

## This Can't Go On Forever

“A long time ago in a galaxy far, far away...”, so long ago, in fact, that the Empire did not exist and there were planets without space travel. In a far corner was a world in which the predominant pet, called *tayes*, reproduced by budding. Once a *taye* had separated from its parent, it took one time unit to mature to the point of breeding, which, coincidentally, was the length of time for a new bud to grow and separate from its parent. The *tayes* are extremely long-lived, so that it became important to investigate how many someone might have, assuming that at time zero the person did not have a *taye*, and at time one had acquired an immature one, freshly budded from the mature *taye* belonging to a friend.

This ends up giving the following recurrence:  $T(0) = 0$ ,  $T(1) = 1$ ,  $T(n) = T(n-1) + T(n-2)$ , for  $n > 1$ .

Computing at the time involved unsigned binary numbers with 24 bits. That motivated a particularly curious inhabitant, Leon, to investigate the series generated by that recurrence, but constrained by a modulus — and not just the modulo  $2^{24}$  forced by computing hardware. So the question becomes how long a series of number is generated by this recurrence, subject to arithmetic with a particular modulus, before it begins repeating. Here are the first few series:

Modulus	Front end of the series under that modulus	Length of the Period
2	<b>0 1 1</b> 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1	3
3	<b>0 1 1 2 0 2 2 1</b> 0 1 1 2 0 2 2 1 0 1 1 2 0 2 2	8
4	<b>0 1 1 2 3 1</b> 0 1 1 2 3 1 0 1 1 2 3 1 0 1 1 2 3	6
5	<b>0 1 1 2 3 0 3 3 1 4 0 4 4 3 2 0 2 2 4 1</b> 0 1 1	20

The problem is to determine the length of the period for each modulus given in the input file and report it.

### Input

The input file contains an indeterminate number of lines, each containing a single integer *mod* guaranteed to be in the range  $2 \leq \text{mod} \leq 16777216$  ( $2^{24}$ ). The final line contains a 0 as end of data and should not be processed.

### Output

For each modulus in the input file, print the modulus, one blank, and then the size of the smallest period of these *T* numbers under that modulus.

#### Sample Input

```
2
3
4
5
6
12345678
16777216
0
```

#### Sample Output

```
2 3
3 8
4 6
5 20
6 24
12345678 700512
16777216 25165824
```

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far away....