalLight, Fog, PointLight, Sound, Spotlight



VRML: Node Types (2)

► Viewing

- NavigationInfo, Viewpoint

► Animation (Interpolators)

- ColorInterpolator, CoordinateInterpolator, NormalInterpolator, OrientationInterpolator, PositionInterpolator, ScalarInterpolator, TimeSensor

► Interaction (Sensors)

- CylinderSensor, PlaneSensor, ProximitySensor, SphereSensor, TouchSensor, VisibilitySensor

► Miscellaneous

- Script, WorldInfo



VRML: Shape and Geometry Nodes (1)

► Shape Node

- Container node to collect geometry and appearance data
- Use various other nodes to specify these fields

► 3D Primitives

- Box: axis-aligned box with specified dimensions
- Cone: cone around Y axis, centered at origin
- Sphere: obvious



VRML: Shape and Geometry Nodes (2)

► Indexed Face Set

- Used to build shapes as a collection of planar polygons
- Polygons are defined from indices into arrays of vertices, colors, normals, and texture coordinates

► The node contains at least

- a list of vertex coordinates (field 'coord')
- a list of vertex indices defining the faces (field 'coordIndex')

► Optionally, attributes can be defined at the vertices

- Colors, normals, texture coordinates

► IndexedLineSet is a similar construct for constructing a collection of lines



VRML: Shape and Geometry Nodes (3)

► Example: Pyramid

```
#VRML V2.0 utf8

Shape
{
  geometry IndexedFaceSet
  {
    coord Coordinate
    {
      point
      [ -1 -1 0,  1 -1 0,  1  1 0, -1  1 0,  0 0 2
      ]
    }
    color Color
    {
      color
      [ 1 0 0, 1 0 1, 0 0 1,  0 1 1, 1 1 0
      ]
    }
    colorPerVertex TRUE
    coordIndex
    [ 0 3 2 1 -1,  # bottom
      0 1 4 -1,    1 2 4 -1,  2 3 4 -1,  3 0 4 -1
    ]
  }
}
```



VRML: Grouping Nodes (1)

► Simplest one is Group

- Collects several children into a group
- Field 'children' contains those node

► Transformation node is similar to Group node

- Scales, rotates and translates (in that order) its children

► Billboard

- Always orients the local Z-axis to point to the viewer by rotating all children around specified axis
- Supports the display of objects that always face the viewer, e.g. "flat trees", signs, etc.



VRML: Grouping Nodes (2)

► Anchor node

- Loads another URL when the user clicks on any of the children nodes
- Replaces the current world

► Inline node

- Reads content of another URL and merges its nodes into the current world (similar to #include in C preprocessor)
- Does not replace the current world



VRML: Grouping Nodes (3)

► Switch

- Selects one amongst its children for display
- The 'whichChoice' field can be changed via events
- Useful e.g. for simple animation or state changes

► LOD (level of detail)

- Selects from several representations (levels) of the same object
- Switching depends on the distance from the viewer
- Switching thresholds are specified for each level
- Useful to increase rendering efficiency by displaying simpler representation for distant objects



VRML: Appearance Nodes

► Appearance nodes are container nodes for various surface properties

- Materials
- Textures

► Textures are specified as images

- **PixelTexture**: specifies the image in the VRML file
- **ImageTexture**: specifies the image by reference to an external file
- **MovieTexture**: time dependent texture loaded from an external MPEG-1 file



VRML: Lighting Models and Materials

► Lighting models and material properties are very similar to OpenGL

- Lights are placed in the scene like regular objects. The subject to standard transformations
- Check out the following nodes:
DirectionalLight, PointLight, SpotLight, Fog, and Material



VRML: Viewing and Navigation

► Viewpoint selection and navigation is primarily controlled by the browser

► Viewpoints can be specified in the VRML file

- Viewpoint node allows to predefine several nodes
- Viewpoints can be selected by the browser
- Viewpoints can be manipulated automatically by changing the parent transformation node

► Navigation specifies how the browser manipulates the viewpoint

- NavigationInfo node supports various modes, e.g. WALK, FLY, EXAMINE



VRML: Authoring and Viewing

- ▶ **Obviously, creating VRML files using a text editor is (at best) inconvenient**
 - The text-based format makes it easy to generate VRML through authoring applications, e.g. 3D editors, scientific visualizations etc.
- ▶ **VRML files are viewable through various tools**
- ▶ **Most popular viewers are known as VRML browser**
 - Plug-ins available for most Web-browser



Summary

- ▶ **Aliasing and Anti-aliasing**
 - Route cause is sampling below Nyquist frequency
 - Area-sampling is an implementation of low-pass filtering the image
 - Super-sampling and compositing
- ▶ **VRML**
 - Basic concepts
 - Syntactical elements
 - We have not covered advanced VRML features



Homework

- ▶ **Prepare for the midterm exam**
- ▶ **The exam is a closed book exam. You are allowed to bring 1 letter-sized sheet with notes.**
- ▶ **Read the lecture notes and the corresponding chapters in the textbook**
 - You must demonstrate understanding of the material and can apply it
 - Fully understand the polygon raster pipeline, i.e. sequence, function, and algorithms
 - You should be able to apply algorithms etc. Except in very simple cases, you do not need to derive formulae.
 - Exam questions will query knowledge, understanding and ability to use what you learned



Assignment

- ▶ **Create a VRML cityscape**
 - Streets, buildings, cars, people, trees, ...
- ▶ **Although not the preferred way, create the world from scratch, i.e. using a text editor**
- ▶ **There are very few requirements**
- ▶ **So ...**

go out, be wild, have some fun
- ▶ **And ...**

come back with a cool VRML world



Next Week ...

► Spring break !!!

