# Haskell Computer Algebra System 

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## Outline

- Tutorial
- Implementation
- Looking Back


## Tutorial: Language Summary

HCAS is a subset of Haskell, plus support for computer algebra.

- Purely functional language
- Construction of mathematical expressions
- Navigation of mathematical expressions


## Tutorial: Running HCAS

\$ echo "main = 7" | ./hcasi
7
\$

## Tutorial: Hello World!

The HCAS Hello World program:
main = "Hello World!"

Output: "Hello World!"

## Tutorial: Basic Data Types

- Number - integer and floating point types for numbers
- Character - single printable character
- List - contains zero or more elements
- String - list of characters


## Tutorial: Numbers

Numbers represent integers or floating point types:

$$
\operatorname{main}=7.5
$$

Output: 7.5

## Tutorial: Strings

Strings represent a list of characters:
main = "Hello World!"

Output: "Hello World!"

## Tutorial: Lists

Lists represent zero or more items:

$$
\text { main }=[1,2,3,4,5]
$$

Output: [1,2,3,4,5]

## Tutorial: Operators

- Math operators - addition, subtraction, multiplication, etc. For basic math.
- List operators - the " ++ " operator concatenates two lists.


## Tutorial: Math Operators

Math operators follow normal rules of associativity and precedence:

$$
\operatorname{main}=2+3 * 4
$$

Output: 14

## Tutorial: List Operators

The concatenation operator lets you concatenate two lists:

$$
\text { main }=[1,2,3]++[4,5]
$$

Output: [1,2,3,4,5]

## Tutorial: Functions

Functions represent callable HCAS expressions:

- Zero or more input arguments.
- Applicative-order evaluation.
- Strict evaluation


## Tutorial: Calling a Function, No Arguments

Calling a function with zero arguments:

$$
\begin{aligned}
& \text { foo }=7 \\
& \text { main }=\text { foo }
\end{aligned}
$$

Output: 7

## Tutorial: Calling a Function, w/ Arguments

Calling a function with one or more arguments:

```
add(x, y) = x + y
main = add(3,4)
```

Output: 7

## Tutorial: Function List Patterns

The colon operator in a function argument creates a list pattern:

```
reverse(x:xs) = reverse(xs) ++ [x]
reverse([]) = []
main = reverse("Hello World!")
```

Output: "!dlroW olleH"

## Tutorial: Math Expression Data Type

If an identifier does not match a function name, it represents a mathematical expression:

$$
\operatorname{main}=\mathrm{x}+\mathrm{y}
$$

Output: $x+y$

## Tutorial: Math Expression Data Type

A math expression is stored as a tree, using the normal rules of precedence and associativity:

$$
\operatorname{main}=\mathrm{a} * \mathrm{~b}+\mathrm{c}-\mathrm{d}
$$





## Tutorial: Function Math Patterns

You can put any math operators in a function argument. These create math patterns:

$$
\begin{aligned}
& \text { printType }(x+y)=\text { "addition" } \\
& \text { printType }(x-y)=\text { "subtraction" } \\
& \text { main }=\text { printType }(a * b+c)
\end{aligned}
$$

Output: "addition"
(In the call to printType, $x$ refers to "a*b" and $y$ refers to "c".)



## Tutorial: Let Expressions

Let expressions create a new scope:

```
main =
    let
    \(x=7\)
    \(\mathrm{y}=8\)
    \(\operatorname{add}(\mathrm{a}, \mathrm{b})=\mathrm{a}+\mathrm{b}\)
    in
        \(\operatorname{add}(\mathrm{x}, \mathrm{y})\)
```

Output: 15

## Tutorial: Derivative Example

```
main = derivative(3*x^2+2*x)
derivative(a+b) = derivative(a) + derivative(b)
derivative(a-b) = derivative(a) - derivative(b)
derivative(c*x^e) = c*e*simplify(x^(e-1))
derivative(c*x) = c
derivative(x) = 0
simplify(x^1) = x
simplify(x^0) = 1
simplify(x+0) = x
simplify(0+x) = x
simplify(x+y) = simplify(x) + simplify(y)
simplify(x-y) = simplify(x) - simplify(y)
simplify(x) = x
```

Output: $6^{*} x+2$

## Tutorial: Questions?

Any questions on the language?

## Implementation: Technologies

- Haskell - the entire interpreter is written in Haskell, using the Glasgow Haskell Compiler, v 6.6.1.
- HUnit - a unit testing framework, similar to JUnit and NUnit.
- Parsec - a monadic parsing library for top-down parsing.


## Implementation: Haskell Modules

- AST.hs - contains the abstract syntax tree.
- Parser.hs - contains the parsing code. Takes an input string, and returns an AST.
- Interpreter.hs - contains the interpreter code.
- MainInterpreter.hs - contains the main bootup code (reading from stdin, writing to stdout).


## Implementation: AST.hs

```
data Block = Block [Statement]
data Statement = Function String [Expression] Expression
data Expression =
    -- Strings and lists.
    List [Expression]
    | Concat Expression Expression
    | ListPattern [Expression]
    | CharValue Char
    -- Function-related items
    | Call String [Expression]
    | Let Block Expression
```


## Implementation: Parser.hs

```
identifier :: Parser String
identifier =
    do {
        c <- letter;
        cs <- many (identifierChar);
        return (c:cs);
    }
identifierChar =
    do {
    (alphaNum <|> char '_');
    }
```


## Implementation: Interpreter.hs

```
interpret :: [Block] -> Expression -> Expression
interpret _ (Number n) = (Number n)
interpret blocks (Let block expr) =
    (interpret ([block] ++ blocks) expr)
interpret blocks (Addition left right) =
        (addition left' right')
        where
        left' = (interpret blocks left)
        right' = (interpret blocks right)
        addition (Number n1) (Number n2) = (Number (n1 + n2))
        addition left'' right'' = (Addition left'' right'')
```


## Implementation: MainInterpreter.hs

```
main =
    do {
        script <- getContents;
        case (parse file "" script) of
        (Right parsed) ->
            do {
                        interpreted <- return (interpretFile parsed);
                        putStrLn (showHCAS interpreted);
            }
            (Left err) ->
        do {
        putStrLn (show err);
        }
}
```


## Implementation: Unit Testing

Unit testing used to verify functionality. Three types of tests:

- Haskell unit tests
- HCAS boolean unit tests
- HCAS expected vs. actual unit tests


## Implementation: Haskell Unit Tests

Haskell unit tests are writing using Haskell:

```
testNum2 = TestCase (
    do {
        expected <- return (Number 1.3);
        (Right actual) <- return (parse numberAtom "" "1.3");
        assertEqual "testNum2" expected actual;
        }
    )
```


## Implementation: HCAS Boolean Unit Tests

HCAS boolean tests are HCAS scripts that must return a boolean true value:

$$
\operatorname{main}=7==1+2+4
$$

Output: True

## Implementation: HCAS Expected vs. Actual Unit Tests

HCAS expected vs. actual tests have an HCAS script and expected output file for each test:

addition.hcas<br>addition_expected.txt<br>subtraction.hcas<br>subtraction_expected.txt<br>functioncall.hcas<br>functioncall_expected.txt<br>...

## Implementation: Questions?

Any questions on the implementation?

## Looking Back

- Haskell works well for parsing. Parsec is fun.
- Professor is right - get started early.
- I wish I wrote a compiler (instead of an interpreter). I missed out on generation of IR and assembly code.
- If I had more time, I would add static typing.


## Questions?

## Any final questions?

