# The SR Domain

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## Fixed-point Semantics are Natural for Synchronous Specifications with Feedback





## Unique Least Fixed Point Theorem

Recall:

A monotonic function on a complete partial order (with  $\perp$ ) has a unique least fixed point.

What does it mean to make the system function f monotonic and the signal values a CPO?





# **Monotonic Block Functions**

Giving a more defined input to a monotonic function always gives a more defined output.



Formally,  $x \sqsubseteq y$  implies  $f(x) \sqsubseteq f(y)$ .

A monotonic function never recants ("changes its mind").



### A Simple Way to Find the Least Fixed Point

$$\perp \sqsubseteq f(\perp) \sqsubseteq f(f(\perp)) \sqsubseteq \cdots \sqsubseteq \mathsf{LFP} = \mathsf{LFP} = \cdots$$

For each instant,

- 1. Start with all signals at  $\perp$
- 2. Evaluate all blocks (in some order)
- 3. If any change their outputs, repeat Step 2



$$(a,b,c) = (\bot,\bot,\bot)$$
  

$$f_0(\bot,\bot,\bot) = (0,\bot,\bot)$$
  

$$f_1(0,\bot,\bot) = (0,1,\bot)$$
  

$$f_2(0,1,\bot) = (0,1,0)$$
  

$$f_2(f_1(f_0(0,1,0))) = (0,1,0)$$







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### Conclusions

- Deterministic specification scheme combining synchrony and heterogeneity
- Semantics: the least fixed point of a continuous function on a CPO
- Iterative execution scheme based on recursive divide-and-conquer
- Exact scheduling practical for small graphs
- Heuristic practical for very large graphs
- Execution time for random graphs growing slower than  $n^{1.5}$