

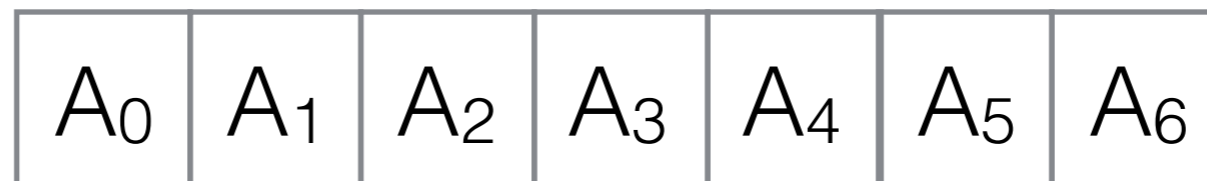
Data Structures in Java

Lecture 2: Array and Linked Lists.

9/9/2015

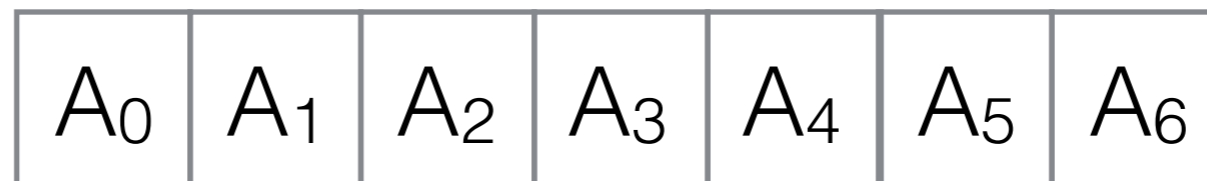
Daniel Bauer

The List ADT



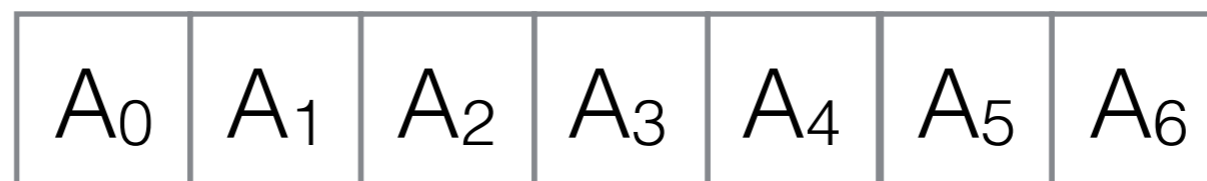
The List ADT

- A list L is a sequence of N objects $A_0, A_1, A_2, \dots, A_{N-1}$



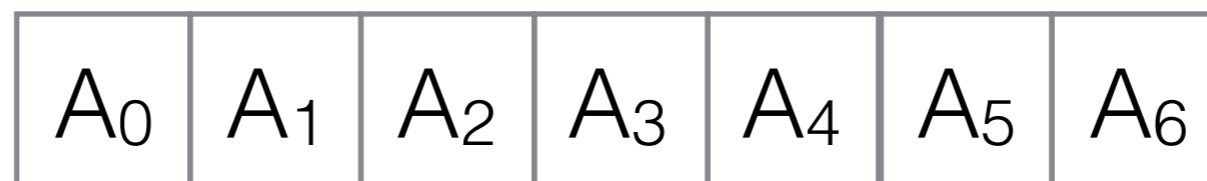
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- N is the length/size of the list. List with length $N=0$ is called the *empty list*.



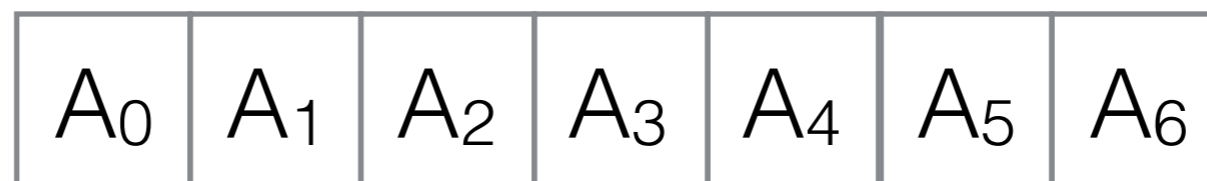
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- A_i *follows/succeeds* A_{i-1} for $i > 0$.

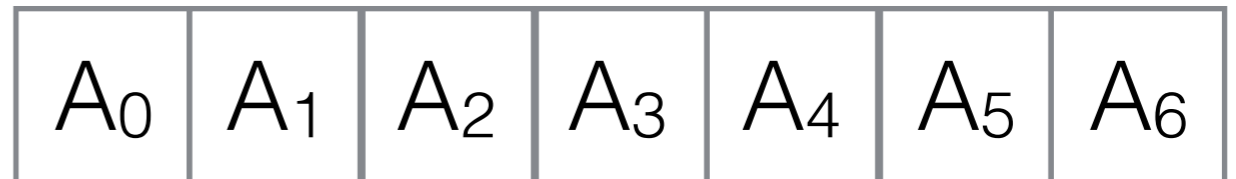


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- N is the length/size of the list. List with length $N=0$ is called the *empty list*.
- A_i *follows/succeeds* A_{i-1} for $i > 0$.
- A_i *precedes* A_{i+1} for $i < N$.

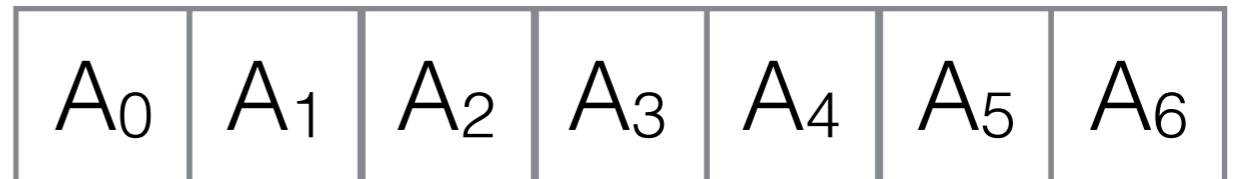


Typical List Operations



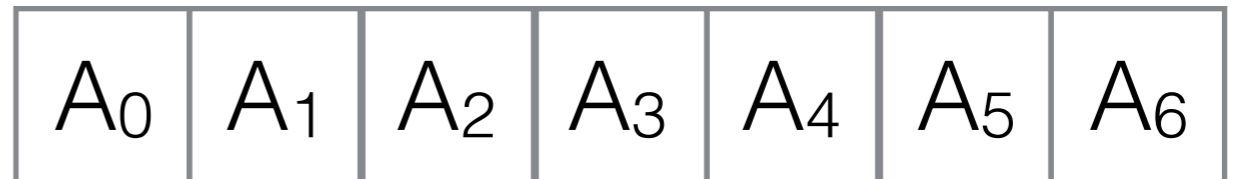
Typical List Operations

- `void printList()`



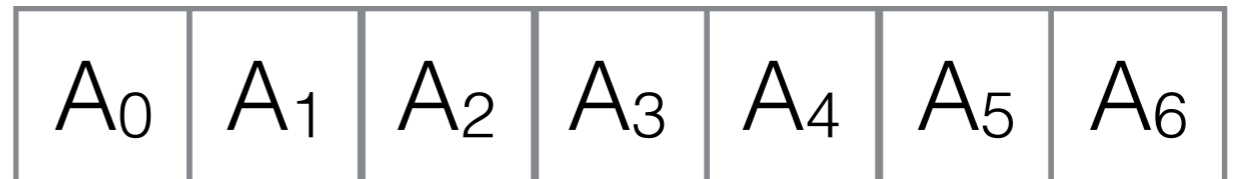
Typical List Operations

- `void printList()`
- `void makeEmpty()`



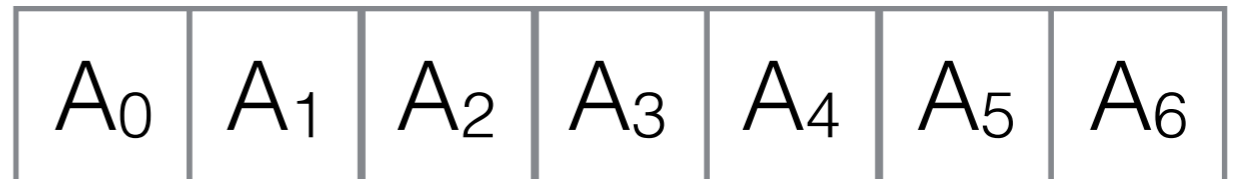
Typical List Operations

- `void printList()`
- `void makeEmpty()`
- `int size()`



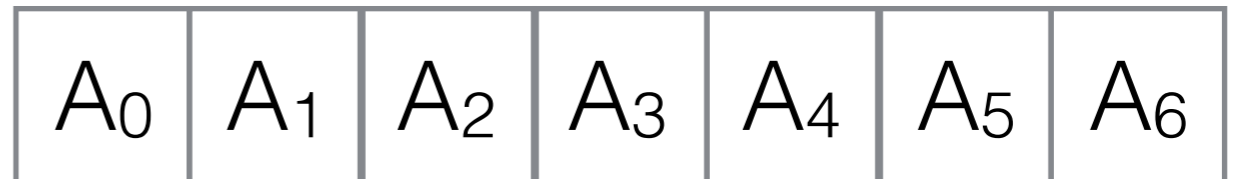
Typical List Operations

- `void printList()`
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- `int size()`
- `Object findKth(k) / get(k)`



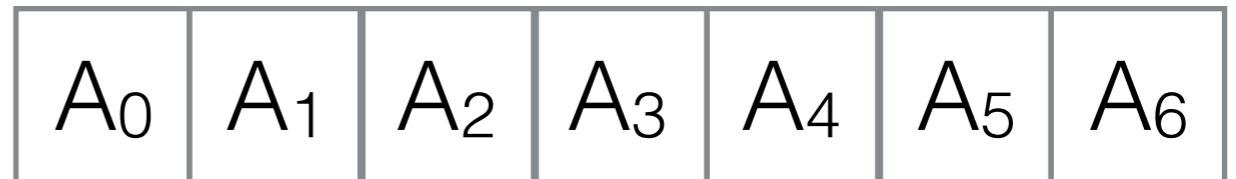
Typical List Operations

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- `Object findKth(k) / get(k)`
- `boolean insert(x, k), append(x)`



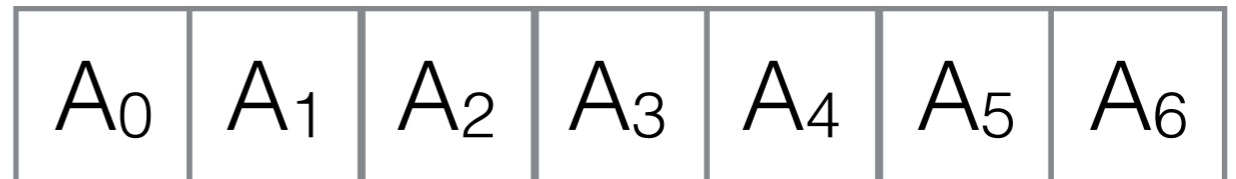
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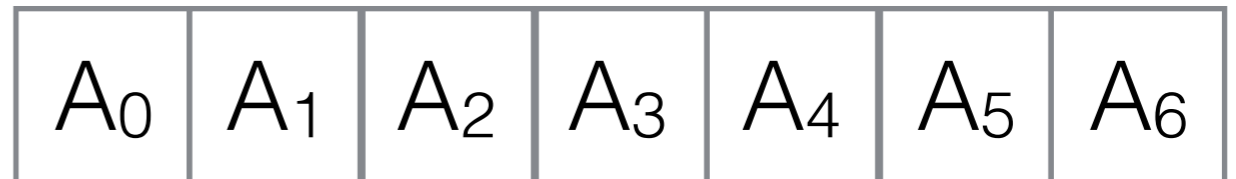
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- `boolean insert(x, k), append(x)`
- `boolean remove(k)`
- `int find(x) / indexOf(x)`



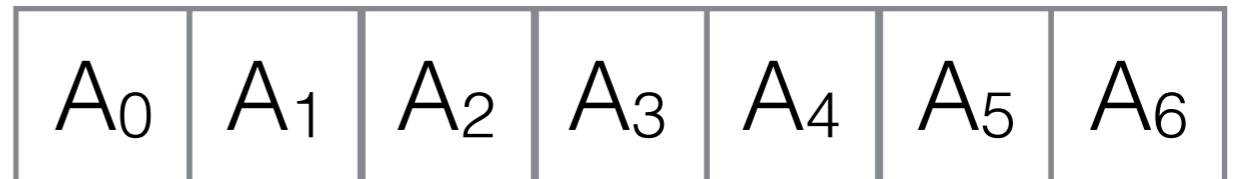
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- `Object findKth(k) / get(k)`
- `boolean insert(x, k), append(x)`
- `boolean remove(k)`
- `int find(x) / indexOf(x)`
- `Object next()`



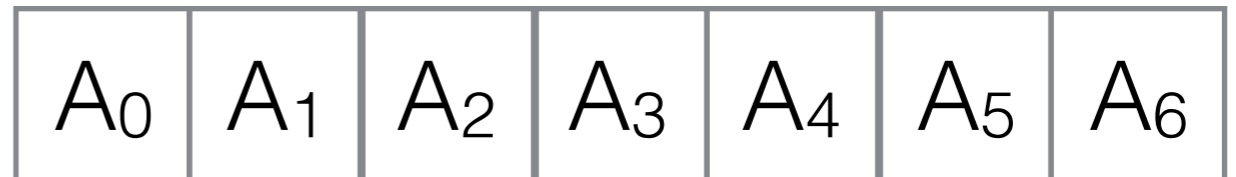
Typical List Operations

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- `Object next()`
- `Object previous()`



Typical List Operations

- `void printList()`
- `void makeEmpty()`
- `int size()`
- `Object findKth(k) / get(k)`
- `boolean insert(x, k), append(x)`
- `boolean remove(k)`
- `int find(x) / indexOf(x)`
- `Object next()`
- `Object previous()`
- `void removeCurrent()`



Array Lists

- Just a thin layer wrapping an array.

```
public class SimpleArrayList implements List{  
    public static final int DEFAULT_CAPACITY = 10;  
    private int theSize;  
    private Integer[] theItems;  
  
    public SimpleArrayList() {  
        theItems = new Integer[DEFAULT_CAPACITY];  
    }  
}
```

1	7	3	5	2	1	3			
---	---	---	---	---	---	---	--	--	--

Running Time for Array List Operations

1	7	3	5	2	1	3			
0	1	2	3	4	5	6	7	8	9

N=7

Operation	Number of Steps
printList	
find(x)	
findKth(k)	
insert(x,k)	
remove(x)	

Running Time for Array List Operations

1	7	3	5	2	1	3			
0	1	2	3	4	5	6	7	8	9

$N=7$

Operation	Number of Steps
printList	N
find(x)	N
findKth(k)	
insert(x,k)	
remove(x)	

Running Time for Array List Operations

1	7	3	5	2	1	3			
0	1	2	3	4	5	6	7	8	9

$N=7$

Operation	Number of Steps
printList	N
find(x)	N
findKth(k)	1
insert(x,k)	
remove(x)	

Array List: Insert/Remove

1	7	3	5	2	1	3			
0	1	2	3	4	5	6	7	8	9

N=7

insert(x,k)	
remove(x)	

Array List: Insert/Remove

1	7	3	5	2	1	3	5		
0	1	2	3	4	5	6	7	8	9

N=7

insert(5,7): 1 step

insert(x,k)	
remove(x)	

Array List: Insert/Remove

1	7	3	5	2	1	3			
0	1	2	3	4	5	6	7	8	9

N=7

insert(5,7): 1 step

remove(7): 1 step

best case

insert(x,k)	
remove(x)	

Array List: Insert/Remove

7 moves →

5	1	7	3	5	2	1	3		
0	1	2	3	4	5	6	7	8	9

N=7

insert(5,7): 1 step

remove(7): 1 step

best case

insert(5,0): 7 steps

worst case

insert(x,k)	
remove(x)	

Array List: Insert/Remove

7 moves →

5	1	7	3	5	2	1	3		
0	1	2	3	4	5	6	7	8	9

N=7

insert(5,7): 1 step

remove(7): 1 step

best case

insert(5,0): 7 steps

remove(0): O(N)

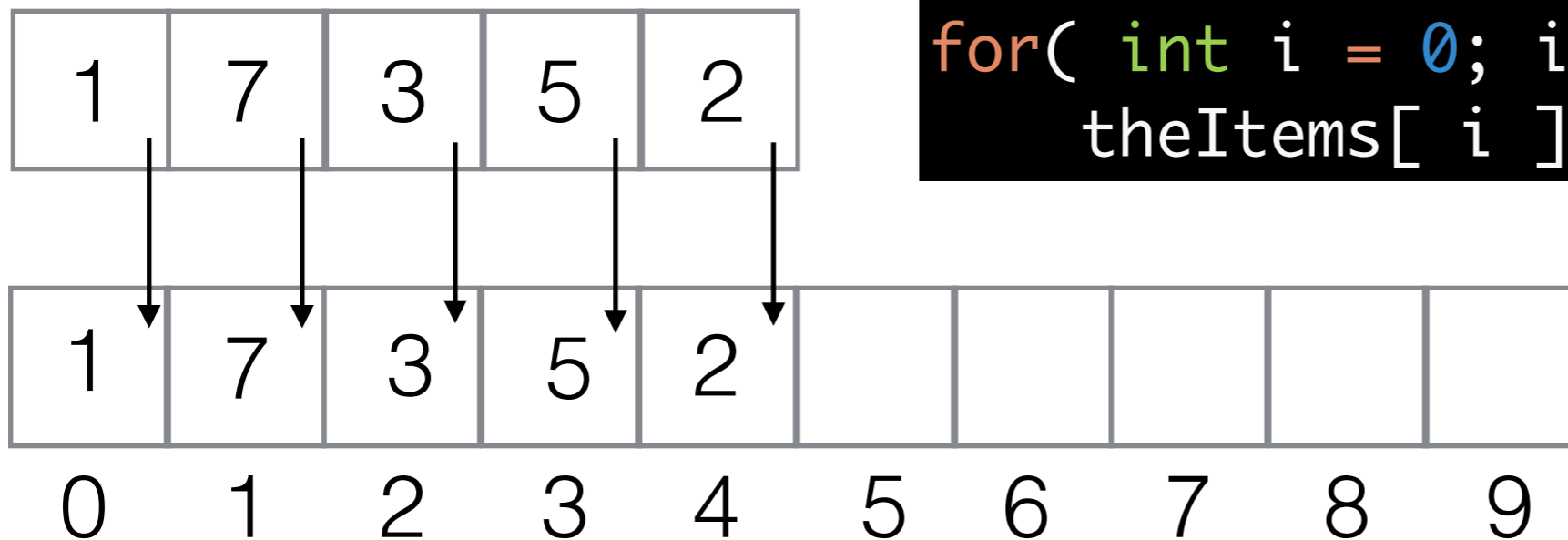
worst case

insert(x,k)	N
remove(x)	N

Expanding Array Lists

- What if we are running out of space during `append/insert`
- first copy all elements into a new array of sufficient size

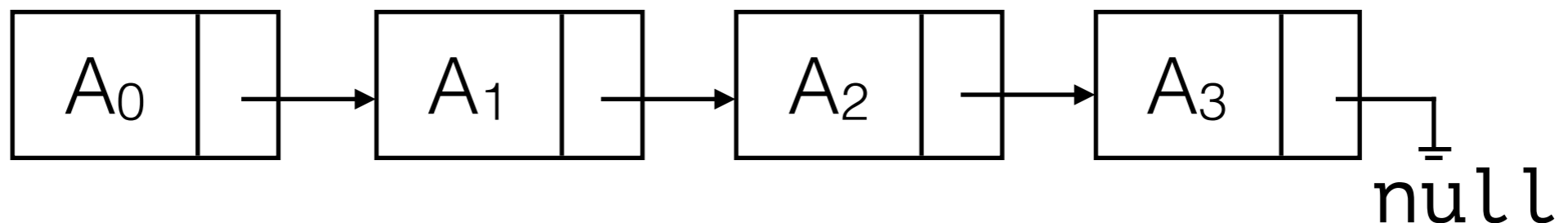
```
newCapacity = arr.length * 2;  
Integer[] old = theItems;  
theItems = new Integer[newCapacity];  
for( int i = 0; i < size(); i++ )  
    theItems[ i ] = old[ i ];
```



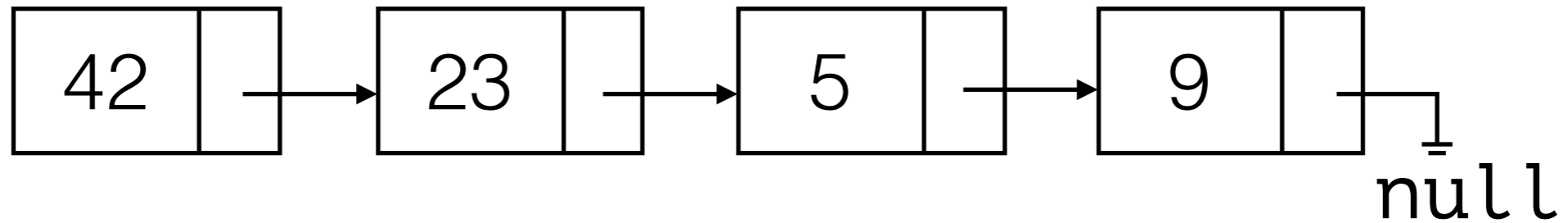
Simple Linked Lists

- Series of *Nodes*. Each *Node* contains:
 - A reference to the data object it contains.
 - A reference to the next node in the List.

```
public class Node {  
    public Integer data;  
    public Node next;  
    public Node(Integer d, Node n) {  
        data = d;  
        next = n;  
    }  
}
```

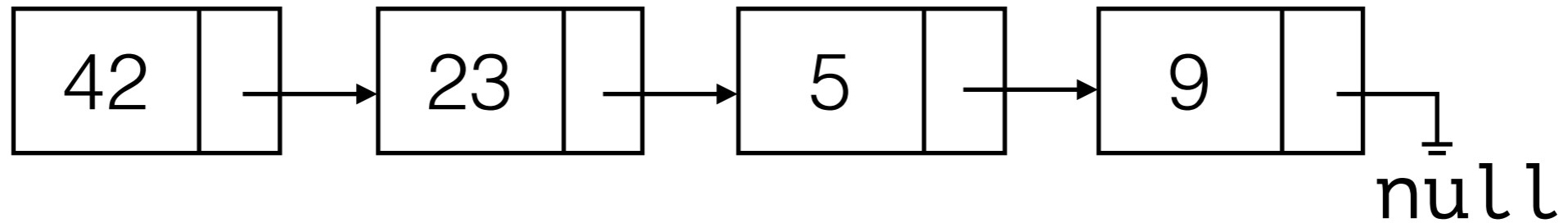


Running Time for Simple Linked List Operations



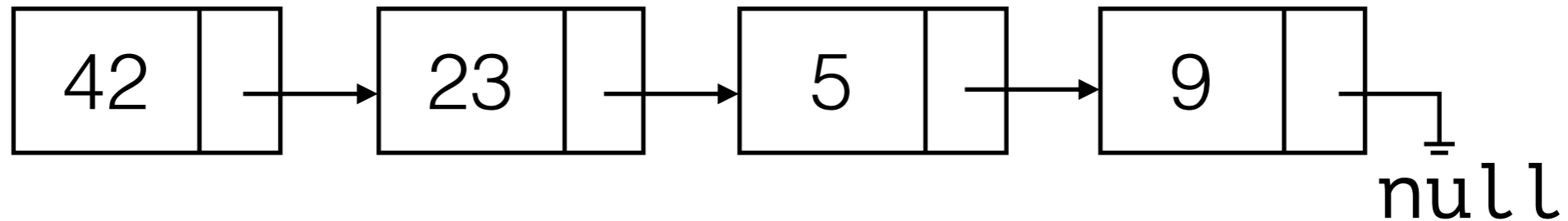
printList	
find(x)	
findKth(k)	
next()	

Running Time for Simple Linked List Operations



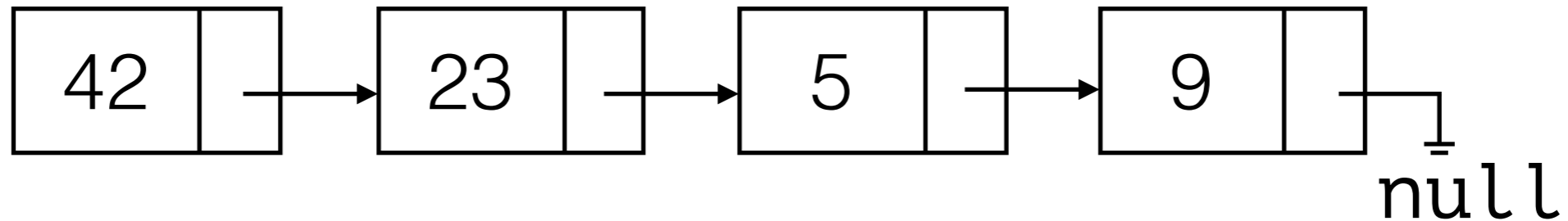
printList	N
find(x)	
findKth(k)	
next()	

Running Time for Simple Linked List Operations



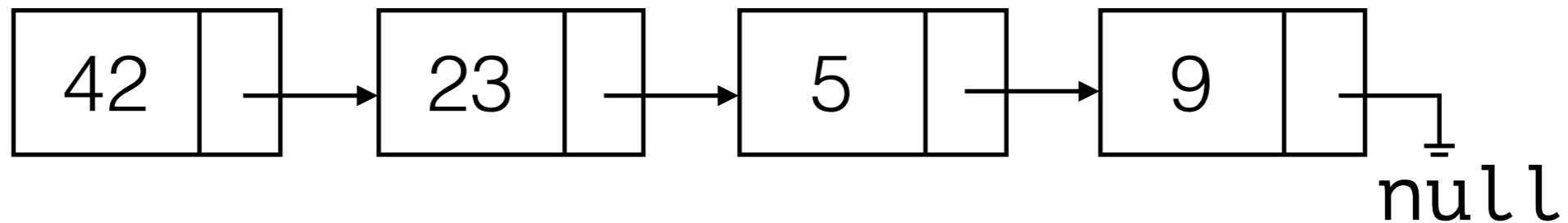
printList	N
find(x)	N
findKth(k)	
next()	

Running Time for Simple Linked List Operations



printList	N
find(x)	N
findKth(k)	k
next()	

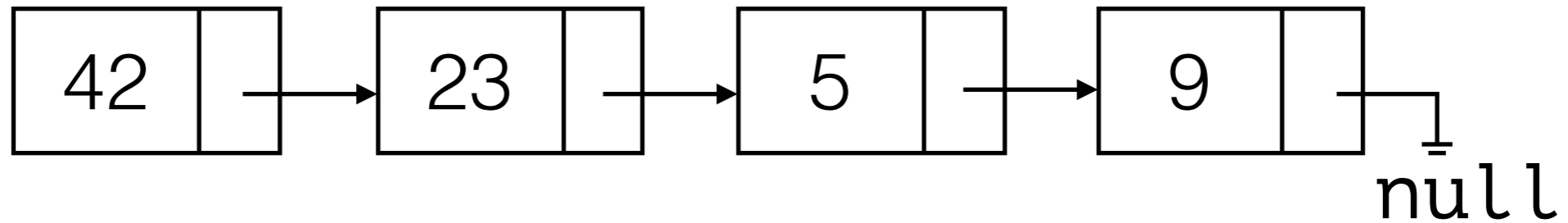
Running Time for Simple Linked List Operations



printList	N
find(x)	N
findKth(k)	k
next()	1

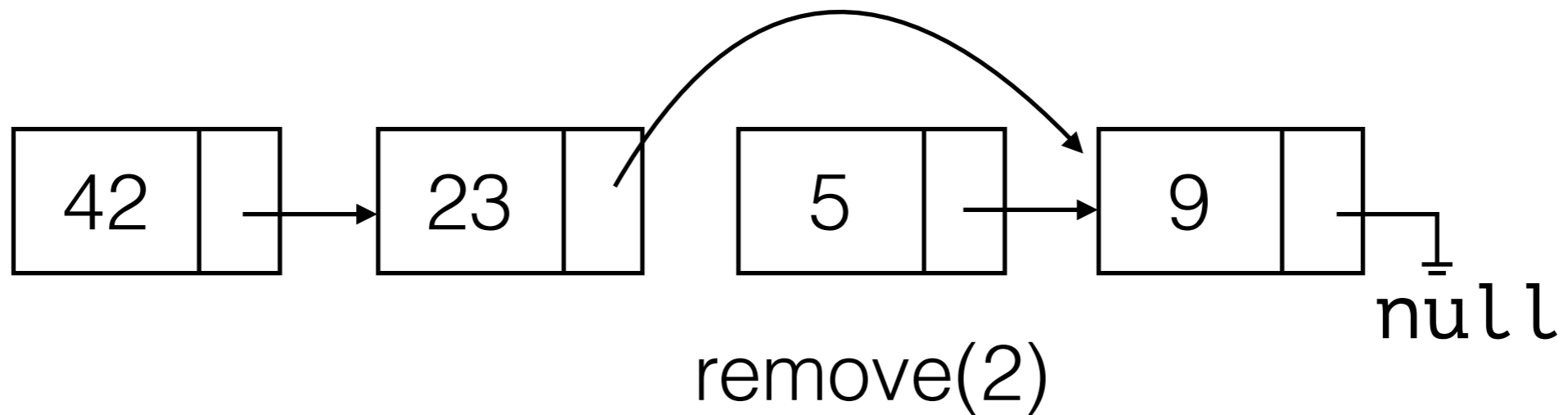
In many applications we can use next() instead of findKth(k).
(for every element in the list do... / filter the list ...)

Simple Linked List Removal



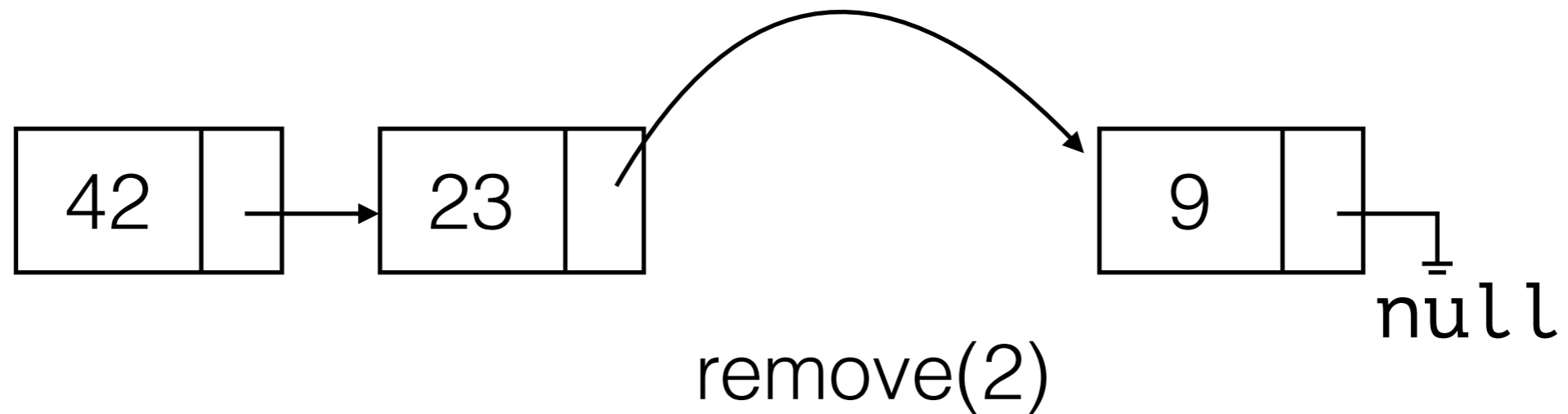
findKth(k)	k
next()	1
insert(x,k)	
remove(k)	

Simple Linked List Removal



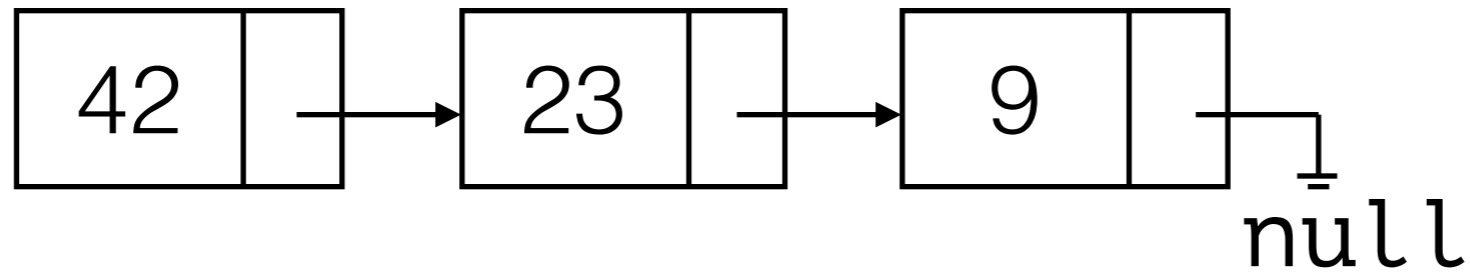
findKth(k)	k
next()	1
insert(x,k)	
remove(k)	search time + 1

Simple Linked List Removal



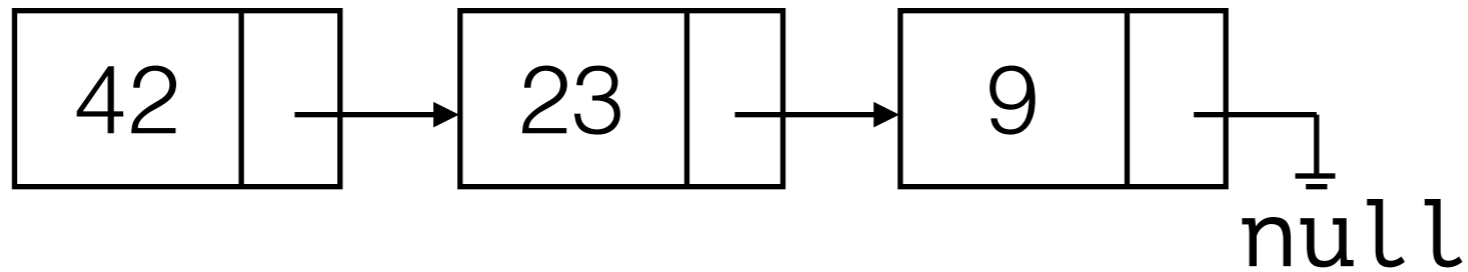
findKth(k)	k
next()	1
insert(x,k)	
remove(k)	search time + 1

Simple Linked List Insertion



insert(x,k)

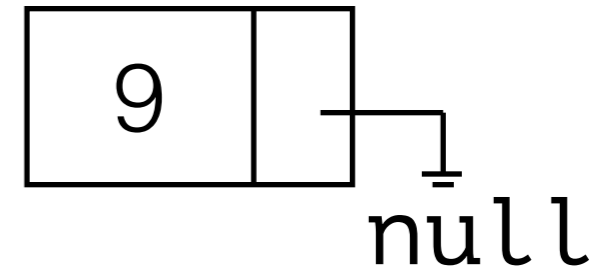
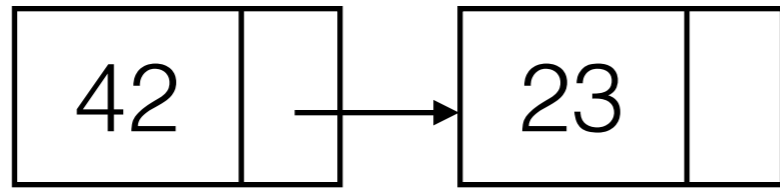
Simple Linked List Insertion



insert(5,2)



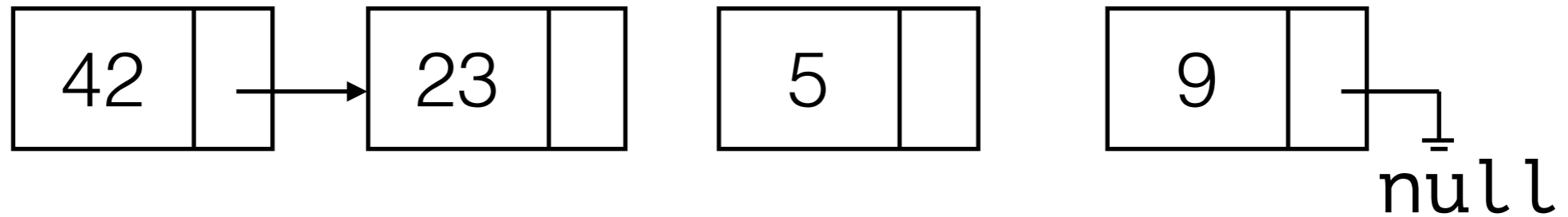
Simple Linked List Insertion



insert(5,2)



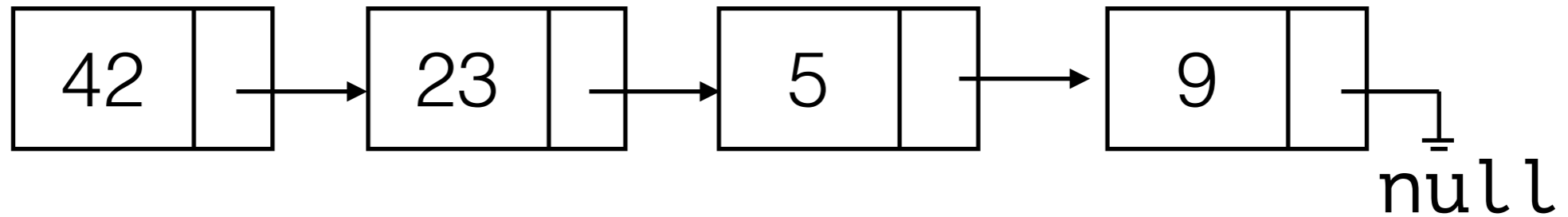
Simple Linked List Insertion



insert(5,2)



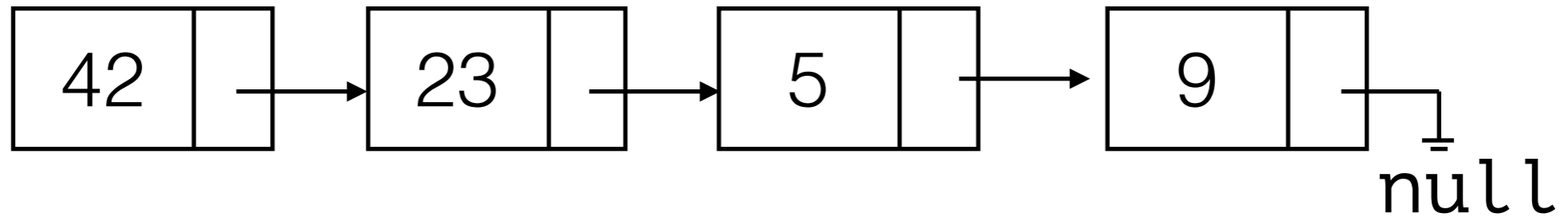
Simple Linked List Insertion



`insert(5,2)`



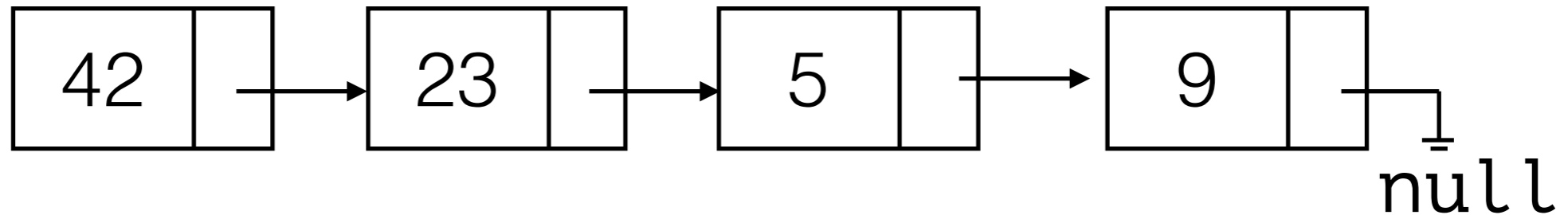
Simple Linked List Insertion



insert(5,2)

insert(x,k)	search time +1
-------------	----------------

Simple Linked List Insertion



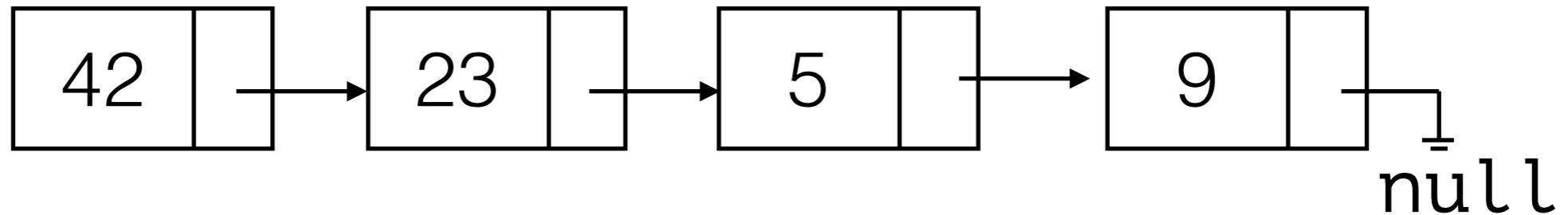
insert(5,2)



Inserting in position 0?

Inserting in position N-1?

Simple Linked List Insertion



insert(5,2)



Inserting in position 0?

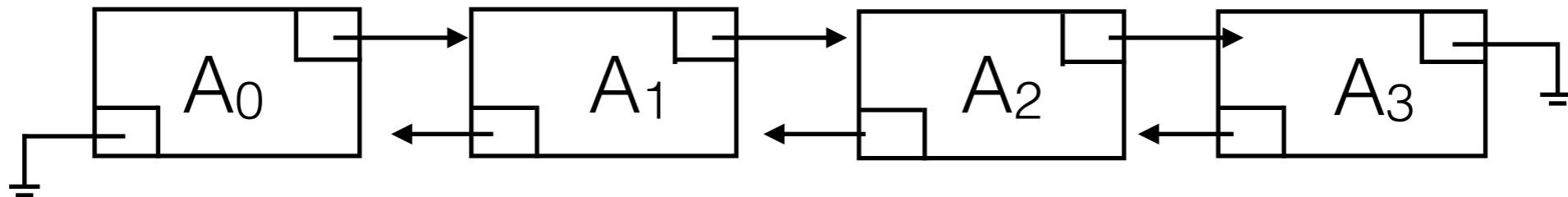
Inserting in position N-1?

Linked list should remember the first and last object.

Doubly Linked Lists

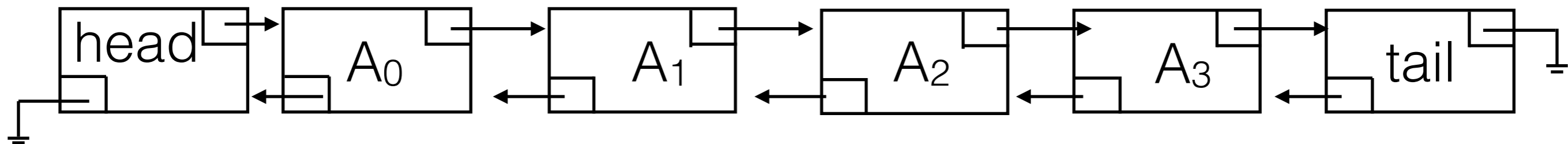
- Also maintain reference to previous node in the list.
- Speeds up append at end of list.

```
private class Node {  
    public Integer data;  
    public Node next;  
    public Node prev;  
    public Node(Integer d, Node n, Node p) {  
        data = d; next = n; prev = n;  
    }  
}
```



Doubly Linked List with Sentinel Nodes

- header node, tail node
- make implementation of `next` / `previous` easier.
- Remove other special cases
(e.g. removing first node/last node)



Empty Doubly Linked List with Sentinel Nodes

