St. Joseph's College
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## G • Area of Polycubes

A polycube is a solid made by gluing together unit cubes (one unit on each edge) on one or more faces. The figure in the lower-left is not a polycube because some cubes are attached along an edge.


For this problem, the polycube will be formed from unit cubes centered at integer lattice points in 3 -space. The polycube will be built up one cube at a time, starting with a cube centered at ( $\mathbf{0}, \mathbf{0}, \mathbf{0}$ ). At each step of the process (after the first cube), the next cube must have a face in common with a cube previously included and not be the same as a block previously included. For example, a 1-by-1-by-5 block (as shown above in the upper-left polycube) could be built up as:
$(0,0,0)(0,0,1)(0,0,2)(0,0,3)(0,0,4)$
and a 2-by-2-by-2 cube (upper-right figure) could be built as:
$(0,0,0)(0,0,1)(0,1,1)(0,1,0)(1,0,0)(1,0,1)(1,1,1)(1,1,0)$


Since the surface of the polycube is made up of unit squares, its area is an integer.
Write a program which takes as input a sequence of integer lattice points in 3 -space and determines whether is correctly forms a polycube and, if so, what the surface area of the polycube is.

## Input

The first line of input contains a single integer $\boldsymbol{N},(1 \leq \boldsymbol{N} \leq 1000)$ which is the number of data sets that follow. Each data set consists of multiple lines of input. The first line contains the number of points $\boldsymbol{P}$, $(1=\boldsymbol{P}=100)$ in the problem instance. Each succeeding line contains the centers of the cubes, eight to a line (except possibly for the last line). Each center is given as 3 integers, separated by commas. The points are separated by a single space.

## Output

For each data set, you should generate one line of output with the following values: The data set number as a decimal integer (start counting at one), a space and the surface area of the polycube if it is correctly formed, OR, if it is not correctly formed, the string "NO" a space and the index (starting with 1) of the first cube which does not share a face with a previous cube. Note that the surface area includes the area of any included holes.

| Sample Input | Sample Output |
| :---: | :---: |
| 4 | 122 |
| 5 | 224 |
| $0,0,00,0,10,0,20,0,30,0,4$ | 3 NO 3 |
| 8 | 472 |
| $0,0,00,0,10,1,00,1,11,0,01,0,11,1,01,1,1$ |  |
| 4 |  |
| 0,0,0 0,0,1 1,1,0 1,1,1 |  |
| 20 |  |
| 0,0,0 0,0,1 0,0,2 0,1,2 0,2,2 0,2,1 0,2,0 0,1,0 |  |
| 1,0,0 2,0,0 1,0,2 2,0,2 1,2,2 2,2,2 1,2,0 2,2,0 |  |
| 2,1,0 2,1,2 2,0,1 2,2,1 |  |

