# **Foundations of Graphical Models**

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## Today's lecture

- Logistics, especially pertaining to enrollment
- What is this course about?
- Latent Dirichlet allocation: An example of a graphical model
- Other examples of applied probabilistic modeling
- Box's loop
- What will we cover?
- Prerequisites, requirements, and grades

## Enrollment

Logistics

- This room holds 54 people.
- Please fill out the Google form at http://www.cs.columbia.edu/~blei/fogm/

Note

- This course will be offered every Fall.
- We will consider expanding it in the future.

What is this course about?

Latent Dirichlet Allocation (An example of a model that I know well)

#### Seeking Life's Bare (Genetic) Necessities

Haemonhiluy

genome 1703 genes

COLD SPRING HARBOR, NEW YORK-How many genes does an organism need to survive! Last week at the genome meeting here," two genome researchers with radically different approaches presented complementary views of the basic genes needed for fifte One research team, using computer analyses to compare known genomes, concluded that today's organism can be sustained with just 250 genes, and that the earliest life forms

required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough.

Although the numbers don't match precisely, those predictions

\* Genome Mapping and Sequencing, Cold Spring Harbor, New York, May 8 to 12.

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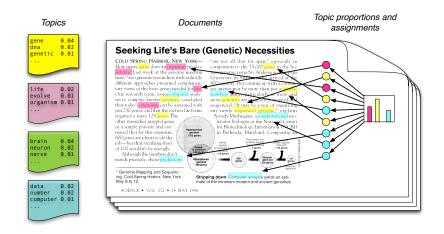
"are not all that far apart," especially in comparison to the 75.000 genes in the human genome, notes Six Andersson of Uppsala University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely mapped and sequenced. "It may be a way of organizing any newly sequenced genome." explains Arcady Mushegian, a computational mo-

lecular biologist at the National Center for Biotechnology Information (NCBI) in Bethesda, Maryland. Comparing an

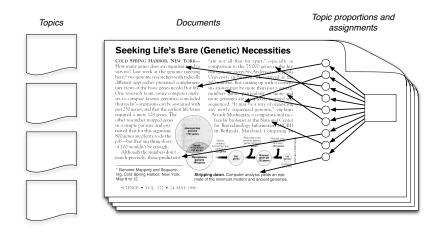


mate of the minimum modern and ancient genomes.

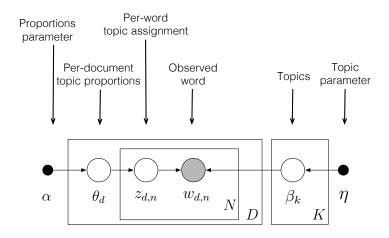
#### Documents exhibit multiple topics.



#### Latent Dirichlet Allocation

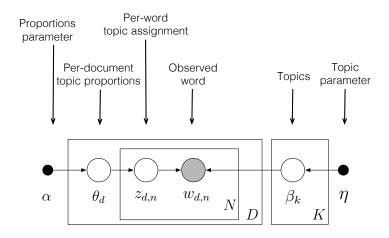


#### Latent Dirichlet Allocation



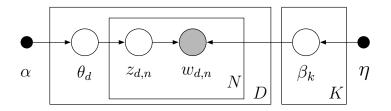
#### LDA as a graphical model

- Nodes are random variables; edges indicate dependence.
- Shaded nodes are observed; unshaded nodes are hidden.
- Plates indicate replicated variables.



#### LDA as a graphical model

- Encodes independence assumptions
- Defines a factorization of the joint distribution
- Connects to algorithms for computing with data



- The joint defines a posterior,  $p(\theta, z, \beta \mid w)$ .
- From a collection of documents, infer
  - Per-word topic assignment z<sub>d,n</sub>
  - Per-document topic proportions  $\theta_d$
  - Per-corpus topic distributions  $\beta_k$
- Then use posterior expectations to perform the task at hand: information retrieval, document similarity, exploration, and others.



- Data: The OCR'ed collection of Science from 1990–2000
  - 17K documents
  - 11M words
  - 20K unique terms (stop words and rare words removed)
- Model: 100-topic LDA model using variational inference.

#### Seeking Life's Bare (Genetic) Necessities

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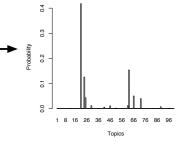
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human genome dna genetic genes sequence gene molecular sequencing map information genetics mapping project sequences

evolution evolutionary species organisms life origin biology groups phylogenetic living diversity group new two common

disease host bacteria diseases resistance bacterial new strains control infectious malaria parasite parasites united tuberculosis

computer models information data computers system network systems model parallel methods networks software new simulations

perspective identifying tumor suppressor genes in human... letters global warming report leslie roberts article global.... research news a small revolution gets under way the 1990s.... a continuing series the reign of trial and error draws to a close... making deep earthquakes in the laboratory lab experimenters... quick fix for freeways thanks to a team of fast working... feathers fly in grouse population dispute researchers...

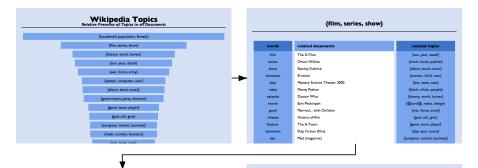
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docs <- read.documents("mult.dat")
K <- 20
alpha <- 1/20
eta <- 0.001
model <- lda.collapsed.gibbs.sampler(documents, K, vocab, 1000, alpha, eta)</pre>

1	2	3	4	5
dna	protein	water	says	mantle
gene	' cell	climate	researchers	high
sequence	cells	atmospheric	new	earth
genes	proteins	temperature	university	pressure
sequences	receptor	global	just	seismic
human	fig	surface	science	crust
genome	binding	ocean	like	temperature
genetic	activity	carbon	work	earths
analysis	activation	atmosphere	first	lower
two	kinase	changes	years	earthquakes
6	7	8	9	10
end	time	materials	dna	disease
article	data	surface	rna	cancer
start	two	high	transcription	patients
science	model	structure	protein	human
readers	59	temperature	site	gene
service	ayatem	molecules	binding	medical
news	number	chemical	sequence	studies
card	different	molecular	proteins	drug
circle		fg	specific	normal
letters		university	sequences	drugs
11	12	13	14	15
vears	species	protein	14 Cells	15 space
11 years million		protein structure		space solar
vears	species	protein	Cells cell virus	space
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#### Stanley Kubrick



related topics (film, series, show) (theory, work, human) (son, year, death) (black, white, people) (god, call, give) (math, energy, light) Standarg Kuberick (bi) 26, (192–14nrb, 7, (199) was an American IIII direction, writes produced and photographic who hold in Eighted during most of the air stronghost areas with which has been shared as a strong method of warding, the warley of genres ha worked in, its technical performances and the reducement about the schemical performance and the schemical performance confines and the Lollynewed sparse, maintaining almost complexe artistic control and multicing most according to his own when and these constraints, but with the rare schemerse.

Kubrick's films are characterized by a formal visual spie and meticulous attention to detail—his later films often have elements of surrealism and expressionism that excheme structured linear narratives. His films are repeatedly described as a low and methodical, and are often proceeving as a reflection of his obsessive and perfectionist nazare.<sup>[1]</sup> A recorring theme in his films is mark inhumanity to man. While often viewed as

#### related decuments Orace Walks Brook Mapsory Science Theater 1990 Decem Walks The A Team The A Team Note Trackingsh The A Team The A Team

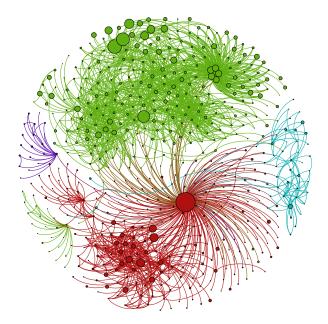
#### {theory, work, human}

words	related documents	related topics
theory	Meme	{work, book, publish}
work	Intelligent design	{law, state, case}
human	Immanuel Kant	{son, year, death}
idea	Philosophy of mathematics	{woman, child, man}
term	History of science	{god, call, give}
study	Free will	{black, white, people}
view	Truth	(film, series, show)
science	Psychoanalysis	{war, force, army}
concept	Charles Peirce	(language, word, form)
form	Existentialism	(@card@, make, design)
world	Deconstruction	(church, century, christian)
argue	Social sciences	{rate, high, increase}
social	Idealism	(company, market, business)

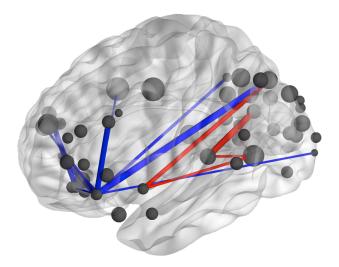
1	2	3	4	5
game	life	film	book	wine
season	know	movie	life	street
team	school	show	books	hotel
coach	street	life	novel	house
play	man	television	story	room
points	family	films	man	night
games	says	director	author	place
giants	house	man	house	restaurant
second	children	story	war	park
players	night	says	children	garden
6	7	8	9	10
bush	building	won	yankees	government
campaign	street	team	game	war
clinton	square	second	mets	military
republican	housing	race	season	officials
house	house	round	run	iraq
party	buildings	cup	league	forces
democratic	development	open	baseball	iraqi
political	space	game	team	army
democrats	percent	play	games	troops
senator	real	win	hit	soldiers
11	12	13	14	15
children	stock	church	art	police
school	percent	war	museum	yesterday
women	companies	women	show	man
family	fund	life	gallery	officer
parents	market	black	works	officers
child	bank	political	artists	case
life	investors	catholic	street	found
says	funds	government	artist	charged
help	financial	jewish	paintings	street
mother	business	pope	exhibition	shot

Topics found in 1.8M articles from the New York Times

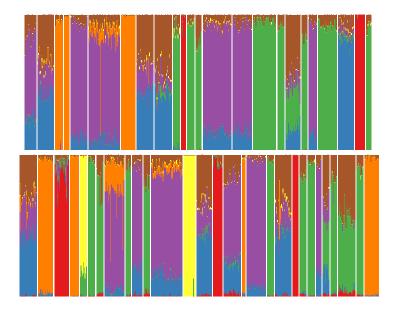
Other examples of applied probabilistic modeling (from my research group and others)



Communities discovered in a 3.7M node network of U.S. Patents



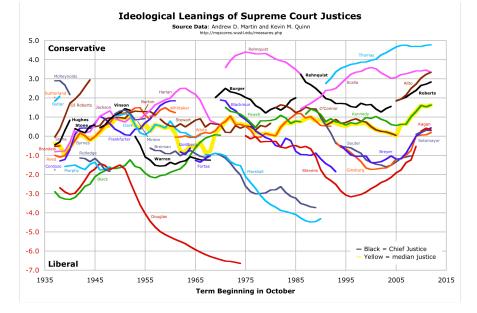
## Neuroscience analysis of 220 million fMRI measurements



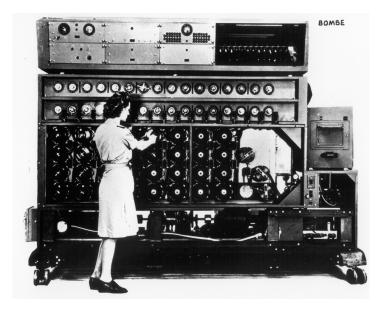
Population analysis of 2 billion genetic measurements



Patterns of preferences found at Etsy.com (Hu et al., 2014)

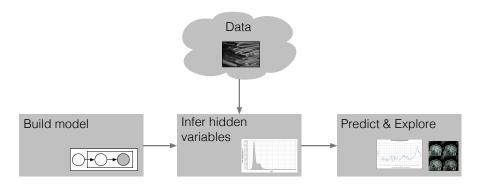


Supreme Court Ideology over time (Martin and Quinn, 2001)



Breaking the Nazi code (Turing and Good, 194?)

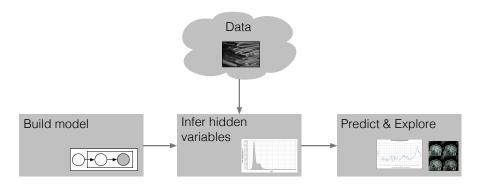
# Box's Loop



#### Why we like this picture:

- Customized data analysis is important to many fields.
- This pipeline separates assumptions, computation, application.
- It facilitates solving data science problems.

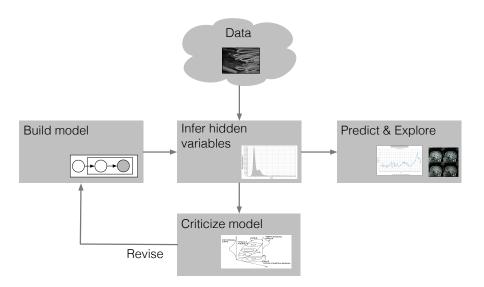
# Box's Loop



#### What we need:

- Expressive components from which to build models
- Scalable and generic inference algorithms
- Stretch probabilistic modeling into new areas

# Box's Loop



What will we cover?

### The basics of graphical models

- · Basic concepts in probability; the semantics of graphical models
- D-separation and conditional independence in graphical models
- Message passing, tree propagation, and a word about the junction tree

## Using probability models to analyze data

- Probability models, data, and statistical concepts
- Bayesian mixtures of Gaussians and why we need approximate inference
- Markov chain Monte Carlo sampling and the Gibbs sampler
- The exponential family, conjugacy, and mixtures of exponential families
- Variational inference (and a word about expectation maximization)

## The building blocks of complex models

- Mixtures and mixed membership models (including topic models)
- Matrix factorization: Gaussian, Poisson, exponential family
- Time series models: Hidden Markov models and state-space models
- Spatial models
- Regression: Linear and logistic, generalized linear models, regularization
- Bayesian nonparametrics I: Clustering models
- Bayesian nonparametrics II: Latent feature models
- Bayesian nonparametrics III: Gaussian processes

### **Advanced topics**

- Scalable inference with stochastic variational inference
- Model checking and revision with posterior predictive checks
- Hierarchical models, multi-level models, empirical Bayes
- Causal inference and probabilistic modeling (a rabbit hole)

### Some additional discussion

- Programming languages
- Applications
- Box's loop, again
- Note: We will usually be at the board.

## Prerequisites, Requirements, Grades, Etc.

- http://www.cs.columbia.edu/~blei/fogm/
- Office hours: Wednesdays 2:30-4:00, 703 CEPSR
- Prerequisites
  - Probability and Statistics
  - Optimization
  - Programming
- Requirements
  - Weekly paper about the reading (< 1 page)
  - Final project
- Your grade: Mostly the final project